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Inter-Subject Variability of Skull Conductivity and Thickness in Calibrated Realistic Head Models



Marios Antonakakis ^{a,*}, Sophie Schrader ^a, Ümit Aydin ^{a,b}, Asad Khan ^a, Joachim Gross ^{a,c,d}, Michalis Zervakis ^e, Stefan Rampp ^{f,g}, Carsten H. Wolters ^{a,b}

- ^a Institute for Biomagnetism and Biosignalanalysis, University of Münster, Münster, Germany
- b Social, Genetic, and Developmental Psychiatry Department, Institute of Psychiatry, Psychology, and Neuroscience, King's College London, London, United Kingdom
- ^c Otto Creutzfeldt Center for Cognitive and Behavioral Neuroscience, University of Münster, Germany
- ^d Centre for Cognitive Neuroimaging (CCNi), University of Glasgow, Glasgow, UK
- e Digital Image and Signal Processing Laboratory, School of Electronic and Computer Engineering, Technical University of Crete, Chania, Greece
- ^f Department of Neurosurgery, University Hospital Erlangen, Erlangen, Germany
- g Department of Neurosurgery, University Hospital Halle (Saale), Germany

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ABSTRACT

Skull conductivity has a substantial influence on EEG and combined EEG and MEG source analysis as well as on optimized transcranial electric stimulation. To overcome the use of standard literature values, we propose a noninvasive two-level calibration procedure to estimate skull conductivity individually in a group study with twenty healthy adults. Our procedure requires only an additional run of combined somatosensory evoked potential and field data, which can be easily integrated in EEG/MEG experiments. The calibration procedure uses the P20/N20 topographies and subject-specific realistic head models from MRI. We investigate the inter-subject variability of skull conductivity and relate it to skull thickness, age and gender of the subjects, to the individual scalp P20/N20 surface distance between the P20 potential peak and the N20 potential trough as well as to the individual source depth of the P20/N20 source. We found a considerable inter-subject variability for (calibrated) skull conductivity $(8.44 \pm 4.84 \text{ mS/m})$ and skull thickness $(5.97 \pm 1.19 \text{ mm})$ with a statistically significant correlation between them (rho=0.52). Age showed a statistically significant negative correlation with skull conductivity (rho=-0.5). Furthermore, P20/N20 surface distance and source depth showed large inter-subject variability of 12.08 \pm 3.21 cm and 15.45 \pm 4.54 mm, respectively, but there was no significant correlation between them. We also found no significant differences among gender subgroups for the investigated measures. It is thus important to take the inter-subject variability of skull conductivity and thickness into account by means of using subject-specific calibrated realistic head modeling.

1. Introduction

State of the art realistic head volume conductor models are a pre-requisite for accurate electroencephalography (EEG) and magnetoencephalography (MEG) source analysis (Akalin Acar, Acar, & Makeig, 2016; Azizollahi, Aarabi, & Wallois, 2016; Brette & Destexhe, 2012; Montes-Restrepo et al., 2014) as well as for optimized transcranial electric (TES) and magnetic (TMS) stimulation (Guler et al., 2016; Huang et al., 2017; Sadleir, Vannorsdall, Schretlen, & Gordon, 2012; Saturnino, Thielscher, Madsen, Knösche, & Weise, 2019; Schmidt, Wagner, Burger, van Rienen, & Wolters, 2015). These head models consist of the most important head tissue compartments incorporating different conductivities, and their accuracies are a crucial factor in the anal-

ysis. At the moment, head models rely on standard conductivities from the literature, while it is known that there is considerable inter-subject variability in their values (Akhtari et al., 2002; Hoekema et al., 2003; McCann, Pisano, & Beltrachini, 2019).

In contrast to the magnetic modalities (MEG, TMS), for EEG source analysis (Akalin Acar et al., 2016; Montes-Restrepo et al., 2014; Vorwerk, Aydin, Wolters, & Butson, 2019) and TES (Sadleir et al., 2012; Schmidt et al., 2015), skull conductivity has been shown to be the most influential of the head tissue conductivity parameters. Several studies investigated the impact of skull conductivity uncertainties on electric potential distributions (Azizollahi et al., 2016; Vallaghé et al., 2009). Small changes on skull conductivity can cause substantial attenuations on the modeled electric fields resulting in localization errors in the cen-

E-mail address: marios.antonakakis@uni-muenster.de (M. Antonakakis).

^{*} Corresponding author. Marios Antonakakis, Ph.D. Student, Institute for Biomagnetism and Biosignalanalysis, University of Muenster, Malmedyweg 15, 48149 Muenster, Germany.

timeter range and orientation changes of more than 25° (Akalin Acar et al., 2016; Aydin et al., 2014). For the somatosensory P20/N20 component, Vorwerk et al. (2019) investigated how uncertainties associated with the experimentally determined conductivity values of the different compartments influence the results of EEG source analysis. Skull conductivity uncertainty was found to have the biggest influence on forward (Vorwerk et al., 2019; Table 2) and inverse source analysis (Vorwerk et al., 2019, Figs. 7 – 9). Uncertainties in the skull conductivity can lead to changes in source localization of up to 2 cm (Vorwerk et al., 2019, Figs. 7A and 9). These changes can also lead to four times higher amplitudes and unrealistic orientations of the modeled current density for TES (Sadleir et al., 2012; Schmidt et al., 2015).

Various measurement approaches such as electrical impedance tomography (EIT) (Abascal et al., 2008; Fernández-Corazza et al., 2018; Gonçalves, Munck, Verbunt, Heethaar, & Lopes da Silva, 2003; Vauhkonen, Kaipio, Somersalo, & Karjalainen, 1997), magnetic resonance EIT (MREIT) (Gao, Zhu, & He, 2006), magneto acoustic tomography (MAT) (Li, Yu, & He, 2016), and directly applied current (DAC) (Akhtari et al., 2002; Hoekema et al., 2003) have already been studied to determine skull conductivity. These approaches require further specialized equipment and/or expertise (EIT, MREIT and MAT) and/or are invasive (DAC). Here, we propose to use the combined modalities EEG and MEG with magnetic resonance imaging (MRI) for the individual estimation of skull conductivity in healthy human subjects with the aim of investigating its inter-subject variability. The used modalities combined EEG/MEG and MRI are available in an MEG-laboratory and the proposed procedure can easily be applied in neuroscientific research on healthy human subjects and/or patients due to its non-invasiveness. Furthermore, MEG is an emerging technology and broader use of it might be pushed by the newest generation of optically pumped magnetometer (OPM) MEG devices (Boto et al., 2018; Labyt et al., 2019).

Estimating skull conductivity with combined EEG/MEG and MRI has already been proposed in studies with three-compartment head models (Baysal & Haueisen, 2004; Fuchs et al., 1998; Gonçalves et al., 2003; Huang et al., 2007) and in first case studies with more realistic head models (Aydin et al., 2014; Wolters, Lew, MacLeod, & Hämäläinen, 2010). In these studies, a so-called 'bulk' skull conductivity parameter (Akhtari et al., 2002; Papageorgakis, 2017) was estimated in a calibration procedure that included source analysis of somatosensory evoked potential (SEP) and field (SEF) data at 20 ms post-stimulus, the P20/N20 component. It was shown that this component has a focal and dipolar origin with mainly tangential orientation with respect to the inner skull surface (Allison, McCarthy, Wood, & Jones, 1991; Hari et al., 1993; Nakamura et al., 1998). Although other studies proposed to estimate skull conductivity based on only SEP data (Lew, Wolters, Anwander, Makeig, & MacLeod, 2009; Vallaghé & Clerc, 2009), additional SEF data stabilize the estimation (Wolters et al., 2010). This is due to the complementarity of EEG and MEG data (Dassios, Fokas, & Hadjiloizi, 2007; Huang et al., 2007) and the insensitivity of MEG localizations to skull conductivity (Fig. 8 in Brette & Destexhe, 2012; Haueisen, Ramon, Eiselt, Brauer, & Nowak, 1997; Lew, Sliva, & Choe, 2013).

Gonçalves et al. (2003) found a strong agreement between the results of an EIT procedure and the SEP/SEF method, even though they are quite different in both theoretical and technical terms, which indicates the stability of the SEP/SEF based calibration. EIT uses Ohm's law between the measured voltages and the currents injected via scalp electrodes (Fernández-Corazza et al., 2018). Both methods function under in vivo conditions and in low frequency ranges (McCann et al., 2019).

A common feature of the aforementioned methods is that they are based on an accurate and realistic head model with individual compartments (McCann et al., 2019; Vorwerk et al., 2014). In this regard, most of the above SEP/SEF calibration studies were based on the modeling of homogenized compartments such as single-layer skull or brain. More realistic subject-specific head volume conductor modeling based on MRI is increasingly becoming a standard procedure due to the now available automatized and open source segmentation ap-

proaches (Antonakakis et al., 2019; Huang, Datta, Bikson, & Parra, 2019; Nielsen et al., 2018). In this work, we investigate the inter-subject variability of *skull conductivity* in a group of twenty subjects using an SEP/SEF calibration procedure for the first time. This procedure is based on six-compartment anisotropic (6CA: skin, skull compacta, skull spongiosa, cerebrospinal fluid (CSF), gray matter and anisotropic white matter) head modeling.

As shown in (Tang et al., 2008) using excised skull samples from patients undergoing surgery, skull conductivity is strongly and positively correlated to skull thickness. It is therefore important that the head model also represents skull thickness accordingly. While accurate skull thickness can best be determined using CT (Lillie, Urban, Lynch, Weaver, & Stitzel, 2016), the non-invasive procedure proposed here is based on MRI. Using T1-weighted (T1w) MRI, Gorbenko, Mikołajczyk, Jasionowska, Narloch, and Kałużyński (2020) accurately segmented soft tissues, but with only 67% specificity and 83% sensitivity, the results concerning the skull were rather limited. This is because the low contrast between CSF and cranial tissue makes it difficult to estimate the inner skull boundary from T1w MRI alone. Therefore, in the present study, we use T1w and T2w scans for an improved MRI-based estimation of skull thickness, which is our second measure used throughout this study.

The use of T1w and T2w scans additionally allows the segmentation of skull compacta and spongiosa to model the skull's three-layeredness (spongiosa located between inner and outer compacta) (Akhtari et al., 2002; Montes-Restrepo et al., 2014). Thus, our procedure distinguishes skull compacta and spongiosa tissues and uses a fixed conductivity ratio for the compacta:spongiosa conductivity values as suggested by (Dannhauer, Lanfer, Wolters, & Knösche, 2011) based on the measurements of (Akhtari et al., 2002). The use of a fixed conductivity ratio reduces the degrees of freedom and helps to avoid overfitting in our skull conductivity calibration procedure (Lew et al., 2009; Wolters et al., 2010). We therefore refine the definition of the term 'bulk skull conductivity' introduced above so that from now on it is the calibrated value for skull compacta in combination with the fixed conductivity ratio to the spongiosa.

It has also been assumed that skull conductivity may vary due to demographic factors such as age (Hoekema et al., 2003; Horesh, 2006; McCann et al., 2019; Wendel, Väisänen, Seemann, Hyttinen, & Malmivuo, 2010), especially over infancy (Azizollahi, Darbas, M. Diallo, El Badia, & Lohrengel, 2018). Using direct measurements of the (homogeneous) skull conductivity of skull pieces, temporarily removed during epilepsy surgery, Hoekema et al. (2003) observed a weak negative correlation over an adult age group of five patients. Such a negative correlation was furthermore supported by (Arumugam et al., 2017) based on EIT measurements in ten participants. On the other hand, in CT studies, it was reported that skull thickness in adults varies substantially among individuals and is independent of age (De Boer, van der Merwe, & Soerdjbalie-Maikoe, 2016; Lillie et al., 2016) but dependent on subject's gender (Pellegrini, Zoghi, & Jaberzadeh, 2018). However, it is not yet clear whether gender can also influence skull conductivity and its inter-individual variation in an adult age group. In this study, our non-invasive approach is used to investigate and evaluate these aspects.

The influence of inter- and intra-individual skull conductivity variations has already been highlighted in earlier studies (Aydin et al., 2014; Dabek et al., 2016; Dannhauer et al., 2011; Fernández-Corazza et al., 2018; Haueisen et al., 1997; Montes-Restrepo et al., 2014; Oostendorp, Delbeke, & Stegeman, 2000). It is clear from these studies that, for a fixed dipolar source in the brain, differences in skull conductivity result in differences in the surface distance between the two poles, the potential peak and trough, of the corresponding EEG forward solution potential topography. The latter means that lower skull conductivity leads to a higher pole distance (Nunez & Srinivasan, 2006; Pernier, Perrin, & Bertrand, 1988). However, in practical P20/N20 measurements, the measure of the scalp surface distance between the peak and trough well depends on the EEG recording quality, the number of

available electrodes and the accuracy in the assumption that the underlying source is a single focal dipolar source. Therefore, we propose here to use the *P20/N20 surface distance* as our third measure investigated in this study. This measure is the distance between the surface potential poles of the simulated EEG forward solution of the best fitting single dipolar source, reconstructed in a calibrated 6CA head model from the combined SEP and SEF measurement data 20 ms post-stimulus (P20/N20 peak). We will show that this forward simulated potential topography leads to an accurate and stable measure of the P20/N20 surface distance, and that this distance is an important additional measure in the evaluation of inter-subject variability of skull conductivity, being in the focus of this study.

Finally, our fourth investigated measure refers to the *source depth*. As in the EEG source analysis studies by (Haueisen et al., 1997; Vorwerk et al., 2019), the source depth is defined here as the distance between source location and the nearest point on the inner skull surface; the larger this distance, the deeper the source is considered to be. Since they are closely related to each other (Vorwerk et al., 2019), we will evaluate this additional measure to gain further insights into the inter-subject variability of skull conductivity.

In summary, we investigate non-invasively the inter-subject variability of the calibrated bulk skull conductivity using 6CA head models, i.e., distinguishing also between spongiosa and compacta compartments, in a group-study of twenty adult subjects. First, we define the four proposed measures individually, i.e., skull conductivity and thickness, P20/N20 surface distance, as well as source depth. In a second step, we compare these measures with the participants' age and gender to statistically evaluate the most relevant factors of variability between the subjects. To the best of our knowledge, this is the first study that uses combined EEG/MEG source analysis with subject-specific realistic head volume conductor models, with the aim to investigate the inter-subject variability of skull conductivity in a large number of participants.

2. Material and Methods

2.1. Participants and Data Acquisition

2.1.1. Participants and Ethics Statement

Twenty right-handed adult subjects, ten males and ten females, in the age range of 18 to 53 years (mean and standard deviation 34.1 ± 10.88) participated in this study. All subjects gave their written informed consent forms and all measurements have been approved by the ethics committee of the University of Erlangen, Faculty of Medicine on 20.02.2018 (Ref No 4453 B).

2.1.2. Experiment and EEG/MEG/MRI Acquisition

Somatosensory evoked responses (SEP and SEF) were simultaneously acquired in a magnetically shielded room. 80 AgCl sintered EEG ring electrodes (EASYCAP GmbH, Herrsching, Germany, 74 channel EEG plus additional 6 channels EOG to detect eye movements), one additional Electrocardiography (ECG) electrode, and a whole head MEG with 275 axial gradiometers and 29 reference coils (OMEGA2005, VSM MedTech Ltd., Canada). The MEG reference coils were used to calculate third order synthetic gradiometers for the reduction of interference caused by magnetic fields originating from distant locations. Before the measurements, the electrode positions of the EEG cap were digitized using a Polhemus device (FASTRAK, Polhemus Incorporated, Colchester, Vermont, U.S.A.). Moreover, during the acquisition, the head position inside the MEG was tracked via three head localization coils placed on nasion and left/right preauricular points.

SEP and SEF activity was elicited by stimulating the median nerve at the wrist of the right arm with monophasic square-wave electrical pulses of 0.5 ms width. The stimulus strength was increased until a clear movement of the right thumb was visible. The stimulus duration was 200 ms and a random stimulus onset asynchrony between 350 and 450 ms was applied to avoid habituation and to obtain a clear pre-stimulus interval.

The duration of the experiment was 10 minutes for a measurement of 1200 trials and data was acquired with a sampling rate of 1200 Hz and online low pass filtered at 300 Hz.

A 3T scanner (MAGNETOM Prisma 3.0 T, Release D13, Siemens Medical Solutions, Erlangen, Germany) was used for MRI acquisition. A 3D-T1-weighted (T1w) fast gradient-echo pulse sequence using water selective excitation to avoid fat shift (TR/TE/TI/FA = 2300/3.51/ 1100 ms/8°, cubic voxels of 1 mm edge length) and a 3D-T2w turbo spin echo pulse sequence (TR/TE/FA = 3200/408 ms/90°, cubic voxels, 1 mm edge length) were measured. Diffusion tensor MRI (DTI) was acquired using an echo planar imaging sequence (TR/TE/FA = 9500/79 ms/90°, cubic voxels, 1.89 mm edge length). DTI included one scan with diffusion sensitivity $b = 0 \, \text{s/mm}^2$ (b_0 , flat diffusion gradient), an additional scan with flat diffusion gradient with reversed spatial encoding gradients for susceptibility artifact correction (Ruthotto et al., 2012) and twenty scans with b=1000s/mm² in different directions, equally distributed on a sphere. During MRI scanning, we placed gadolinium markers at the same positions as in combined EEG/MEG, i.e., nasion, left and right distal outer ear canal, for landmark-based registration of combined EEG/MEG to MRI. We perform all measurements in supine position to reduce head movements and to prevent CSF effects due to a brain shift when combining EEG/MEG and MRI (Rice, Rorden, Little, & Parra,

2.2. Head Model Preparation

We created a realistic and individual six-compartment head volume conductor model for each subject. The head modeling procedure combines T1w and T2w MRIs for improved modeling of the skin, skull compacta (SC), skull spongiosa (SS), CSF, gray matter (GM) and anisotropic white matter (WM). The use of T2w MRI was important for the segmentation of the cancellous bone because there is no water-fat-shift that could otherwise cause mispositioning of the skull compacta. All algorithmic steps were developed in MATLAB (The MathWorks, Inc., Natick, Massachusetts, U.S.A.) using our own custom code and open-source toolboxes for integration into a quasi-automated pipeline.

The procedure starts with the rigid registration of the T1w and T2w MRIs using the FSL¹ software that is used through subroutines in the FieldTrip toolbox (Oostenveld, Fries, Maris, & Schoffelen, 2011). The flirt routine of FSL is used with mutual information as a cost function for the registration procedure and spline interpolation for the reslicing (i.e., transformation of MRI slices) of the registered T2w MRI to the reference T1w MRI. Then, the segmentation of the skin, GM and WM compartments is performed using the T1w MRI, while the T2w MRI is used to segment SC, SS, and CSF. All segmentations are performed with SPM12² which is embedded in the FieldTrip toolbox. The spongiosa is calculated using a 2 mm eroded full skull compartment image to define a region-of-interest (ROI) and then gray-value thresholding is used within this ROI in the T2w MRI. After visual inspection in some cases, 1 mm dilation is performed in the eroded full skull image, if the resulting SS mask is not matching the corresponding cancellous bone represented in the registered T2w MRI. In addition, the brain mask, including CSF, GM and WM, is segmented from the combined T1w and T2w MRIs. These masks are important for the subsequent merging of the segmented tissues to construct the six-compartment model. During this merging procedure, further enhancements based on MATLAB image processing routines such as regionprops and imfill are applied to the segmented tissues to avoid overlap and reduce segmentation inaccuracies. In this procedure, regionprops is used to remove unrealistic areas created during the merging of the segmented tissues. We also apply imfill for the correction of artificial tiny holes still present in the initially segmented compartments skull and skin. Following the recommendation of (Lanfer

http://www.fmrib.ox.ac.uk/fsl

² https://www.fil.ion.ucl.ac.uk/spm/software/spm12/

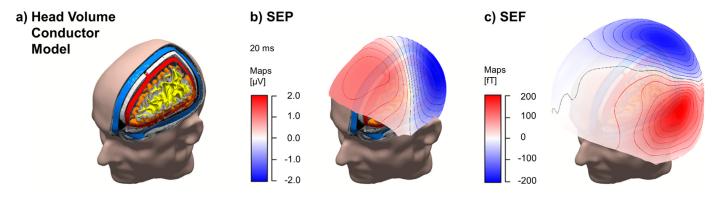


Figure 1. The main ingredients for the skull conductivity calibration procedure. a) The individual high-resolution head model with six-compartments (skin (human light skin color); skull compacta (blue) and spongiosa (gray); CSF (red); gray matter (orange) and white matter (yellow)). b and c) The iso-potential and field lines of the bipolar scalp topographies for the somatosensory evoked potential and fields (SEP and SEF) at 20 ms post stimulus (the P20/N20 component) for one of the subjects.

et al., 2012), a cut 40 mm below the lower skull compartment is applied in order to avoid unnecessary FEM calculations (see Section 2.4.1).

DTI data was preprocessed to reduce eddy current artifacts and nonlinear susceptibility artifacts following (Aydin et al., 2014), using FSL and the subroutine *HySCO* from the SPM12 toolbox (Ruthotto et al., 2012). Diffusion tensors were calculated and transformed into WM conductivity tensors by an effective medium approach (Aydin et al., 2014; Tuch, Wedeen, Dale, George, & Belliveau, 2001). These tensors were then included in the head model to account for WM tissue conductivity anisotropy.

For the labeled volumes, geometry-adapted hexahedral finite element (FE) head models were constructed using SimBio-VGRID³ (Wolters, Anwander, Berti, & Hartmann, 2007). The adaptation was performed with a node-shift of 0.33, ensuring that interior angles at element vertices were convex and the Jacobian determinant in the FE computations remained positive. This approach increases the conformance to the real geometry and mitigates the effects of the staircase-like segmented voxel meshes. As a result, subject-specific six-compartment anisotropic head models were built.

In the next step, a 2 mm resolution source space was constructed in the middle of the GM compartment without restriction to source orientations (no normal-constraint). This positioning of the source space ensured that all sources were located inside GM and sufficiently far away from the neighboring tissue compartments to fulfill the so-called Venant condition, i.e., for each source node, the closest FE node should only belong to elements labeled as GM. The fulfillment of this condition is important to avoid numerical problems and unrealistic source modeling for the chosen Venant dipole modeling approach (Vorwerk et al., 2014). Fig. 1a depicts one of the realistic head volume conductor models of this study exemplarily.

2.3. Preprocessing of EEG/MEG

The raw combined EEG and MEG recordings were first filtered from 20 to 250 Hz (Buchner et al., 1994) using digital bandpass filtering in CURRY8⁴. A notch filter was used to reduce the effect of power line noise at 50 Hz and its harmonics. Then, the preprocessed recordings were separated into epochs with 100 ms pre-stimulus and 200 ms post-stimulus. After deselecting the bad channels visually, artifact reduction was performed in CURRY8 using a threshold-based determination of candidate bad trials in each modality, followed by visual inspection and exclusion of bad trials from the rest of the analysis. The SEP/SEF evoked responses were then determined by averaging across all the remaining

trials. Fig. 1b and c depict exemplarily the artifact-corrected SEP and SEF scalp topographies of the P20/N20 component for one of the subjects.

2.4. Definition of Measures

In this section, we define the four measures that will be investigated with regard to their inter-subject variability, age and gender dependence, as follows: (i) skull conductivity (as well as the related measures of the calibration process) (ii) skull thickness (iii) P20/N20 surface distance and (iv) source depth.

2.3.1. Measures for Skull Conductivity Calibration

Skull conductivity is individually modeled by adapting a calibration procedure that benefits from the different sensitivity profiles of EEG and MEG (algorithm 2 in Aydin et al., 2014). While the procedure in (Aydin et al., 2014) only uses a single resolution level, we refine it here by proposing two resolution levels, resulting into the following three steps procedure.

Step 1 (source localization): While individual skull conductivity has a considerable influence on the P20/N20 SEP source reconstruction, it hardly influences source analysis of the SEF component at 20 ms poststimulus (Brette & Destexhe, 2012; Lew et al., 2013). Therefore, using a dipole scan approach (Fuchs et al., 1998; Knösche, 1997) throughout the whole source space and a head model with the standard skull conductivity parameters 1.6 mS/m for SC and 5.76 mS/m for SS (Akhtari et al., 2002), we exploit the SEF data to accurately localize the peak at 20 ms post-stimulus. The single dipole scan assumes that its generator is focal and single-dipolar (Allison et al., 1991; Buchner et al., 1994; Hari et al., 1993; Nakamura et al., 1998). The main goal of the dipole scan is the determination of the source for which the residual variance (RV) between the measured and the simulated SEF data at 20 ms post-stimulus is minimal. Furthermore, the dipole scan is regularized accordingly to suppress the amplification of high-frequency spatial noise into erroneously high radial dipole orientation components within the inversion procedure (Fuchs et al., 1998; Wolters, Beckmann, Rienäcker, & Buchner, 1999). This source location is then fixed as the outcome of step 1 and will no longer be modified by the next two steps of our calibration procedure.

Step 2 (coarse resolution calibration): Our coarse resolution level uses the predefined set of skull compacta conductivity values SC = [0.8, 1.6, 2.4, 2.8, 3.3, 4.1, 5.5, 7, 8.3, 16.5, 33] mS/m. These values were selected based on (Aydin et al., 2014) including the additional value of 0.8 mS/m (Altakroury, 2017; McCann et al., 2019). The ratio of SC:SS is fixed to 1:3.6 (Akhtari et al., 2002; Dannhauer et al., 2011). Therefore, our skull conductivity calibration includes only one degree of freedom, namely the SC conductivity, to avoid overfitting due to a too high number of degrees of freedom (Lew et al., 2009; Wolters et al., 2010). The

³ http://vgrid.simbio.de/

⁴ https://compumedicsneuroscan.com/products/by-name/curry/

following steps compensate for the insensitivity of MEG to quasi-radial source components: For the fixed source location of step 1 and an SC value out of the above predefined coarse resolution set, we then determine the dipole orientation and strength that achieves lowest RV to the measured SEP and SEF components at 20 ms post-stimulus and store the RV to the SEP data as output value. This results in one point of the calibration curve of the corresponding subject in Figure 4. These steps are repeated for all values of the coarse resolution level, resulting in a coarse resolution calibration curve, for which minimum is then finally selected as the coarse level calibration optimum.

Step 3 (fine resolution calibration): A finer resolution level for SC calibration conductivity is now produced around the coarse level calibration optimum of step 2 and the new RV minimum is determined as in step 2. The outcome is a calibration curve with refinement around the minimum, the skull conductivity calibration value, as shown in Figure 4. Thereby, our two-level procedure helps to reach an even lower residual variance to the simultaneously measured SEF and SEP P20/N20 peaks.

For the compartments skin (430 mS/m, Ramon, Schimpf, & Haueisen, 2004), CSF (1790 mS/m, Baumann, Wozny, Kelly, & Meno, 1997) and GM (330 mS/m, Ramon et al., 2004), we select standard (non subject-specific) conductivity values from the literature, while for the WM compartment, we perform the DTI modeling procedure from Section 2.2 to determine subject-specific anisotropic conductivity tensor maps.

For the above two-level skull conductivity calibration, EEG and MEG forward methods are employed, as described in the following: All EEG and MEG forward solutions in this study are calculated using the finite element method (FEM), as implemented in the SimBio⁵ software. We use the Venant direct FEM approach (Buchner et al., 1997; Wolters et al., 2007) due to its high numerical accuracy (Bauer, Pursiainen, Vorwerk, Kostler, & Wolters, 2015) and high computational efficiency when used in combination with EEG and MEG transfer matrices and an algebraic multigrid preconditioned conjugate gradient (AMG-CG) solver (Wolters, Grasedyck, & Hackbusch, 2004). Standard piecewise trilinear basis functions are furthermore used in an isoparametric FEM framework.

In order to adapt to the different units of the EEG and MEG measurements, a signal to noise ratio (SNR) based transformation is applied, whitening the data by means of each channel's individual noise level, and resulting in unitless measures for both EEG and MEG (Fuchs et al., 1998).

Besides (i) the calibrated skull conductivity, we also investigate further measures that are taken into account when accessing the overall quality of the source reconstruction in the calibration procedure (Fuchs et al., 1998). These further measures are the following: (ii) The individual P20/N20 latency. (iii) The individual SNR_{SEP} and SNR_{SEF}, quantifying the quality of our SEP and SEF data, respectively, at the specific P20/N20 signal peak. In this study, the SNR is estimated based on (Fuchs et al., 1998) and it is considered as the maximum value across all sensors, separately for SEP and SEF data. (iv) The Residual Variance of the SEP data (RV_{SEP}) indicating the remaining distance of the forward simulated to the measured P20/N20 component. (v) The source strength of the dipole scan result of the calibration procedure.

2.3.2. P20/N20 Surface Distance

The scalp surface distance is defined between the potential peak (point P in Fig. 2a) and the potential trough (point N in Fig. 2a), based on the following methodological steps. (1) We estimate the subject-specific Cartesian coordinates of P and N as follows. With the result from the calibration in Section 2.4.1 (Fig. 2a, green dipole), we produce a forward simulated dipolar scalp topography. The following aspects characterize

this topography: (a) it maximally resembles the measured SEP/SEF topography at 20 ms post-stimulus, (b) it reduces the influence of data noise on the peak-to-peak detection procedure and (c) it allows to identify accurately the positive and negative potential peaks P and N, especially since they are most often between electrodes. Thus, this procedure can be seen as a subject-specific inter- and extrapolation method for the scalp potentials. An example of the dipole scalp topography is presented in Fig. 2a for one of the subjects. (2) We connect P and N through a line with a length corresponding to the Euclidean distance between P and N and discretize this line into equidistant line points, where the distance is chosen according to the discretization size of the scalp surface triangles. (3) We then use the MATLAB function point2trimesh⁶ to determine for each line point the corresponding closest point on the triangulated scalp surface mesh (Fig. 2a, a subset of these points is shown by black dots). Thereby, a distinct curved line results which consists of linear elements over the surface. (4) We then approximate the final surface distance between P and N, by summing up the Euclidean length of all linear elements of this curved surface line.

2.3.3. Skull Thickness

The ROI, in which skull thickness is determined, includes an important area of the left hemisphere (due to right-hand stimulation) under the main SEP topography. It does not necessarily include the potential peak P and the potential trough N. For example, including P would mean to include mid-sagittal areas, where the pronounced dura compartment might influence skull segmentation accuracy. Fig. 2b shows an exemplary skull ROI (in dark yellow) for one subject used in this study.

The investigated skull thickness in this ROI is measured for four different compartments: (i) full skull (ii) outer skull compacta (iii) skull spongiosa and (iv) inner skull compacta. For this purpose, the segmented masks of the full skull (including both compacta compartments and the spongiosa) and of the skull spongiosa (Section 2.2) are utilized. For each one of these masks, a surface-based geometry (or surface), i.e., a set of triangles and nodes, is constructed through the MATLAB function isosurface. Then, the thicknesses are estimated following a recent approach of (Lillie et al., 2016). In short, the thickness is measured using the compartments outer surface and its inner surface for each one of the four skull compartments. To determine the outer and inner surface of the given skull compartment, the normal vectors (Fig. 2b, green box, arrows in black), and the center of gravity (CG) of the skull ROI is used (Fig. 2b, red point). The determination of the normal vectors is established at each node of the skull compartment surfaces. If the scalar product of CG and a surface node normal is positive, the corresponding node is labeled as outer skull surface point, otherwise inner. By applying this procedure independently both to the full skull and the skull spongiosa surfaces, we extract the surfaces F_{OUT} and S_{OUT} (Fig. 2b, blue box, surfaces in green) and $F_{\rm IN}$ and $S_{\rm IN}$ (Fig. 2b, blue box, surfaces in red) where 'F' and 'S' denote full skull and spongiosa, respectively. We then measure the four different skull compartment thicknesses. Each thickness value is the average value across the minimum Euclidean distance between each node of the corresponding outer surface (FOUT for full skull and outer skull compacta; S_{OUT} for skull spongiosa; S_{IN} for inner skull compacta) to all nodes of the corresponding inner surface (F_{IN} for full skull and inner skull compacta; S_{OUT} for outer skull compacta; S_{IN} for skull spongiosa).

2.3.4. Source Depth

For each participant, we define the source depth as the minimum Euclidean distance between the P20/N20 reconstructed dipole source location, resulting from the procedure in Section 2.4.1 and the inner surface of the skull. In Fig. 2c, we present a sketch for the determined

⁵ SimBio: https://www.mrt.uni-jena.de/simbio/index.php/Main_Page and its integration into Fieldtrip (see Vorwerk et al., 2018) http://fieldtrip.fcdonders.nl/development/simbio

⁶ https://de.mathworks.com/matlabcentral/fileexchange/52882-point2trimesh-distance-between-point-and-triangulated-surface?s_tid=prof_contriblnk

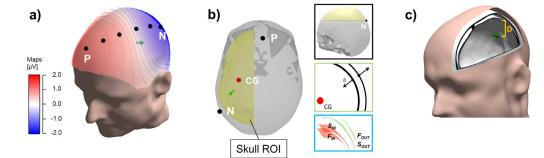


Fig. 2. Visualization of the measures of Section 2.4 for one subject. a) Dipole scan result (in green) for the measured P20/N20 component. The black points represent a subset of the surface points for the determination of the distance between the interpolated most positive (P) and most negative (N) potentials of the forward simulated topography. b) Skull ROI (in dark yellow) under the P20/N20 topography (P and N points) and dipole scan result (in green). The ROI includes an important area of the left hemisphere (due to right-hand stimulation) under the main SEP topography. It does not contain the potential peak P in order to avoid inclusion of mid-sagittal skull areas where the segmentation quality might be influenced by the pronounced dura compartment. Color boxes show the main steps for the calculation of skull thickness. The black box shows the skull ROI (sagittal view). The green box shows the normal vectors (\hat{n} in black) for the determination of outer and inner skull surfaces. The red point represents the center of gravity (CG) of the ROI. The blue box shows the two outer surfaces F_{OUT} (outer surface of full skull) and S_{OUT} (outer surface of skull spongiosa) (in green) and the two inner surfaces F_{IN} (inner surface of full skull) and S_{IN} (inner surface of skull spongiosa) (in red). c) Determination of the source depth: Minimum distance (D) between the reconstructed P20/N20 dipole scan result (in green) and the inner skull surface. Visualizations were performed with custom MATLAB code and CURRY 8.

source depth, given a reconstructed P20/N20 source (green dipole) for one of the participants.

2.4. Statistical Analysis

The statistical analysis includes a correlation procedure for testing whether (a) the measures on the head tissues defined in Section 2.4 are age-related, (b) skull thickness is related to the calibrated skull conductivity and (c) the P20/N20 surface distance is related to the source depth. We use the Robust Correlation Toolbox⁷, allowing automatic detection of outliers and determination of statistical significance through percentile bootstrap confidence intervals (CIs). We select the skipped Pearson correlation (rho) as a non-parametric method that takes into account the heteroscedasticity effects compared to the standard Pearson correlation (Pernet, Wilcox, & Rousselet, 2013). The rejection of the null hypothesis is based on the bootstrapped CIs at the 95 % percentile level (95 % CI). We further derive the corresponding p-value (P) of each 95 % CI and apply false discovery rate control (FDR) due to the multiple correlation estimations. The applied FDR method follows (Benjamin & Hochberg, 1995) and the adjustment level is set to 0.05. The data resampling within the bootstrap procedure is performed 1000 times while the outlier detection is based on the rule of the interquartile range from the same toolbox.

In a subsequent analysis of variance (ANOVA)⁸, the effect of the gender is taken into account by adding it as a between-subject factor in a linear regression analysis⁹ with each of the above-mentioned pairs. In a last step, we conduct pairwise gender comparisons, including two-tailed tests separately for each measure of Section 2.4 and P20/N20 source analysis parameters. The examined null hypothesis H₀ is that females and males have the same mean value. For each test, we first apply a data normality test based on a Kolmogorov-Smirnov test (Massey et al., 1951). A parametric (paired sample t-test), or non-parametric (Mann-Whitney u-test, Mann & Whitney, 1947) pairwise test is then applied depending on the result of the normality test. A threshold is defined at 95 % level of confidence for both ANOVA and pairwise tests for the significance level of the p-value. FDR adjustment is also applied to the p-values for the multiple comparison correction.

3. Results

The result section is divided into two parts: The first part presents the results for the four defined measures of Section 2.4 in male and female participants: (i) calibrated skull conductivity (ii) skull thickness (iii) P20/N20 surface distance and (iv) source depth. To improve readability, unless otherwise stated, the term skull thickness will be the full skull thickness (including outer compacta, spongiosa and inner compacta). In the second part, we outline results from the correlation analysis, as defined in Section 2.5.

3.1. Inter-Subject Variability in the Defined Measures

3.1.1. Variability in the Measures for Skull Conductivity Calibration

In Figure 3, the P20/N20 reconstructed dipole source (in red) is presented on the individual MRI for one of the subjects. This source reconstruction is the result of the combined EEG and MEG source analysis within the skull conductivity calibration procedure (Section 2.4.1). The calibrated conductivity is 12.5 mS/m for skull compacta and, due to the fixed conductivity ratio of 1:3.6, 45 mS/m for the spongiosa. The dipole source is located on the postcentral wall of the central sulcus in Brodmann area 3b in primary somatosensory cortex (SI) and has a mainly tangential orientation with regard to the inner skull surface.

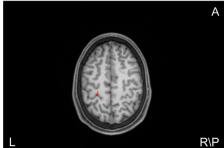
For each participant, the skull conductivity calibration procedure (Section 2.4.1) was applied in the corresponding subject-specific realistic 6CA head model, resulting in a 6CA calibrated (6CA_cal) head model. The Residual Variance (RV) of the simulated to the measured data, collected for each conductivity within the calibration procedure, resulted in subject-specific calibration curves that are depicted in Fig. 4. Finally, determining the minimum in the RV curve allowed us to set up the individual 6CA_cal head model for each subject.

As Figure 4 and Table 1 show, the resulting residual variance for the SEP skull conductivity calibration (minimum of each curve) has a mean of 8.57 % with a standard deviation of 3.44 %, is below 20 % for all of the subjects and the best fit goes down to only 4 %. Furthermore, large inter-subject variability of the skull conductivity can be observed across all subjects with the lowest skull compacta (spongiosa) conductivity being at 2.6 mS/m (9.36 mS/m) and the highest at 16.9 mS/m (60.84 mS/m), respectively. In Figure 4, the age-related color coding of the curves shows that the calibration skull conductivity values of the younger participants are overall at higher skull conductivities than those of the older participants. Only a more detailed inspection ex-

⁷ https://sourceforge.net/projects/robustcorrtool/

⁸ https://de.mathworks.com/help/stats/regression-and-anova.html

 $^{^{9}\ \}text{https://www.mathworks.com/help/matlab/data_analysis/linear-regression.html}$





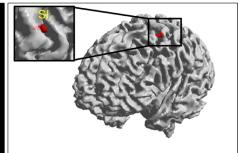


Figure 3. Source reconstruction of the P20/N20 component using combined SEP and SEF. The reconstructed dipole source (in red) is the final result of the skull conductivity calibration procedure of Section 2.4.1 applied in one of the subjects of the study. The reconstruction result is presented on axial (left) and sagittal (middle) slices of the subject's T1w MRI and on a 1 mm resolution volume-rendering of the cortical surface (right). The dipole is localized in Brodmann area 3b on the postcentral wall of the central sulcus in the primary somatosensory cortex (SI). Further abbreviations correspond to Superior (S), Inferior (I), Anterior (A), Posterior (P), Left (L) and Right (R).

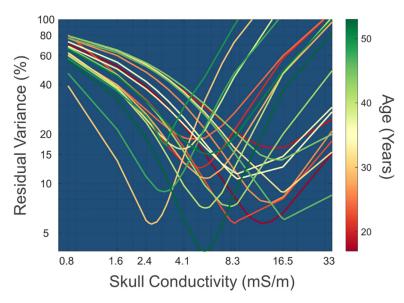


Figure 4. Skull conductivity calibration curves for the twenty subjects. Skull compacta conductivity (horizontal axis, in mS/m) and Residual Variance (in %) to the P20/N20 SEP data on the vertical axis, for the dipole scan result as determined by the skull conductivity calibration procedure (Section 2.4.1). Each subject is represented by one of the curves, color-coded by age. Y-axis is logarithmically-scaled for better readability.

Table 1

Gender-based mean and standard deviation across all the participants of the P20/N20 source analysis with regard to latency (second column), signal-to-noise ratio (SNR) for SEP and SEF (third and fourth columns, resp.), source strength Q (fifth column) and residual variance to the SEP data RV_{SEP} (sixth column) resulting from the calibration procedure as described in Section 2.4.1. The symbol asterisk '*' indicates a significant statistical difference (p-value < 0.05) between genders.

Gender	Latency (ms)	$\mathrm{SNR}_{\mathrm{SEP}}$	SNR_{SEF}	Q (nAm)	RV _{SEP} (%)
Male	23.92 ± 1.30*	14.94 ± 3.86	22.20 ± 7.52	19.98 ± 10.93	8.57 ± 3.44
Female	22.67 ± 0.84*	14.81 ± 4.72	23.25 ± 7.42	21.02 ± 7.34	12.43 ± 4.76
Total	23.29 ± 1.24	14.88 ± 4.20	22.72 ± 7.29	20.50 ± 9.08	10.50 ± 4.51

^{*}indicates statistically significant difference at the level of alpha 95 %

presses a rather complex relationship between cranial conductivity and age, especially due to two older subjects of age 40 and 43 for whom the calibrated skull conductivities are at 16.1 and 16.9 mS/m, respectively, i.e., as high as for most of the young participants.

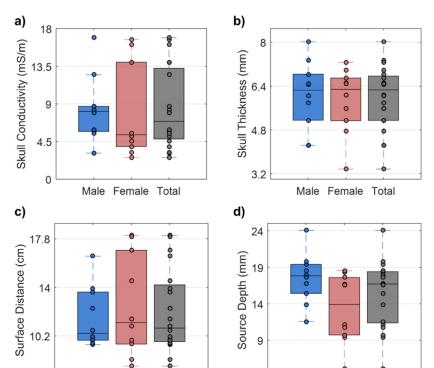
In the following, we present the P20/N20 source analysis parameters monitored during the skull conductivity calibration procedure as additional measures introduced in Section 2.4.1. The resulting average value across all subjects is shown in Table 1. Between genders (Table 1, first row: males, second row: females), the P20/N20 latency is significantly shorter (P < 0.05) for females (22.67 \pm 0.84 ms) than males (23.92 \pm 1.3 ms). Otherwise, we do not observe any significant gender differences for the remaining P20/N20 source analysis parameters.

3.1.2. Variability in Measures and Gender Differences

In the present section, we investigate the inter-subject variability of the four measures defined in Section 2.4 and examine if gender differences can be found in those measures. The variability and the median of the measures is provided in Fig. 5 across all subjects (gray boxplot) and split into subgroups of males (blue) and females (pink).

The most important result is the wide inter-subject variability with large ranges (from minimum to maximum) for all four measures for the total group as well as for the male and female subgroups.

The calibrated skull compacta conductivity ranges from 3.1 up to 16.9 mS/m for males and from 2.6 up to 16.7 mS/m for females (Fig. 5a). The mean and standard deviation across all subjects is 8.44 \pm 4.84 mS/m.



4

Male

Female

Figure 5. Descriptive statistics and inter-subject variabilities. Boxplots depict the inter-subject variability for a) skull compacta conductivity (in mS/m), b) the averaged full skull thickness in the ROI as indicated in Fig. 2b (in mm) c) the P20/N20 surface distance (distance of P to N; in cm) and d) source depth (in mm). Color-coding is used to distinguish male (blue; 10 subjects), female (pink; 10 subjects) and total (gray; 20 subjects) groups. The filled circles represent individual results per subject. Note that there are overlapping values within some of the boxplots. Per boxplot, the central horizontal black line is the median and the edges of the box are the 25th and 75th percentiles.

Table 2Gender-wise mean and standard deviation of the thicknesses for outer and inner compacta and spongiosa skull compartments in the ROI as indicated in Fig. 2b.

Total

Male Female

Skull Compartment	Gender	Average Thickness in the ROI (mm)
Outer-	Male	1.12 ± 0.52
Compacta	Female	0.93 ± 0.62
	Total	1.02 ± 0.57
Spongiosa	Male	3.41 ± 0.93
	Female	3.96 ± 0.96
	Total	3.69 ± 0.96
Inner-	Male	1.10 ± 0.80
Compacta	Female	1.06 ± 0.46
	Total	1.08 ± 0.64

Fig. 5b shows that full skull thickness in the ROI ranges from 4.22 up to $8.02\,\mathrm{mm}$ for males and 3.36 up to $7.27\,\mathrm{mm}$ for females. Mean and standard deviation across all subjects are at $5.97\pm1.19\,\mathrm{mm}$. In Table 2, we additionally present group-wise (male, female, total) mean and standard deviation of the thicknesses for the three different cranial compartments. For outer- and inner-compacta, we find the male subgroup having a higher mean thickness value than the female one, while it is the other way around for the spongiosa.

The P20/N20 surface distance was found to be in a range of 9.5 to 16.4 cm for males and 7.8 to 18.1 cm for females (Fig. 5c). Mean and standard deviation across all subjects are 12.08 ± 3.21 cm.

In Fig. 5d, we present the inter-subject variability in source depth, where values range from 11.57 up to 24.05 mm for males and from 5.1 up to 18.56 mm for females. Additionally to the results presented in Fig. 5d, we determined for source depth a mean and standard deviation of 15.45 \pm 4.54 mm across all participants.

Finally, no statistically significant gender difference was observed when applying pairwise statistical analysis on the mean value of each of these measures.

Table 3

Total

Interaction of age with the measures from Section 2.4, i.e., cranial compartment thickness in the ROI, surface distance and source depth with age. The first and second columns indicate the number and the name of the correlation pair, respectively. The third column shows the correlation value (rho) and the fourth column presents the bootstrapped confidence interval (CI). The fifth column shows the p-value (P) as derived from each bootstrapped CI and adjusted with FDR. 95 % CI were computed using bootstrapping with 1000 permutations.

P
0.210
0.216
0.216
0.216
0.210
0.210

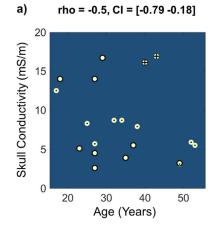
3.2. Statistical Results

The robust pairwise correlation was applied independently between the investigated adult age group and each of the four measures. We also assessed the relationship i) between the thickness of the skull (for all three cranial compartments) and the calibrated skull conductivity and ii) between the P20/N20 surface distance and the source depth.

In Figure 6, we show the statistically significant correlation pairs, i.e., calibrated skull conductivity with age (left subfigure) and calibrated skull conductivity with skull thickness (right subfigure). The remaining correlation pairs are outlined in Table 3 and 4.

When including gender as a between-subject factor in these pairs through linear regression modeling, no statistically significant effect (P > 0.05) could be observed. Therefore, the corresponding ANOVA results are not presented.

In our first investigation, we examined if the defined measures in Section 2.4 are correlated with age. In Fig. 6a, we show that a statis-



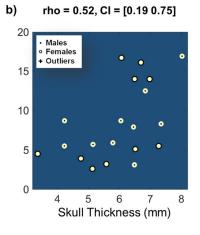


Figure 6. Interaction of skull conductivity with age and skull thickness. The figure contains the robust correlations between the (calibrated) skull conductivity (in mS/m) and a) age (years), b) (full) skull thickness (in mm). The skipped Pearson correlation value (rho) and the confidence interval (CI) are presented on top of both images. 95 % CI were computed using bootstrapping with 1000 permutations. The corresponding FDR adjusted p-value was 0.017 and 0.01 for a) and b), respectively. Notice that the data from the participants are overlapping in case that less than twenty points are depicted.

Table 4
Interaction of the calibrated skull conductivity (skull conductivity) with all the cranial compartment thicknesses and the surface distance with the source depth. The first column indicates the row number, the second the correlation pair, the third the correlation value (rho), the fourth the bootstrapped confidence interval (CI) and the fifth the p-value (P) derived from each bootstrapped CI and adjusted with FDR. 95 % CI were computed using bootstrapping with 1000 permutations.

No	Correlation pair	rho	CI		P
1	(Skull Conductivity, Outer-Compacta Thickness)	-0.25	-0.59	0.17	0.210
2	(Skull Conductivity, Spongiosa Thickness)	0.13	-0.41	0.62	0.216
3	(Skull Conductivity, Inner-Compacta Thickness)	0.26	-0.13	0.61	0.210
4	(Surface Distance, Source Depth)	-0.11	-0.53	0.35	0.216

tically significant negative relationship (rho = -0.5, 95 % CI = [-0.78 - 0.18], P = 0.017) occurs between age and calibrated skull conductivity. One female (43 years old and calibrated skull conductivity: 16.9 mS/m) and one male (40 years old, calibrated skull conductivity: 16.1 mS/m) were identified as outliers (Fig. 6a, two circled black crosses on yellow background). The P20/N20 surface distance has a weak positive interaction with age (Table 3, fifth row: rho = 0.29, 95 % CI = [-0.12 0.64]), while the thicknesses of the full skull, outer compacta, spongiosa and inner skull compacta in the ROI are also weakly, but negatively, correlated with age (Table 3, rows 1–4). For the correlation pair of source depth and age, a positive interaction is observed but not statistically significant (Table 3, row 6: rho = 0.35, 95 % CI = [-0.14 0.65]). No outliers were detected for these correlations.

In our second study, we investigated whether there is a dependence between skull thickness and conductivity, also with the aim of observing whether our non-invasive approach can achieve a similar result as an invasive approach (e.g. Tang et al., 2008). With regard to the correlations between the thickness of all of the cranial compartments in the ROI and the calibrated skull conductivity, the results varied depending on the combination. In Fig. 6b, a statistically significant positive correlation was revealed between skull thickness and calibrated skull conductivity (rho = 0.52, 95 % CI = [0.19 0.75], P = 0.01). The remaining correlation pairs, shown in Table 4, are not statistically significant according to their CIs and p-values. In particular, the thickness of the cranial compartments spongiosa and inner compacta has a low positive interaction with the calibrated skull conductivity (Table 4, rows 2-3), while an opposite low interaction occurs with the outer compacta thickness and the calibrated skull conductivity (Table 4, row 1, rho = -0.25).

For the last correlation pair, i.e., the surface distance and the source depth, we found a marginally negative but non-significant value (Table 4, row 4, rho = -0.11).

No outliers occurred during the assessment of the correlations shown in Table 4.

Taking into account the significant correlations (Fig. 6), a linear mixed-effect analysis 10 was also used to assess the effect of age and full skull thickness on the calibrated skull conductivity based on gender. The predicted variable was the calibrated skull conductivity which age, full skull thickness and gender were the predictor variables (b). From this analysis, we get that age and (full) skull thickness are two significant predictors ($b_{\rm age}=-0.01$ and $b_{\rm skull_thickness}=0.18$, P < 0.05) while gender showed a weak effect ($b_{\rm gender}=-0.39$, P=0.06). In this analysis, similar outliers were observed as presented in Fig. 6.

4. Discussion

In this study in a group of twenty adult subjects in the age of 18 to 53, we estimated and evaluated the inter-subject variability of bulk (calibrated) skull conductivity using the non-invasive modalities EEG and MEG in fusion with MRI, modalities that are available in MEG laboratories and for which ethical clearance is nowadays standard. We proposed a two-level calibration procedure to estimate individual skull conductivity using source analysis based on detailed FEM head modeling of the P20/N20 component of combined SEP and SEF data from electric wrist stimulation. Our most important result is the high inter-subject variability over the investigated age range and in each age subgroup, as the high variances in Figures 4, 5 and 6 clearly illustrate. This means that approaches like the proposed calibration procedure are needed to individually estimate skull conductivity, one of the most important forward modeling parameters in EEG and combined EEG/MEG source analysis (Aydin et al., 2014; Vorwerk et al., 2014, 2019) as well as in transcranial electric stimulation (TES) (Saturnino et al., 2019; Schmidt et al., 2015). Besides the high inter-subject variability, pointing to the need for individualization of experimental procedures, we also found two significant relationships (Fig. 6). Our results therefore motivate the following experimental setup: In a first run of 10 min, SEP and SEF data are

¹⁰ https://www.mathworks.com/help/stats/fitlme.html

collected, serving for head model calibration, followed by the main acquisition runs of combined EEG/MEG data of interest. Then, these main data are being analyzed using the individually calibrated realistic head model.

The application of the presented calibration procedure in a group of twenty adult subjects yielded large inter-subject variability among the estimated skull conductivities (Figs. 4, 5a and 6). This was also reported in a recent review (McCann et al., 2019). Furthermore, other studies using DAC on skull pieces temporarily removed during surgery showed a high inter-subject variability (Hoekema et al., 2003; Tang et al., 2008). For 1 kHz DAC, Tang et al. (2008) indicated a variation of skull conductivity between 3.77 and 17.29 mS/m, which is close to our range of 2.6 to 16.9 mS/m. Arumugam et al. (2017) used EIT in ten subjects and found a skull conductivity variability of 1.8 to 5.6 mS/m. Compared to the above studies, our results (Fig. 4 and Fig. 5a) were found to be in a similar variability range. Those results are measured under in vivo conditions and in the low frequency range of interest, when considering the frequency-dependence of conductivity measurements (Akhtari et al., 2002; Gabriel, Gabriel, & Corthout, 1996; Stinstra et al., 1998; Tang et al., 2008).

In Table 1, we presented the further defined measures from Section 2.4.1 for the source analysis within our skull conductivity calibration procedure. With SNR values of 14.88 \pm 4.20 for SEP and 22.72 ± 7.29 for SEF data, a single run of only 10 min for 1200 trials gave us enough data quality for accurate source analysis. The higher SNR value for MEG compared to EEG for the same number of trials shows the higher sensitivity of MEG than EEG to the rather lateral (Fig. 5, maximally 24 mm deep) and mainly tangentially-oriented (on average $25.5^{\circ} \pm 18.6^{\circ}$ deviation from the tangential plane, being parallel to the inner skull surface) P20/N20 dipole source in Brodmann area 3b. It has been shown in various studies that such sources are better detectable by MEG than by EEG (Goldenholz et al., 2009; Hillebrand & Barnes, 2002; Huang et al., 2007). This higher detectability together with the insensitivity of MEG to skull and skin conductivity (Brette & Destexhe, 2012) supports the idea of relying on MEG dipole scans for an accurate localization within our SEP/SEF calibration procedure. The low residual variance (Fig. 4 and Table 1) shows that the collection of only a single run with 1200 trials together with the model of a focal dipolar P20/N20 source (Allison et al., 1991; Hari et al., 1993; Nakamura et al., 1998) in a calibrated and highly realistic head model seems acceptable for our calibration needs. A simultaneously activated deep thalamic source at the P20/N20 peak as proposed by (Buchner et al., 1994; Fuchs et al., 1998) is hardly detectable in the MEG and therefore also hardly influences our MEG driven localization process. Furthermore, Götz, Huonker, Witte, and Haueisen (2014) showed that in 10 out of 12 subjects, the single dipole model performed accordingly at the P20/N20 peak and in some first test simulations, an additional thalamic source also did not significantly influence our calibration results. The short acquisition time of 10 min for SEP/SEF data is an important advantage when compared to e.g. MREIT, which takes longer (McCann et al., 2019). The computation time for the skull conductivity calibration, including all EEG/MEG forward calculations for six-compartment anisotropic (6CA) head modeling, was an overnight job for each subject, using a conventional laptop (Dell, XPS 15, 2016). We can thus summarize that our proposed calibration procedure is feasible in a standard MEG laboratory with an additional EEG/MEG measurement time of only 10 min per subject.

A particularly strong influence of skull conductivity on EEG forward simulations and EEG source analysis has been reported in many studies using realistic head models of different detail (Akalin Acar et al., 2016; Azizollahi et al., 2016, 2018; Cuartas Morales, Acosta-Medina, Castellanos-Dominguez, & Mantini, 2019; Gençer & Acar, 2004; Montes-Restrepo et al., 2014; Vallaghé & Clerc, 2009; Vorwerk et al., 2019). Previous studies on EEG (Cuartas Morales et al., 2019; Montes-Restrepo et al., 2014) and combined EEG/MEG (Aydin et al., 2014) source analysis also showed that skull conductivity inaccuracies can easily lead to localization errors in the centimeter range. Furthermore, skull

conductivity was also found to be the most influential parameter for optimized TES, as shown in recent uncertainty analyses (Saturnino et al., 2019; Schmidt et al., 2015). Therefore, the use of subject-specific calibrated realistic head volume conductor modeling, as presented in our work, is suggested to take into account the inter-subject variability of skull conductivity in EEG and combined EEG/MEG source analysis as well as in optimized TES.

Based on the results of our correlation analysis, (calibrated) skull conductivity and age showed a significant negative correlation (Fig. 6a). This inverse relationship is in line with previous studies on this topic (Arumugam et al., 2017; Hoekema et al., 2003). In agreement with our result, Hoekema et al. (2003), who worked on a group study with five patients aged 11 to 50 years, found that skull conductivity is higher in younger patients than in older patients. Using EIT, Arumugam and colleagues (2017) found a negative correlation trend in a group study with ten subjects, aged 23 to 49 years. Other studies with mammals such as for example rats (Peyman, Rezazadeh, & Gabriel, 2001; 2007), which however measured skull conductivity at microwave frequency, have also reported such a negative relationship. In the present study, the skull conductivity was estimated by means of a non-invasive procedure based on SEP/SEF recordings in the low frequency range of interest and in an age range from 18 to 53 years. Since EIT and SEP/SEF methods have shown agreement on their estimated skull conductivities (Gonçalves et al., 2003), our resulting correlation of the calibrated skull conductivity with age could have been expected, considering the distribution of the age range used in this study.

Our correlation analysis also yielded a statistically significant positive correlation between skull conductivity and (full) skull thickness (Fig. 6b). This finding is supported by (Tang et al., 2008) who measured resistivities of 388 skull samples, excised from 48 skull flaps of patients undergoing surgery using DAC. Furthermore, we observed a non-significant negative correlation between skull thickness and age (Table 3). As shown by (Delye, Clijmans, Mommaerts, Sloten, & Goffin, 2015; see Fig. 5), skull thickness increases exponentially in the age range from 0 to 18 years, while in the age range from 18 to 20 years, a high inter-subject variability starts dominating an only small remaining linear increase of skull thickness over time. It can be assumed that this variability continues for older subjects, as shown here (Fig. 5b) and similarly supported by (De Boer et al., 2016; Lillie et al., 2016; Lynnerup, Astrup, & Sejrsen, 2005), which makes it difficult to extract a robust correlation of skull thickness with age.

Our significant finding on the relationship of skull conductivity and age could depend on the chosen age range. When excluding the older participants around 50 (49 – 53), we do no longer observe a significant negative correlation (rho = 0.11, CI = [-0.55 0.60]) between calibrated skull conductivity and age. When excluding the same subgroup of participants, we still get a non-significant correlation of spongiosa thickness over age (rho = 0.17, CI = $[-0.30 \ 0.63]$) compared to (Table 3, row 3). This irregularity in the age subgroups over our larger age range should be further studied, also due to the results of (Lynnerup et al., 2005; Figs. 3 – 5), where it was shown that the spongiosa thickness varies nonmonotonically over the large age range from 16 to 90 years. Therefore, a future study should include a larger number of participants, particularly in the age range from 40 to 53, to further investigate the relationship between skull conductivity, age and thickness, with a possible further focus on age subgroups. Finally, osteoporosis (Aspray & Hill, 2019) or osteopetrosis (Boskey & Coleman, 2010) could potentially influence these relationships.

Our evaluated correlation pairs were determined for a group of subjects in the adult age range (age of 18 to 53). The results could differ for groups of subjects in childhood and also in older age. Particularly in newborns, also due to the presence of fontanelles, as well as in the first years of life, cranial development, including skull thickness and skull conductivity, can be considered highly nonlinear (Azizollahi et al., 2016, 2018; Delye et al., 2015; Gibson, Bayford, & Holder, 2000; Li et al., 2015; Odabaee et al., 2014).

Regarding the lack of further significant correlations (Table 3, 4), the limited sample size and the relatively non-uniform age range could be main factors, and remaining modeling simplifications might play a role. Sowell *et al.* (2006) determined that cortical thickness in the post-central gyrus could decrease in the age from 20 to 87, replaced by CSF (Fjell et al., 2010). The latter could be a reason for the positive, however, non-significant, correlation of P20/N20 source depth over age (Table 3). In addition, modeling simplifications, such as the use of standard non-individualized skin and gray matter conductivity values could have influenced our results for the calibrated skull conductivity, source strength and residual variance to the SEP data RV_{SEP} in Table 1 (Vorwerk et al., 2019; Fig. 7).

With regard to gender, the only significant difference we found was the P20/N20 latency (Table 1). The shorter P20/N20 latency we measured in males is in line with previous studies (Allison, Wood, & Goff, 1983; Huttunen et al., 1999) and can easily be attributed to the longer arms of males (Huttunen et al., 1999). Furthermore, even if gender is often considered as an additional factor in the relationship between skull thickness and age (Pellegrini et al., 2018), in our data inter-subject variability limits the possibility of an observation of such a gender effect. Since skull thickness and conductivity are related (Fig. 6b and Tang et al., 2008), we assumed that through a possible influence of gender on skull thickness, an indirect influence of gender on skull conductivity could also exist. However, as ANOVA analysis showed, no gender effect was observed (P > 0.1). Considering also gender in a linear mixedeffects analysis (Section 3.2), age and full skull thickness remained significant predictors of the calibrated skull conductivity while gender was weak (P = 0.06). Considering the variability of cranial thickness in both subgroups (Fig. 5b, Table 2) which is supported by (De Boer et al., 2016; Lillie et al., 2016), the absence of a gender effect could be expected. These two studies used a large number of CT datasets and also showed no significant gender differences for thickness of the skull regions in the left hemisphere. Our and their results mainly only emphasize the large inter-subject variability. In summary, due to the large inter-subject variability, the evaluation of gender effects and differences in the measures studied here might remain a challenging task.

Two subjects in the age of 40 and 43 were detected as outliers in the correlation pair presented in (Fig. 6a) due to their exceptionally high calibrated skull conductivity. We found that their average skull thicknesses of 6.5 mm and 8 mm in the defined skull ROI (Fig. 2b) was also relatively large, with large variation over the ROI (3.4 – 8 mm). However, while in our group study, these values were on the higher side, according to (Fig. 6 in Tang et al., 2008, Fig. 1 in De Boer et al., 2016), even higher thicknesses can be found. We expect that a larger number of participants in the age range of 40 would smoothen the skull thickness range presented in this study.

The selected age group in this study reflects the age range of the subject pool at a MEG center, with fewer data points in the range under 22 and over 40 and many participants of student age. In particular, however, this study is an important part of an epilepsy project to investigate whether combined EEG/MEG analysis in individualized head-volume conductor models with calibrated skull conductivity can provide a better estimate of the epileptogenic zone. Of particular interest is the comparison to EEG or MEG single-modality analyses and analyses using simplified and non-calibrated head models. In first proofof-principle studies, a superiority of combined EEG/MEG analysis using head models calibrated for skull conductivity has already been shown (Aydin et al., 2015, 2017). Most epilepsy patients in presurgical epilepsy diagnosis - a main clinical application of EEG/MEG source analysis - in whom surgery is considered are also in the age group as investigated here (Rampp et al., 2019). Therefore, in especially this age range, individually calibrated skull conductivity can provide useful information for epilepsy diagnostics. Thus, it was our specific interest to use a noninvasive method using hardware available in a MEG center to investigate how age and gender can influence skull conductivity and thickness in middle-aged adults. We therefore did not collect the same number of participants in all age subgroups, but we only paid attention to an equal number of men and women for the gender investigations. The main result of our study, namely to show the need for individually calibrated head models for a combined EEG/MEG source analysis due to the large variance in skull conductivity for this important age range, could therefore be achieved.

Correlations between skull conductivity, thickness and age in child-hood have not been examined here due to the limitation of our ethics vote to adult studies. Future studies using our non-invasive procedure could thus investigate not only larger sample sizes, but also include the childhood age range, and thereby stabilize the statistics for an analysis in a complete age-range. It would also be interesting to investigate how other factors, e.g., nutrition or health, might influence the defined measures.

Within the construction of the realistic head models in Section 2.2, modifications in the erosion operator would have influenced the determined ratio between cancellous and cranial bone. An erosion of only 1 mm could have resulted in too thin inner and outer compacta and could have thereby led to 'skull leakage' as described by (Engwer, Vorwerk, Ludewig, & Wolters, 2017; Piastra et al., 2018). A higher erosion value (> 2 mm) could have artificially reduced the skull spongiosa and increased the inner and outer compacta thicknesses, which would in turn have increased our value for calibrated skull conductivity. In the future, investigations will be carried out for the use of level set tissue segmentation approaches in combination with unfitted finite element methods that better take into account the partial volume effects (Nüßing et al., 2016), and its influence on skull conductivity calibration.

In order to avoid overfitting (Wolters et al., 2010; Lew et al., 2009), we only allowed one degree of freedom in our calibration procedure for the most influential parameter as detected by uncertainty analysis, namely skull conductivity (Vorwerk et al., 2019; Saturnino et al., 2019). We cannot exclude that possible inter-subject variabilities in skin or GM conductivity could have influenced our calibrated skull conductivity values (Vorwerk et al., 2019; Saturnino et al., 2019). However, for the influence of the second most important parameter for the EEG, namely skin conductivity (Vorwerk et al., 2019, Figs. 7 and 9), it was also found that for lower skull conductivities, variability of skin conductivity has a smaller influence on source depth (Vorwerk et al., 2019; Fig. 9). Furthermore, since MEG is insensitive to skin conductivity, at least our source localizations and source depths should be mainly not influenced by individual variations in skin conductivity. An overlayed thalamic activity might also simultaneously be present in the P20/N20 component in a small percentage of subjects (Götz et al., 2014). Still, future studies are needed to determine the potential of these effects on the calibration procedure.

Our head models ignored the volume conduction effects of the dura (Ramon, Garguilo, Fridgeirsson, & Haueisen, 2014), blood vessels (Fiederer et al., 2016) as well as local skull inhomogeneities such as sutures, which could provide a path of higher conductance (Tang et al., 2008; Ollikainen, Vauhkonen, Karjalainen, & Kaipio, 1999; Pohlmeier et al., 1997). In addition, following (Baumann et al., 1997) for CSF conductivity, we assumed a fixed value of 1.79 S/m at body temperature, which is nearly identical to the recommended weighted mean value of 1.71 S/m of a recent meta-analysis (McCann et al., 2019). In the latter study, however, a larger variability of CSF conductivity was reported when using MREIT instead of DAC for its determination (Fig. 8 in McCann et al., 2019). These are the main reasons why we have consistently used the terms 'estimation' or 'calibration' of skull conductivity in this study, since the term 'determination' would have feigned too much precision. Despite these limitations, we believe that our proposed procedure is a considerable step forward when compared to the current standard, i.e., the use of non-individual literature-based or only age-dependent skull conductivity values.

We fixed the conductivity ratio between skull compacta and spongiosa, using the measurements of (Akhtari et al., 2002), again with the main argument to avoid overfitting (Wolters et al., 2010; Lew et al., 2009). First of all, skull conductivity calibration with such a fixed conductivity ratio for compacta:spongiosa has been successfully used in a proof-of-principle study for combined EEG/MEG source analysis in presurgical epilepsy diagnosis (Aydin et al., 2017). Secondly, also the simulation studies of (Montes-Restrepo et al., 2014; Dannhauer et al., 2011; Vorwerk et al., 2014) support the use of skull modeling approaches that distinguish between skull spongiosa and compacta. However, it was also shown that for the somatosensory cortex this distinction causes only a weak effect in both EEG and MEG when using an optimized conductivity value for the homogenized full skull compartment (Fig. 12 in Vorwerk et al., 2014). Therefore, we do not expect that a calibration similar to our approach would be able to additionally estimate an individual ratio as a second degree of freedom. For the MEG, the observed effect on forward solutions was even much smaller compared to EEG (Fig. 12 in Vorwerk et al., 2014), and since our calibration uses the MEG for the localization part, we do not expect a high sensitivity of our calibration procedure on the chosen ratio. Skull conductivity calibration could also be performed using a homogenized full skull compartment, which would lead to a calibration value reflecting the combined effect of both compartments. Because of the overall weak effect of the spongiosa compartment on EEG and especially MEG forward solutions for somatosensory sources (Fig. 12 in Vorwerk et al., 2014), we expect only moderate changes in the calibration value.

Finally, comparison with EIT and/or combination with EIT procedures are also interesting as future goals (Gonçalves et al., 2003). Calibration procedures might be studied that exploit other SEP/SEF (left median nerve, tibial nerve, trigeminal nerve) or auditory or visually evoked potential (AEP, VEP) and field (AEF, VEF) data in order to calibrate other skull ROI's. Combinations of such calibration datasets might even allow the use of more than one degree of freedom in the calibration process, which, if presented alternately, need not even extend the measurement time.

5. Conclusion

In this group study with twenty participants, we evaluated the intersubject variability of skull conductivity in the context of combined EEG/MEG source analysis using a non-invasive calibration procedure. Our method is based on the reconstruction of the SEP and SEF P20/N20 component with subject-specific realistic head modeling. We found large inter-subject variability for the calibrated skull conductivity, as well as for the examined related measures of skull thickness, P20/N20 surface distance and source depth. Our statistical analysis shows that the calibrated skull conductivity is significantly related to the skull thickness and age of the participants with no clear gender effects. We did not find gender differences besides a significantly shorter P20/N20 latency in females than males. In the context of source analysis of EEG or combined EEG/MEG data and also for optimized TES, our study emphasized the critical importance of taking the inter-subject variabilities of skull conductivity and thickness into account. We therefore propose the additional measurement of the individual SEP/SEF P20/N20 component and its use for subject-specific calibrated realistic head modeling. Our procedure is non-invasive and easily applicable in a standard MEG laboratory.

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Data and Code Availability

The data that support the results of this group study are available in anonymized form on request from the corresponding author. The data are not publicly available due to privacy or ethical restrictions.

The developed code in the present study is part of an ongoing research project and only parts of it can be made available on request by the corresponding author. The third-party code used in the present study is either cited accordingly or the corresponding openly available code repository is provided via a link in the footnote that a description of the code exists.

Author contributions

Marios Antonakakis: Conceptualization, Methodology, Visualization, Formal analysis, Writing - Original Draft, Writing - Review & Editing; Sophie Schrader: Writing - Review & Editing; Ümit Aydin: Conceptualization; Asad Khan: Writing - Review & Editing; Joachim Gross: Writing - Review & Editing; Michalis Zervakis: Writing - Review & Editing; Stefan Rampp: Resources, Writing - Review & Editing; Carsten H. Wolters: Conceptualization, Supervision, Resources, Project administration, Writing - Review & Editing.

Declaration of Competing Interest

None

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References

- Abascal, J.-F.P.J., Arridge, S.R., Atkinson, D., Horesh, R., Fabrizi, L., Lucia, M.de, Horesh, L., Bayford, R.H., Holder, D.S., 2008. Use of anisotropic modelling in electrical impedance tomography: Description of method and preliminary assessment of utility in imaging brain function in the adult human head. NeuroImage 43 (2), 258–268. https://doi.org/10.1016/j.neuroimage.2008.07.023.
- Akalin Acar, Z., Acar, C.E., Makeig, S., 2016. Simultaneous head tissue conductivity and EEG source location estimation. NeuroImage 124, 168–180. https://doi.org/10.1016/j.neuroimage.2015.08.032.
- Altakroury, H. F. (2017). In-vivo human head conductivity estimation by SEEG and EEG recorded in simultaneous with intracerebral electrical stimulation. Automatic. Université de Lorraine. English. ffNNT: 2017LORR0304ff. fftel-01709247f
- Akhtari, M., Bryant, H.C., Mamelak, A.N., Flynn, E.R., Heller, L., Shih, J.J., Mandelkern, M., Matlachov, A., Ranken, D.M., Best, E.D., DiMauro, M.A., Lee, R.R., Sutherling, W.W., 2002. Conductivities of three-layer live human skull. Brain topography 14 (3), 151–167. https://doi.org/10.1023/a:1014590923185.
- Allison, T., McCarthy, G., Wood, C.C., Jones, S.J., 1991. Potentials evoked in human and monkey cerebral cortex by stimulation of the median nerve. A review of scalp and intracranial recordings. Brain 114 (6), 2465–2503. https://doi.org/10.1093/brain/114.6.2465.
- Allison, T., Wood, C.C., Goff, W.R., 1983. Brain stem auditory, pattern-reversal visual, and short-latency somatosensory evoked potentials: Latencies in relation to age, sex, and brain and body size. Electroencephalography and clinical neurophysiology 55 (6), 619-636. https://doi.org/10.1016/0013-4694(83)90272-9.
- Antonakakis, M., Schrader, S., Wollbrink, A., Oostenveld, R., Rampp, S., Haueisen, J., Wolters, C.H., 2019. The effect of stimulation type, head modeling, and combined EEG and MEG on the source reconstruction of the somatosensory P20/N20 component. Hum Brain Mapp 40 (17), 5011–5028. https://doi.org/10.1002/hbm.24754.
- Arumugam, E.M.E., Turovets, S., Price, N., Rech, D., Luu, P., Tucker, D.M. (Eds.), In vivo estimation of scalp and skull conductivity using bEIT for non-invasive neuroimaging and stimulation, 2017. Brain Stimulation and Imaging Meeting, Vancouver.
- Aspray, T.J., Hill, T.R., 2019. Osteoporosis and the Ageing Skeleton. Sub-cellular biochemistry 91, 453–476. https://doi.org/10.1007/978-981-13-3681-2_16.
- Aydin, Ü., Vorwerk, J., Küpper, P., Heers, M., Kugel, H., Galka, A., Hamid, L., Wellmer, J., Kellinghaus, C., Rampp, S., Wolters, C.H., 2014. Combining EEG and MEG for the Reconstruction of Epileptic Activity Using a Calibrated Realistic Volume Conductor Model. PLoS ONE 9 (3), e93154. https://doi.org/10.1371/journal.pone.0093154.
- Aydin, Ü., Vorwerk, J., Dümpelmann, M., Küpper, P., Kugel, H., Heers, M., Wellmer, J., Kellinghaus, C., Haueisen, J., Rampp, S., Stefan, H., Wolters, C.H., 2015. Combined EEG/MEG can outperform single modality EEG or MEG source

- reconstruction in presurgical epilepsy diagnosis. PloS one 10 (3), e0118753. https://doi.org/10.1371/journal.pone.0118753.
- Aydin, Ü., Rampp, S., Wollbrink, A., Kugel, H., Cho, J.-H., Knösche, T.R., Grova, C., Wellmer, J., Wolters, C.H., 2017. Zoomed MRI Guided by Combined EEG/MEG Source Analysis: A Multimodal Approach for Optimizing Presurgical Epilepsy Work-up and its Application in a Multi-focal Epilepsy Patient Case Study. Brain Topogr 30 (4), 417–433. https://doi.org/10.1007/s10548-017-0568-9.
- Azizollahi, H., Aarabi, A., Wallois, F., 2016. Effects of uncertainty in head tissue conductivity and complexity on EEG forward modeling in neonates. Hum. Brain Mapp. 37 (10), 3604–3622. https://doi.org/10.1002/hbm.23263.
- Azizollahi, H., Darbas, M., M. Diallo, M., El Badia, A., Lohrengel, S., 2018. EEG in neonates: Forward modeling and sensitivity analysis with respect to variations of the conductivity. Mathematical Biosciences & Engineering 15 (4), 905–932. https://doi.org/10.3934/mbe.2018041.
- Bauer, M., Pursiainen, S., Vorwerk, J., Kostler, H., Wolters, C.H., 2015. Comparison Study for Whitney (Raviart–Thomas)-Type Source Models in Finite-Element-Method-Based EEG Forward Modeling. IEEE Trans. Biomed. Eng. 62 (11), 2648–2656. https://doi.org/10.1109/TBME.2015.2439282.
- Baumann, S.B., Wozny, D.R., Kelly, S.K., Meno, F.M., 1997. The electrical conductivity of human cerebrospinal fluid at body temperature. IEEE Trans. Biomed. Eng. 44 (3), 220–223. https://doi.org/10.1109/10.554770.
- Baysal, U.u., Haueisen, J., 2004. Use of a priori information in estimating tissue resistivities—application to human data in vivo. Physiol. Meas. 25 (3), 737–748. https://doi.org/10.1088/0967-3334/25/3/013.
- Benjamini, Y., Hochberg, Y., 1995. Controlling the False Discovery Rate: A Practical and Powerful Approach to Multiple Testing. J. Royal Statistical Society. Series B (Methodological) 57 (1), 289–300.
- Boskey, A.L., Coleman, R., 2010. Aging and bone. J. dental research 89 (12), 1333–1348. https://doi.org/10.1177/0022034510377791.
- Boto, E., Holmes, N., Leggett, J., Roberts, G., Shah, V., Meyer, S.S., Muñoz, L.D., Mullinger, K.J., Tierney, T.M., Bestmann, S., Barnes, G.R., Bowtell, R., Brookes, M.J., 2018. Moving magnetoencephalography towards real-world applications with a wearable system. Nature 555 (7698), 657–661. https://doi.org/10.1038/nature26147.
- Brette, R., Destexhe, A., 2012. Handbook of Neural Activity Measurement. Cambridge University Press, Cambridge.
- Buchner, H., Fuchs, M., Wischmann, H.A., Dössel, O., Ludwig, I., Knepper, A., Berg, P., 1994. Source analysis of median nerve and finger stimulated somatosensory evoked potentials: Multichannel simultaneous recording of electric and magnetic fields combined with 3D-MR tomography. Brain topography 6 (4), 299–310. https://doi.org/10.1007/bf01211175.
- Buchner, H., Knoll, G., Fuchs, M., Rienäcker, A., Beckmann, R., Wagner, M., Silny, J., Pesch, J., 1997. Inverse localization of electric dipole current sources in finite element models of the human head. Electroencephalography and clinical neurophysiology 102 (4), 267–278. https://doi.org/10.1016/S0013-4694(96)95698-9.
- Cuartas Morales, E., Acosta-Medina, C.D., Castellanos-Dominguez, G., Mantini, D., 2019. A Finite-Difference Solution for the EEG Forward Problem in Inhomogeneous Anisotropic Media. Brain Topogr 32 (2), 229–239. https://doi.org/10.1007/s10548-018-0683-2.
- Dabek, J., Kalogianni, K., Rotgans, E., van der Helm, F.C.T., Kwakkel, G., van Wegen, E.E.H., Daffertshofer, A., Munck, J.C.de, 2016. Determination of head conductivity frequency response in vivo with optimized EIT-EEG. NeuroImage 127, 484–495. https://doi.org/10.1016/j.neuroimage.2015.11.023.
- Dannhauer, M., Lanfer, B., Wolters, C.H., Knösche, T.R., 2011. Modeling of the human skull in EEG source analysis. Hum. Brain Mapp. 32 (9), 1383–1399. https://doi.org/10.1002/hbm.21114.
- Dassios, G., Fokas, A.S., Hadjiloizi, D., 2007. On the complementarity of electroencephalography and magnetoencephalography. Inverse Problems 23 (6), 2541–2549. https://doi.org/10.1088/0266-5611/23/6/016.
- De Boer, H.H., van der Merwe, A.E., Soerdjbalie-Maikoe, V., 2016. Human cranial vault thickness in a contemporary sample of 1097 autopsy cases: Relation to body weight, stature, age, sex and ancestry. Int J Legal Med 130 (5), 1371–1377. https://doi.org/10.1007/s00414-016-1324-5.
- Delye, H., Clijmans, T., Mommaerts, M.Y., Sloten, J.V., Goffin, J., 2015. Creating a normative database of age-specific 3D geometrical data, bone density, and bone thickness of the developing skull: A pilot study. PED 16 (6), 687–702. https://doi.org/10.3171/2015.4.PEDS1493.
- Engwer, C., Vorwerk, J., Ludewig, J., Wolters, C.H., 2017. A Discontinuous Galerkin Method to Solve the EEG Forward Problem Using the Subtraction Approach. SIAM J. Sci. Comput. 39 (1), B138–B164. https://doi.org/10.1137/15M1048392.
- Fernández-Corazza, M., Turovets, S., Luu, P., Price, N., Muravchik, C.H., Tucker, D., 2018. Skull Modeling Effects in Conductivity Estimates Using Parametric Electrical Impedance Tomography. IEEE transactions on bio-medical engineering 65 (8), 1785– 1797. https://doi.org/10.1109/TBME.2017.2777143.
- Fjell, A.M., Walhovd, K.B., Fennema-Notestine, C., McEvoy, L.K., Hagler, D.J., Holland, D., Blennow, K., Brewer, J.B., Dale, A.M.Alzheimer's Disease Neuroimaging Initiative, 2010. Brain atrophy in healthy aging is related to CSF levels of Aβ1-42. Cerebral cortex 20 (9), 2069–2079. https://doi.org/10.1093/cercor/bhp279.
- Fiederer, L.D.J., Vorwerk, J., Lucka, F., DANNHAUER, M., Yang, S., Dümpelmann, M., Schulze-Bonhage, A., Aertsen, A., Speck, O., Wolters, C.H., Ball, T., 2016. The role of blood vessels in high-resolution volume conductor head modeling of EEG. NeuroImage 128, 193–208. https://doi.org/10.1016/j.neuroimage.2015.12.041.
- Fuchs, M., Wagner, M., Wischmann, H.A., Köhler, T., Theissen, A., Drenckhahn, R., Buchner, H., 1998. Improving source reconstructions by combining bioelectric and biomagnetic data. Electroencephalography and clinical neurophysiology 107 (2), 93–111. https://doi.org/10.1016/s0013-4694(98)00046-7.
- Gabriel, C., Gabriel, S., Corthout, E., 1996. The dielectric properties of biological tis-

- sues: I. Literature survey. Physics in medicine and biology 41 (11), 2231–2249. https://doi.org/10.1088/0031-9155/41/11/001.
- Gao, N., Zhu, S.A., He, B., 2006. A new magnetic resonance electrical impedance tomography (MREIT) algorithm: The RSM-MREIT algorithm with applications to estimation of human head conductivity. Phys Med Biol 51 (12), 3067–3083. https://doi.org/10.1088/0031-9155/51/12/005.
- Gençer, N.G., Acar, C.E., 2004. Sensitivity of EEG and MEG measurements to tissue conductivity. Physics in medicine and biology 49 (5), 701–717. https://doi.org/10.1088/0031-9155/49/5/004.
- Gibson, A., Bayford, R.H., Holder, D.S., 2000. Two-dimensional finite element modelling of the neonatal head. Physiological measurement 21 (1), 45–52. https://doi.org/10.1088/0967-3334/21/1/306.
- Goldenholz, D.M., Ahlfors, S.P., Hämäläinen, M.S., Sharon, D., Ishitobi, M., Vaina, L.M., Stufflebeam, S.M., 2009. Mapping the signal-to-noise-ratios of cortical sources in magnetoencephalography and electroencephalography. Hum. Brain Mapp. 30 (4), 1077– 1086. https://doi.org/10.1002/hbm.20571.
- Gonçalves, S., Munck, J.C.de, Verbunt, J.P.A., Heethaar, R.M., Lopes da Silva, F.H., 2003. In vivo measurement of the brain and skull resistivities using an eit-based method and the combined analysis of sef/sep data. IEEE Trans. Biomed. Eng. 50 (9), 1124–1128. https://doi.org/10.1109/TBME.2003.816072.
- Gorbenko, I., Mikołajczyk, K., Jasionowska, M., Narloch, J., Kałużyński, K., 2020. Automatic segmentation of facial soft tissue in MRI data based on non-rigid normalization in application to soft tissue thickness measurement. Biomedical Signal Processing and Control 56, 101698. https://doi.org/10.1016/j.bspc.2019.101698.
- Götz, T., Huonker, R., Witte, O.W., Haueisen, J., 2014. Thalamocortical Impulse Propagation and Information Transfer in EEG and MEG. J. Clinical Neurophysiology 31 (3), 253–260. https://doi.org/10.1097/WNP.0000000000000048.
- Guler, S., Dannhauer, M., Erem, B., Macleod, R., Tucker, D., Turovets, S., Luu, P., Erdogmus, D., Brooks, D.H., 2016. Optimization of focality and direction in dense electrode array transcranial direct current stimulation (tDCS). J. Neural Eng. 13 (3), 36020. https://doi.org/10.1088/1741-2560/13/3/036020.
- Hari, R., Karhu, J., Hämäläinen, M., Knuutila, J., Salonen, O., Sams, M., Vilkman, V., 1993. Functional Organization of the Human First and Second Somatosensory Cortices: A Neuromagnetic Study. European J. Neuroscience 5 (6), 724–734. https://doi.org/10.1111/j.1460-9568.1993.tb00536.x.
- Haueisen, J., Ramon, C., Eiselt, M., Brauer, H., Nowak, H., 1997. Influence of tissue resistivities on neuromagnetic fields and electric potentials studied with a finite element model of the head. IEEE Trans. Biomed. Eng. 44 (8), 727–735. https://doi.org/10.1109/10.605429.
- Hillebrand, A., Barnes, G.R., 2002. A Quantitative Assessment of the Sensitivity of Whole-Head MEG to Activity in the Adult Human Cortex. NeuroImage 16 (3), 638–650. https://doi.org/10.1006/nimg.2002.1102.
- Hoekema, R., Wieneke, G.H., Leijten, F.S.S., van Veelen, C.W.M., van Rijen, P.C., Huiskamp, G.J.M., Ansems, J., van Huffelen, A.C., 2003. Measurement of the conductivity of skull, temporarily removed during epilepsy surgery. Brain topography 16 (1), 29–38. https://doi.org/10.1023/a:1025606415858.
- Horesh, L. (2006). Some Novel Approaches in Modelling and Image Reconstruction for Multi-Frequency Electrical Impedance Tomography of the Human Brain.
- Huang, M.-X., Song, T., Hagler, D.J., Podgorny, I., Jousmaki, V., Cui, L., Gaa, K., Harrington, D.L., Dale, A.M., Lee, R.R., Elman, J., Halgren, E., 2007. A novel integrated MEG and EEG analysis method for dipolar sources. NeuroImage 37 (3), 731–748. https://doi.org/10.1016/j.neuroimage.2007.06.002.
- Huang, Y., Datta, A., Bikson, M., Parra, L.C., 2019. Realistic volumetric-approach to simulate transcranial electric stimulation—ROAST—a fully automated open-source pipeline. J. Neural Eng. 16 (5), 56006. https://doi.org/10.1088/1741-2552/ab208d.
- Huang, Y., Liu, A.A., Lafon, B., Friedman, D., Dayan, M., Wang, X., Bikson, M., Doyle, W.K., Devinsky, O., Parra, L.C., 2017. Measurements and models of electric fields in the in vivo human brain during transcranial electric stimulation. eLife 6, e18834. 258 https://doi.org/10.7554/eLife.18834.
- Huttunen, J., Tolvanen, H., Heinonen, E., Voipio, J., Wikström, H., Ilmoniemi, R.J., Hari, R., Kaila, K., 1999. Effects of voluntary hyperventilation on cortical sensory responses. Experimental brain research 125 (3), 248–254. https://doi.org/10.1007/s002210050680.
- Knösche, T.R., 1997. Solutions of the neuroelectromagnetic inverse problem PhD Thesis. University of Twente, Enschede, The Netherlands.
- Labyt, E., Corsi, M.C., Fourcault, W., Palacios Laloy, A., Bertrand, F., Lenouvel, F., Cauffet, G., Le Prado, M., Berger, F., Morales, S., 2019. Magnetoencephalography With Optically Pumped 4He Magnetometers at Ambient Temperature. IEEE transactions on medical imaging 38 (1), 90–98. https://doi.org/10.1109/TMI.2018.2856367.
- Lew, S., Sliva, D.D., Choe, M.S., et al., 2013. Effects of sutures and fontanels on MEG and EEG source analysis in a realistic infant head model. Neuroimage 76, 282-293. doi:10.1016/j.neuroimage.2013.03.017.
- Lew, S., Wolters, C.H., Anwander, A., Makeig, S., MacLeod, R.S., 2009. Improved EEG source analysis using low-resolution conductivity estimation in a fourcompartment finite element head model. Hum. Brain Mapp. 30 (9), 2862–2878. https://doi.org/10.1002/hbm.20714.
- Li, X., Yu, K., He, B., 2016. Magnetoacoustic tomography with magnetic induction (MAT-MI) for imaging electrical conductivity of biological tissue: A tutorial review. Phys Med Biol 61 (18), R249–R270.
- Li, Z., Park, B.-K., Liu, W., Zhang, J., Reed, M.P., Rupp, J.D., Hoff, C.N., Hu, J., 2015. A Statistical Skull Geometry Model for Children 0-3 Years Old. PLoS ONE 10 (5), e0127322. https://doi.org/10.1371/journal.pone.0127322.
- Lillie, E.M., Urban, J.E., Lynch, S.K., Weaver, A.A., Stitzel, J.D., 2016. Evaluation of Skull Cortical Thickness Changes With Age and Sex From Computed Tomography Scans. J Bone Miner Res 31 (2), 299–307. https://doi.org/10.1002/jbmr.2613.
- Lynnerup, N., Astrup, J.G., Sejrsen, B., 2005. Thickness of the human cranial diploe

- in relation to age, sex and general body build. Head Face Med 1 (1), 270. https://doi.org/10.1186/1746-160X-1-13.
- Mann, H.B., Whitney, D.R., 1947. On a Test of Whether one of Two Random Variables is Stochastically Larger than the Other. Ann. Math. Statist. 18 (1), 50–60. https://doi.org/10.1214/aoms/1177730491.
- Massey, F.J., 1951. The Kolmogorov-Smirnov Test for Goodness of Fit. J. American Statistical Association 46 (253), 68–78.
- McCann, H., Pisano, G., Beltrachini, L., 2019. Variation in Reported Human Head Tissue Electrical Conductivity Values. Brain Topogr 32 (5), 825–858. https://doi.org/10.1007/s10548-019-00710-2.
- Montes-Restrepo, V., van Mierlo, P., Strobbe, G., Staelens, S., Vandenberghe, S., Hallez, H., 2014. Influence of Skull Modeling Approaches on EEG Source Localization. Brain Topogr 27 (1), 95–111. https://doi.org/10.1007/s10548-013-0313-y.
- Nakamura, A., Yamada, T., Goto, A., Kato, T., Ito, K., Abe, Y., Kachi, T., Kakigi, R., 1998. Somatosensory homunculus as drawn by MEG. NeuroImage 7 (4 Pt 1), 377–386. https://doi.org/10.1006/nimg.1998.0332.
- Nielsen, J.D., Madsen, K.H., Puonti, O., Siebner, H.R., Bauer, C., Madsen, C.G., Saturnino, G.B., Thielscher, A., 2018. Automatic skull segmentation from MR images for realistic volume conductor models of the head: Assessment of the state-of-the-art. NeuroImage 174, 587–598. https://doi.org/10.1016/j.neuroimage.2018.03.001.
- Nunez, P.L., Srinivasan, R., 2006. Electric fields of the brain: The neurophysics of EEG. Oxford Univ. Press, Oxford, p. 611.
- Odabaee, M., Tokariev, A., Layeghy, S., Mesbah, M., Colditz, P.B., Ramon, C., Vanhatalo, S., 2014. Neonatal EEG at scalp is focal and implies high skull conductivity in realistic neonatal head models. NeuroImage 96, 73–80. https://doi.org/10.1016/j.neuroimage.2014.04.007.
- Ollikainen, J.O., Vauhkonen, M., Karjalainen, P.A., Kaipio, J.P., 1999. Effects of local skull inhomogeneities on EEG source estimation. Medical engineering & physics 21 (3), 143–154. https://doi.org/10.1016/s1350-4533(99)00038-7.
- Oostendorp, T.F., Delbeke, J., Stegeman, D.F., 2000. The conductivity of the human skull: Results of in vivo and in vitro measurements. IEEE Trans. Biomed. Eng. 47 (11), 1487–1492. https://doi.org/10.1109/TBME.2000.880100.
- Oostenveld, R., Fries, P., Maris, E., Schoffelen, J.-M., 2011. FieldTrip: Open source software for advanced analysis of MEG, EEG, and invasive electro-physiological data. Computational Intelligence and Neuroscience 2011, 156869. https://doi.org/10.1155/2011/156869.
- Papageorgakis, C., 2017. Patient specific conductivity models: Characterization of the skull bones Ph.D. thesis. Université Côte d'Azur, France.
- Pellegrini, M., Zoghi, M., Jaberzadeh, S., 2018. Biological and anatomical factors influencing interindividual variability to noninvasive brain stimulation of the primary motor cortex: A systematic review and meta-analysis. Reviews in the neurosciences 29 (2), 199–222. https://doi.org/10.1515/revneuro-2017-0048.
- Pernet, C.R., Wilcox, R., Rousselet, G.A., 2013. Robust Correlation Analyses: False Positive and Power Validation Using a New Open Source Matlab Toolbox. Front. Psychology 3. https://doi.org/10.3389/fpsyg.2012.00606.
- Pernier, J., Perrin, F., Bertrand, O., 1988. Scalp current density fields: Concept and properties. Electroencephalography and clinical neurophysiology 69 (4), 385–389. https://doi.org/10.1016/0013-4694(88)90009-0.
- Peyman, A., Holden, S.J., Watts, S., Perrott, R., Gabriel, C., 2007. Dielectric properties of porcine cerebrospinal tissues at microwave frequencies: In vivo, in vitro and systematic variation with age. Phys. Med. Biol. 52 (8), 2229–2245. https://doi.org/10.1088/0031-9155/52/8/013.
- Peyman, A., Rezazadeh, A.A., Gabriel, C., 2001. Changes in the dielectric properties of rat tissue as a function of age at microwave frequencies. Phys. Med. Biol. 46 (6), 1617–1629. https://doi.org/10.1088/0031-9155/46/6/303.
- Piastra, M.C., Nüßing, A., Vorwerk, J., Bornfleth, H., Oostenveld, R., Engwer, C., Wolters, C.H., 2018. The Discontinuous Galerkin Finite Element Method for Solving the MEG and the combined MEG/EEG Forward Problem. Frontiers in Neuroscience: Brain Imaging Methods.
- Pohlmeier, R., Buchner, H., Knoll, G., Rienäcker, A., Beckmann, R., Pesch, J., 1997. The influence of skull-conductivity misspecification on inverse source localisation in realistically shaped finite element head models. Brain Top 9, 157–162.
- Ramon, C., Garguilo, P., Fridgeirsson, E.A., Haueisen, J., 2014. Changes in scalp potentials and spatial smoothing effects of inclusion of dura layer in human head models for EEG simulations. Front. Neuroeng. 7, 1383. https://doi.org/10.3389/fneng.2014.00032.
- Ramon, C., Schimpf, P.H., Haueisen, J., 2004. Effect of model complexity on EEG source localizations. Neurology & clinical neurophysiology: NCN 2004, 81.

- Rampp, S., Stefan, H., Wu, X., Kaltenhäuser, M., Maess, B., Schmitt, F.C., Wolters, C.H., Hamer, H., Kasper, B.S., Schwab, S., Doerfler, A., Blümcke, I., Rössler, K., Buchfelder, M., 2019. Magnetoencephalography for epileptic focus localization in a series of 1000 cases. Brain: A journal of neurology 142 (10), 3059–3071. https://doi.org/10.1093/brain/awz231.
- Rice, J.K., Rorden, C., Little, J.S., Parra, L.C., 2013. Subject position affects EEG magnitudes. NeuroImage 64, 476–484. https://doi.org/10.1016/j.neuroimage.2012.09.041.
- Ruthotto, L., Kugel, H., Olesch, J., Fischer, B., Modersitzki, J., Burger, M., Wolters, C.H., 2012. Diffeomorphic susceptibility artifact correction of diffusionweighted magnetic resonance images. Phys. Med. Biol. 57 (18), 5715–5731. https://doi.org/10.1088/0031-9155/57/18/5715.
- Sadleir, R.J., Vannorsdall, T.D., Schretlen, D.J., Gordon, B., 2012. Target Optimization in Transcranial Direct Current Stimulation. Front. Psychiatry 3. https://doi.org/10.3389/fpsyt.2012.00090.
- Saturnino, G.B., Thielscher, A., Madsen, K.H., Knösche, T.R., Weise, K., 2019. A principled approach to conductivity uncertainty analysis in electric field calculations. NeuroImage 188, 821–834. https://doi.org/10.1016/j.neuroimage.2018.12.053.
- Schmidt, C., Wagner, S., Burger, M., van Rienen, U., Wolters, C.H., 2015. Impact of uncertain head tissue conductivity in the optimization of transcranial direct current stimulation for an auditory target. J. Neural Eng. 12 (4), 46028. https://doi.org/10.1088/1741-2560/12/4/046028.
- Stinstra, J.G., Peters, M.J., 1998. The volume conductor may act as a temporal filter on the ECG and EEG. Med. Biol. Eng. Comput. 36 (6), 711–716. https://doi.org/10.1007/BF02518873.
- Tang, C., You, F., Cheng, G., Gao, D., Fu, F., Yang, G., Dong, X., 2008. Correlation Between Structure and Resistivity Variations of the Live Human Skull. IEEE Trans. Biomed. Eng. 55 (9), 2286–2292. https://doi.org/10.1109/TBME.2008.923919.
- Tuch, D.S., Wedeen, V.J., Dale, A.M., George, J.S., Belliveau, J.W., 2001. Conductivity tensor mapping of the human brain using diffusion tensor MRI. Proceedings of the National Academy of Sciences of the United States of America 98 (20), 11697–11701. https://doi.org/10.1073/pnas.171473898.
- Vallaghé, S., Clerc, M., 2009. A Global Sensitivity Analysis of Three- and Four-Layer EEG Conductivity Models. IEEE Trans. Biomed. Eng. 56 (4), 988–995. https://doi.org/10.1109/TBME.2008.2009315.
- Vauhkonen, M., Kaipio, J.P., Somersalo, E., Karjalainen, P.A., 1997. Electrical impedance tomography with basis constraints. Inverse Problems 13 (2), 523–530. https://doi.org/10.1088/0266-5611/13/2/020.
- Vorwerk, J., Aydin, Ü., Wolters, C.H., Butson, C.R., 2019. Influence of Head Tissue Conductivity Uncertainties on EEG Dipole Reconstruction. Front. Neurosci. 13, 531. 258 https://doi.org/10.3389/fnins.2019.00531.
- Vorwerk, J., Cho, J.-H., Rampp, S., Hamer, H., Knösche, T.R., Wolters, C.H., 2014. A guideline for head volume conductor modeling in EEG and MEG. NeuroImage 100, 590–607. https://doi.org/10.1016/j.neuroimage.2014.06.040.
- Vorwerk, J., Oostenveld, R., Piastra, M.C., Magyari, L., Wolters, C.H., 2018. The FieldTrip-SimBio pipeline for EEG forward solutions. BioMedical Engineering OnLine 17 (1), 37. https://doi.org/10.1186/s12938-018-0463-y.
- Wendel, K., Väisänen, J., Seemann, G., Hyttinen, J., Malmivuo, J., 2010. The Influence of Age and Skull Conductivity on Surface and Subdermal Bipolar EEG Leads. Computational Intelligence and Neuroscience 2010 (2), 1–7. https://doi.org/10.1155/2010/397272.
- Wolters, C.H., Anwander, A., Berti, G., Hartmann, U., 2007. Geometry-adapted hexahedral meshes improve accuracy of finite-element-method-based EEG source analysis. IEEE Transactions on Biomedical Engineering 54 (8), 1446–1453. https://doi.org/10.1109/TBME.2007.890736.
- Wolters, C.H., Beckmann, R.F., Rienäcker, A., Buchner, H., 1999. Comparing regularized and non-regularized nonlinear dipole fit methods: A study in a simulated sulcus structure. Brain topography 12 (1), 3–18. https://doi.org/10.1023/a:1022281005608.
- Wolters, C.H., Grasedyck, L., Hackbusch, W., 2004. Efficient computation of lead field bases and influence matrix for the FEM-based EEG and MEG inverse problem. Inverse Problems 20 (4), 1099–1116. https://doi.org/10.1088/0266-5611/20/4/007.
- Wolters, C.H., Lew, S., MacLeod, R.S., Hämäläinen, M.S., 2010. Combined EEG/MEG source analysis using calibrated finite element head models. Biomedical Technology 55 (Suppl.1), 64–67.