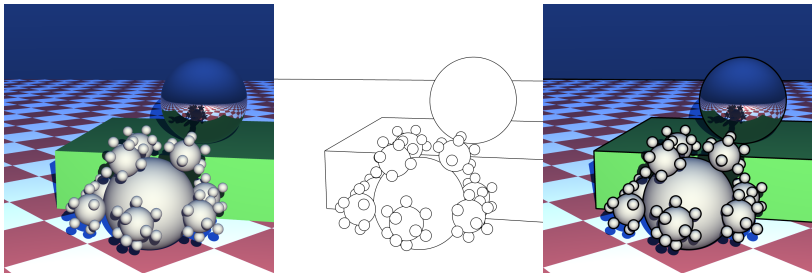


# Ray Tracing NPR-Style Feature Lines

A.N.M. Imroz Choudhury    Steven G. Parker

Scientific Computing and Imaging Institute  
University of Utah

August 1, 2009



# Why Ray Tracing?

- High-quality images (shadows, refraction/reflection, etc. are straightforward)
- Photorealism without hacks
- Interactive now, and still improving
- Easier to use than OpenGL (for some applications)
- On the rise

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It pays to see how NPR fits in ray tracing.

# Why Ray Tracing?

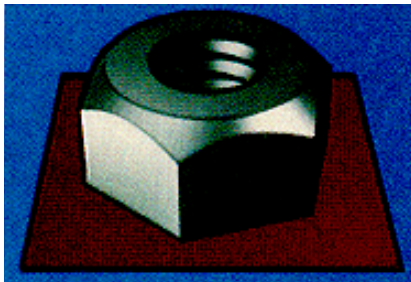
High-Quality Images



# Why Feature Lines?

Feature lines can

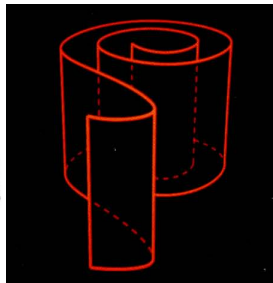
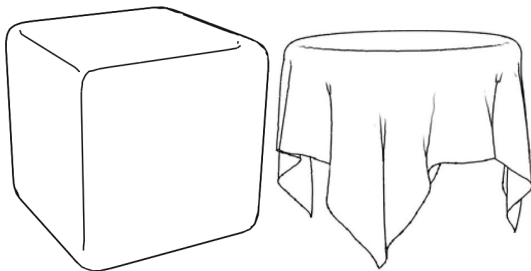
- enhance geometric features (Saito and Takahashi 1990)
- succinctly express shape (Judd et al. 2007, Dooley and Cohen 1990)
- indicate confidence in architectural rendering (Potter et al. 2009)



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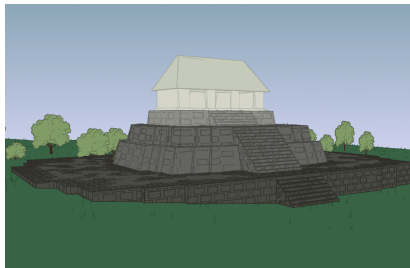
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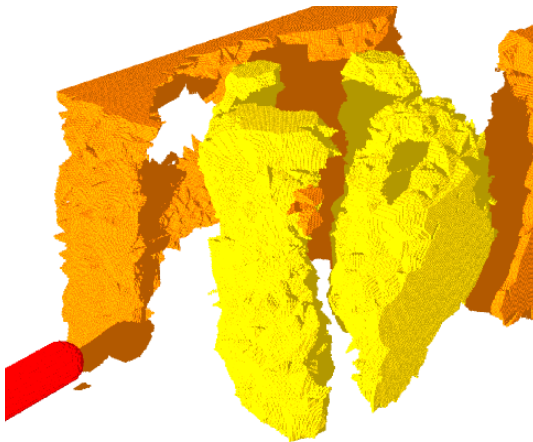
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# Driving Application—Scientific Visualization

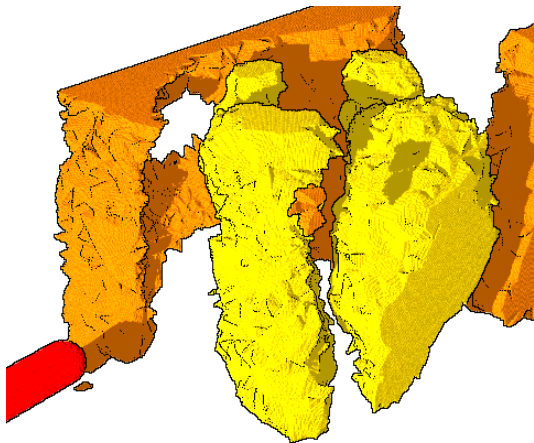
Silhouette edges can indicate particle groupings  
(Bigler et al. 2006).





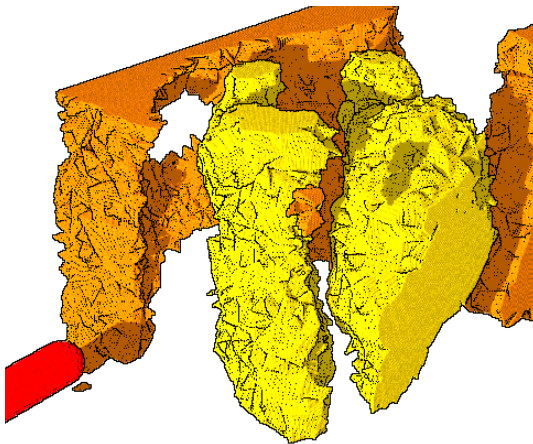
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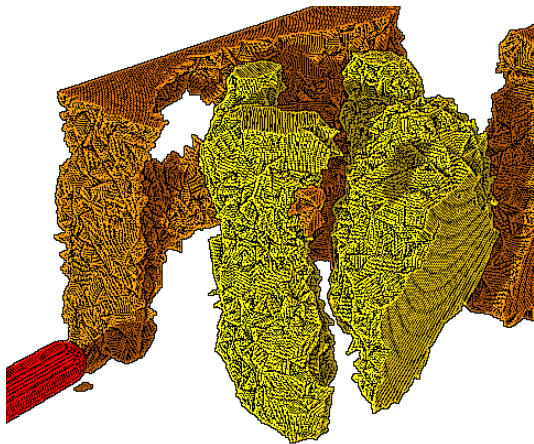
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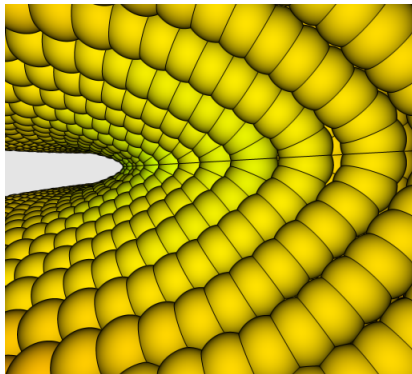
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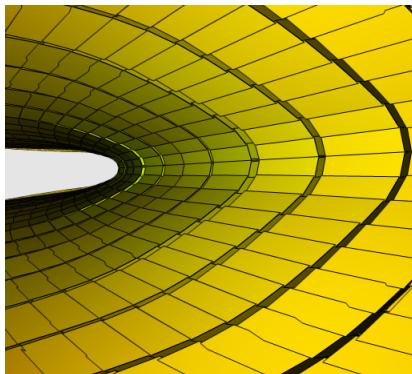
# Driving Application—Scientific Visualization

Generalize to *direct rendering* of feature lines from geometry itself  
(Choudhury et al.)



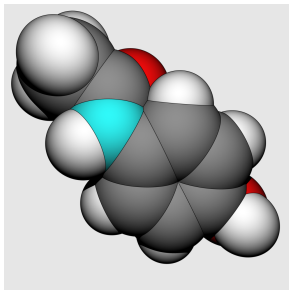
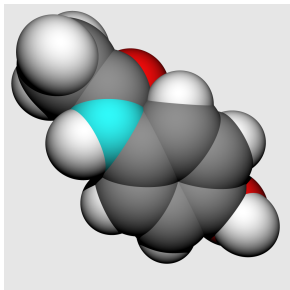
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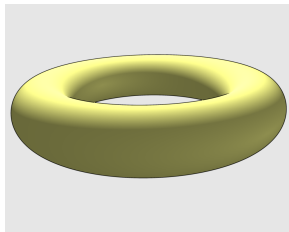
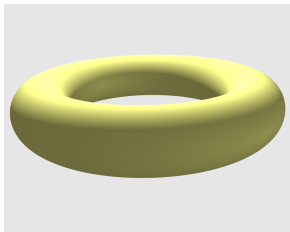
# Feature Line Types

- *Intersection lines*: two objects intersect and form a seam
- *Silhouette lines* (or *edges*): the edge of an object lies against the background, a different object, or a further part of itself (i.e. a *self-occluding* silhouette)
- *Crease lines*: an object has a sharp corner (a discontinuity in the gradient of the normal field)



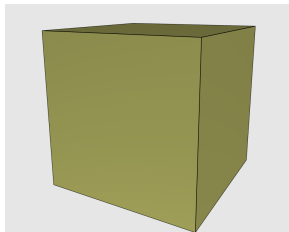
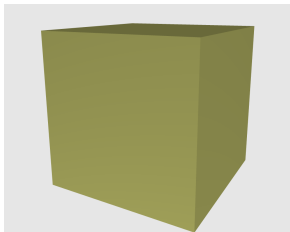
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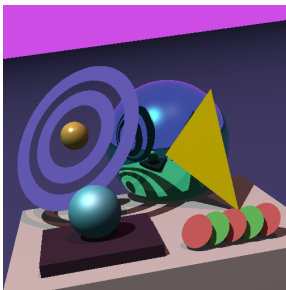
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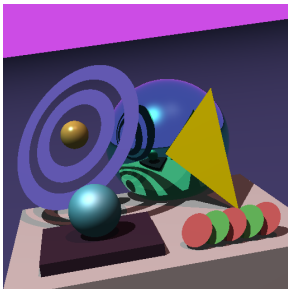
# Lines in Ray Tracing?

- Ray tracing deals in “physical” primitives: sphere, cone, torus, disc, triangle, etc.



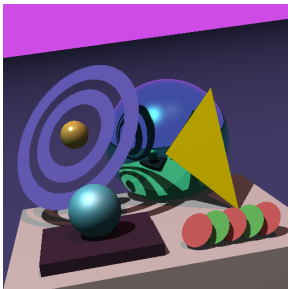
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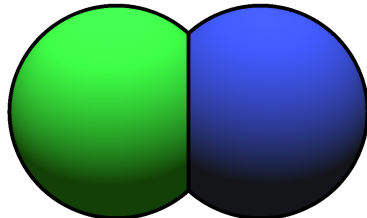
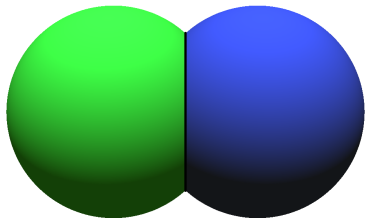
# Lines in Ray Tracing?

- Ray tracing deals in “physical” primitives: sphere, cone, torus, disc, triangle, etc.
- Lines are *not* physical—they have no breadth
- Can try “line-like” primitives, e.g. thin cylinders and toruses



# Lines in Ray Tracing?

*But geometry doesn't work as lines!*



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*But geometry doesn't work as lines!*



# Lines in Ray Tracing?

But *geometry* doesn't work as *lines*!



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We would like to

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- with **constant width** in screen space



# Lines in Ray Tracing?

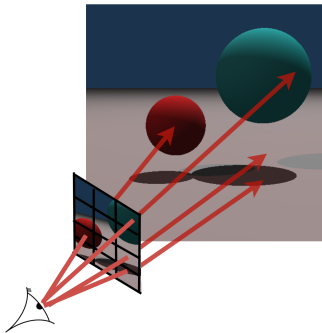
We would like to

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i.e. we want to **rasterize** lines

# Ray Tracing

## Algorithm Overview

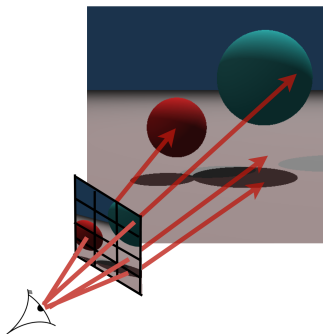


(Figure courtesy of Thiago Ize)

- *Camera rays* cast through the *image plane*, striking the scene at *intersection points*
- *Secondary rays* cast from the intersection points for secondary effects (shadows, reflections, etc.)
- *Sample colors* computed from ray results and *shading model*
- *Final image* assembled from filtered sample colors

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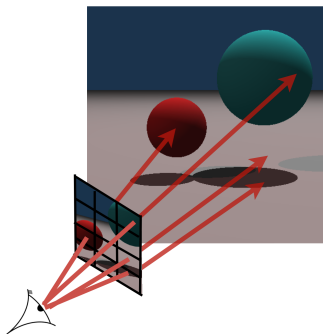


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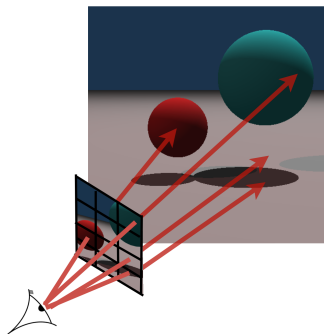


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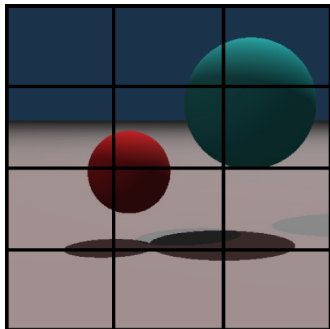


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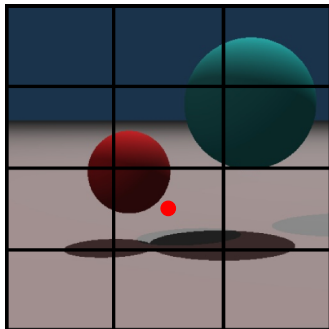
## Navigating Screen Space



- Camera rays determine visibility

# Ray Tracing

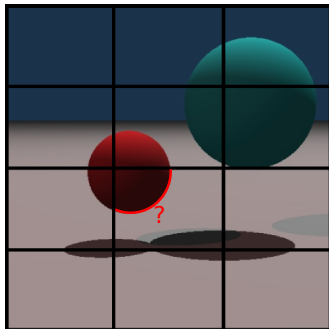
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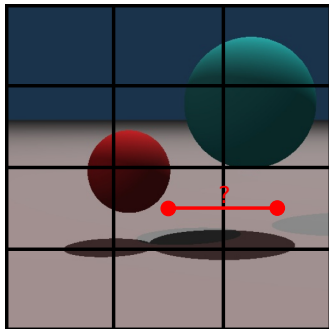


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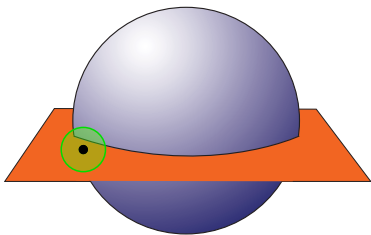
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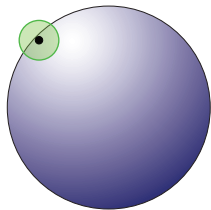
- Camera rays determine visibility
- Parameterized by camera position and **pixel position**; i.e., they live in screen space
- With a way to
  - 1 **detect feature lines**, and
  - 2 **measure distances** in screen space

we can incorporate feature line rendering into a ray tracer.

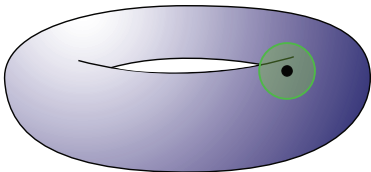
# Detecting Feature Lines



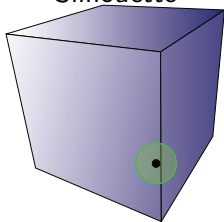
Intersection



Silhouette



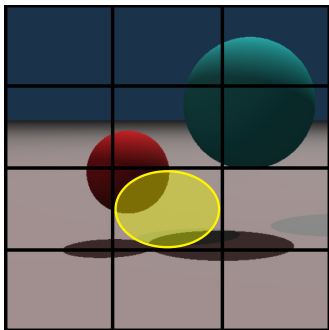
Self-occluding silhouette



Crease

# Measuring Distances

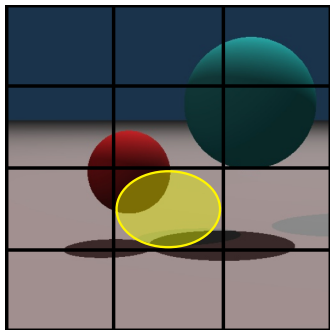
Cone Tracing (Amanatides 1984)



- Trace a *cone* instead of a ray; footprint is circle instead of point

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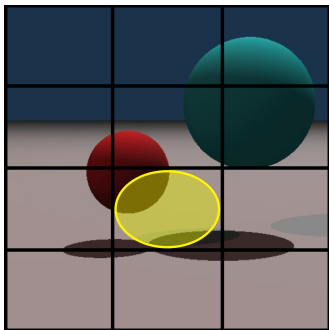
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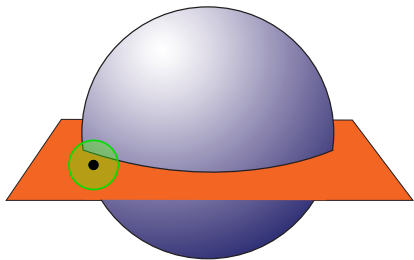
Cone Tracing (Amanatides 1984)



- Trace a *cone* instead of a ray; footprint is circle instead of point
- Used for non-singular scene coverage: anti-aliasing, glossy reflections, etc.
- We borrow the idea of a ray having a **radius**; our notion of non-physical feature lines exists over **some area** of the image.

# Drawing Feature Lines

## Continuous Case



- Estimate *foreign geometry area (FGA)*

# Drawing Feature Lines

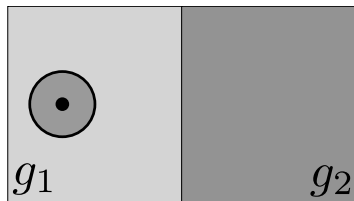
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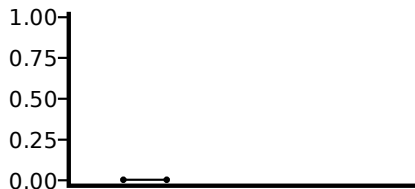
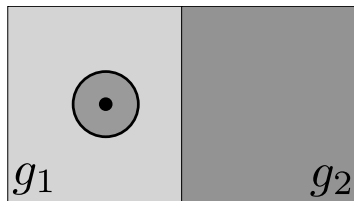


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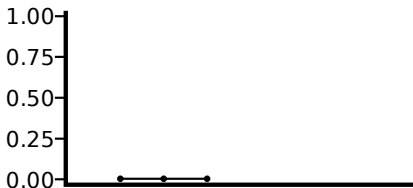
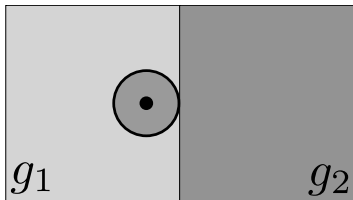
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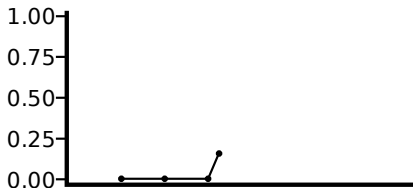
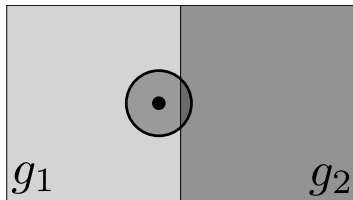
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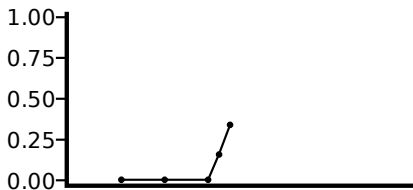
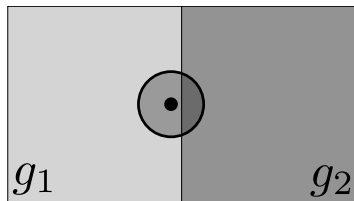
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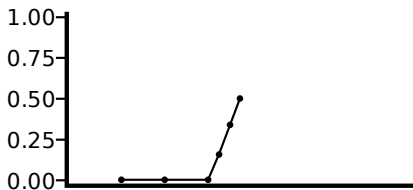
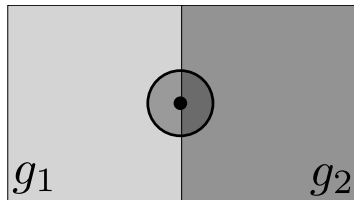
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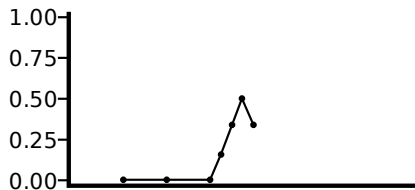
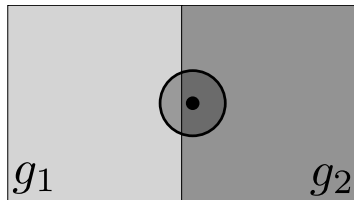
## Continuous Case



- Estimate *foreign geometry area (FGA)*
- Intuition: edge must be strong where *FGA* is 50%

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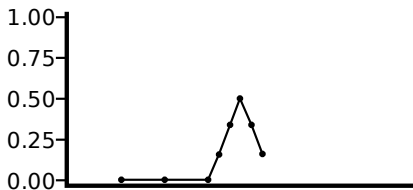
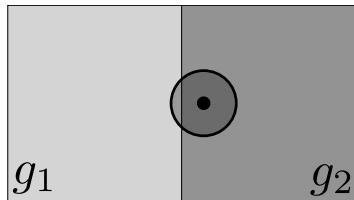
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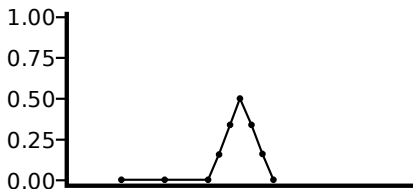
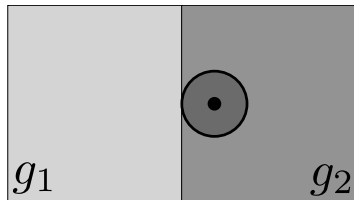
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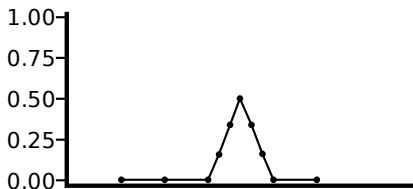
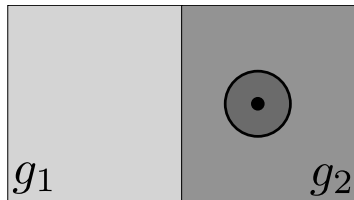


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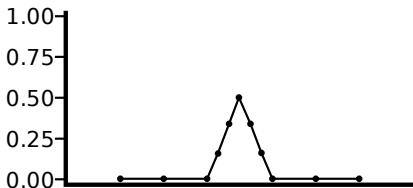
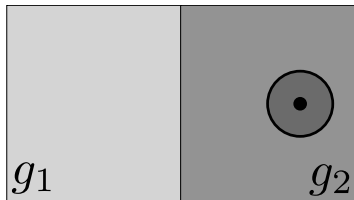
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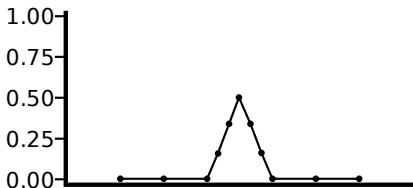
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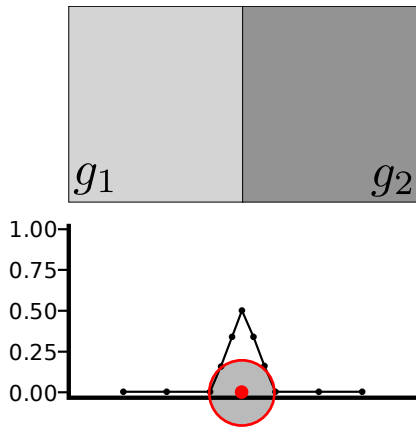
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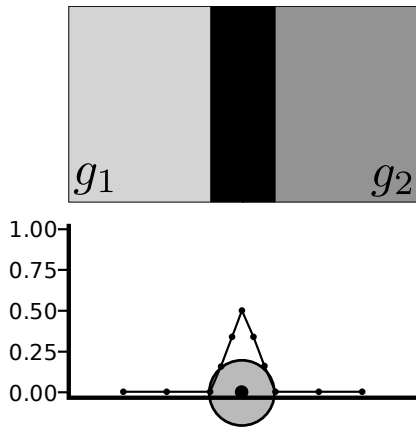
## Continuous Case



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- Note: filter diameter equals width of peak

# Drawing Feature Lines

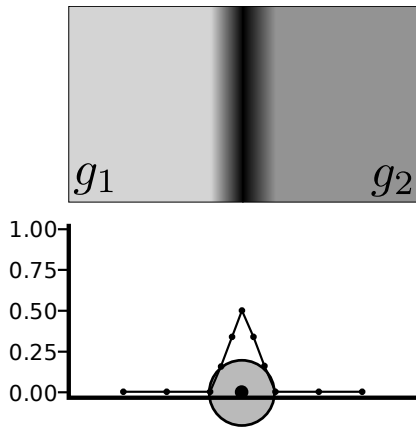
## Continuous Case



- Estimate *foreign geometry area (FGA)*
- Intuition: edge must be strong where  $FGA$  is 50%
- Note: filter diameter equals width of peak
- Easiest way to create a line: black where  $FGA > 0$ ; sample color where  $FGA = 0$

# Drawing Feature Lines

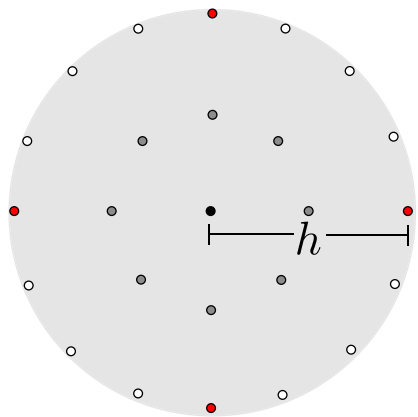
## Continuous Case



- Estimate *foreign geometry area (FGA)*
- Intuition: edge must be strong where  $FGA$  is 50%
- Note: filter diameter equals width of peak
- Easiest way to create a line: black where  $FGA > 0$ ; sample color where  $FGA = 0$
- More generally: determine darkness of line as a *function of FGA*; i.e. use an *edge strength metric*

# Drawing Feature Lines

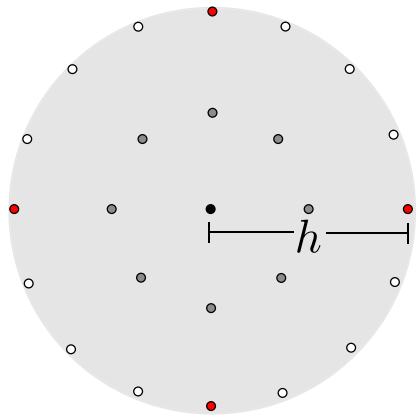
## Discretizing to Ray Stencils



- Approximate filter by sampling the disc
- $h$  is a distance in *screen space*
- Increase sampling density by packing more rings of samples
- Estimate *FGA* by *counting* which rays hit what
- Red samples form *finite difference stencil* for computing creases

# Drawing Feature Lines

## Discretizing to Ray Stencils

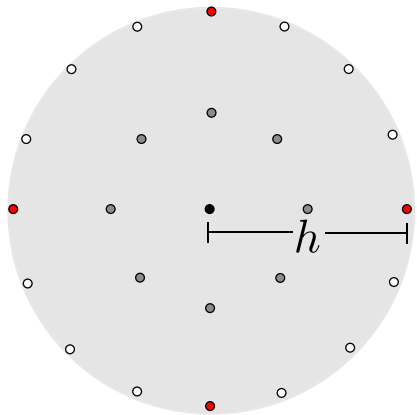


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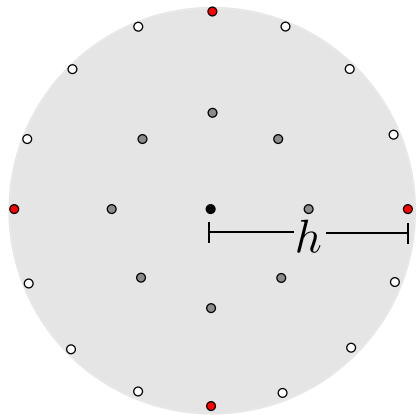
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# Drawing Feature Lines

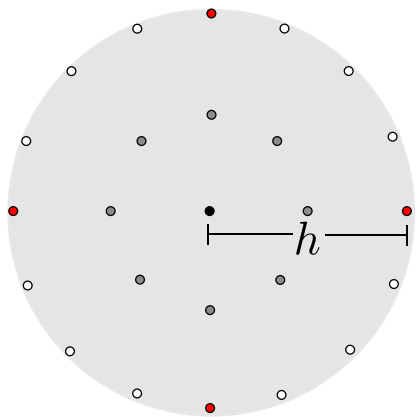
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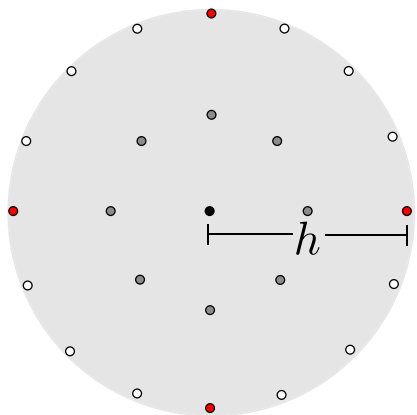
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# Drawing Feature Lines

## Computing Edge Strength

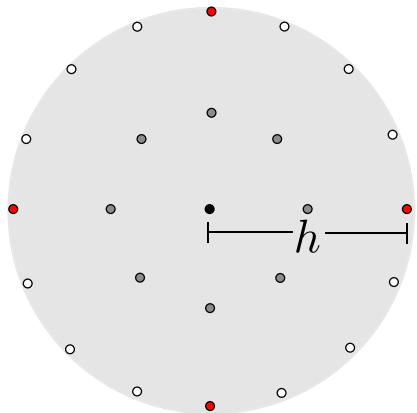


sample ray  $s$  (black), striking object  $g_s$ , surrounded by  $M$  stencil rays (gray, white, red)

- Select *edge strength metric*  $E$  (e.g.  $E(m) = \frac{m}{\frac{1}{2}M}$ )
- if *entire stencil* hits object  $g_s$ ,
  - 1 compute  $\nabla \vec{n}$ ; if above threshold, edge strength  $e_s = 1$ , otherwise,
  - 2  $d$  is the number of stencil rays “far” from the sample ray:  $e_s = E(d)$
- otherwise, set  $e_s = E(m)$ , where  $m$  is the number of rays *not* striking  $g_s$

# Drawing Feature Lines

## Computing Edge Strength

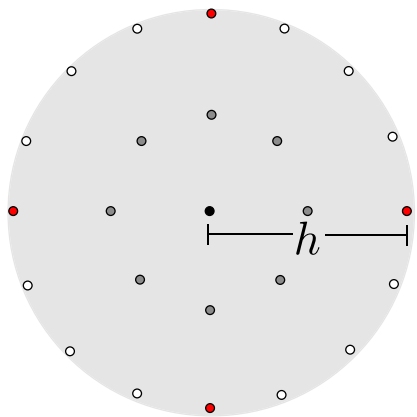


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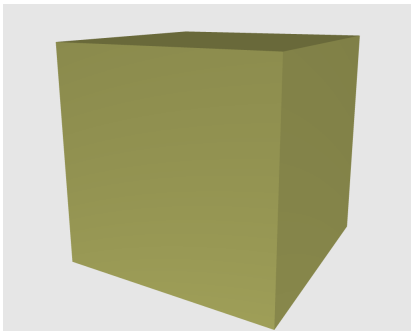
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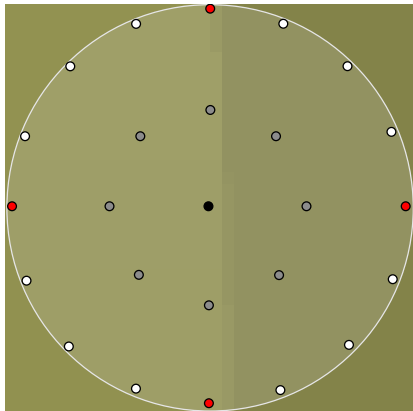
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## Computing Edge Strength

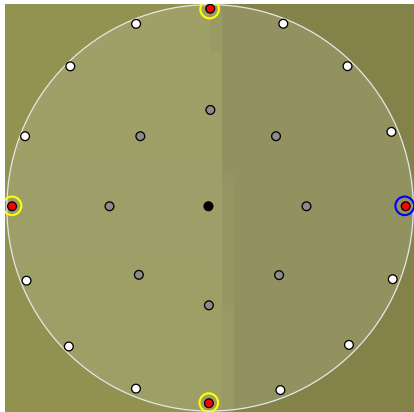


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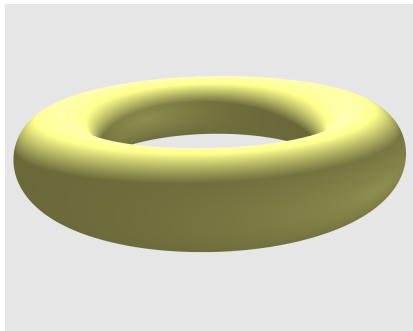
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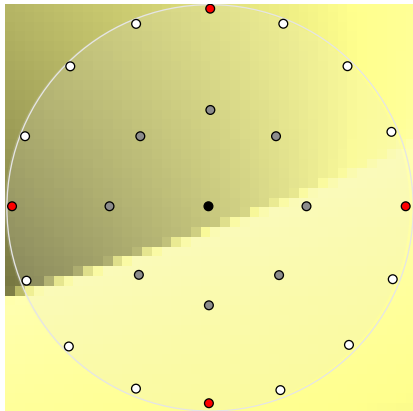
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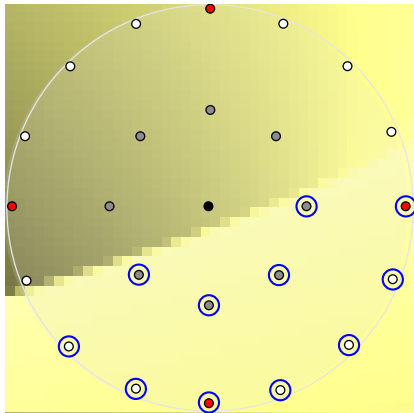
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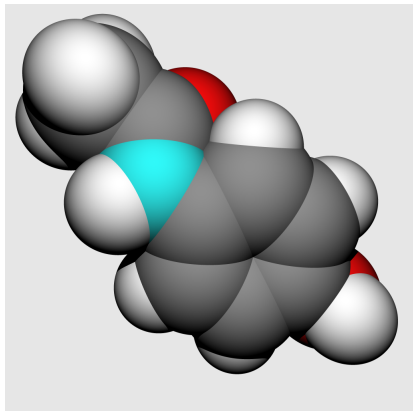
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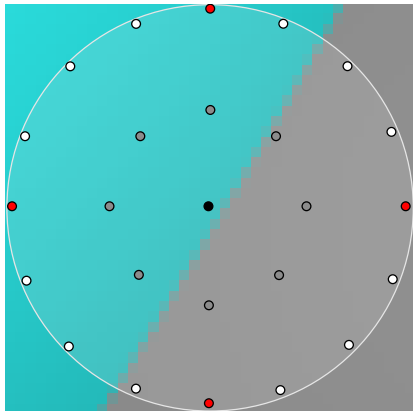
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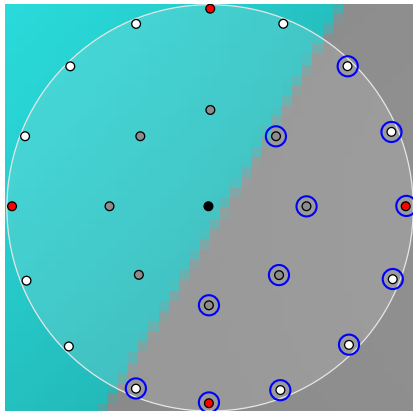
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# Drawing Feature Lines

## Computing Edge Strength

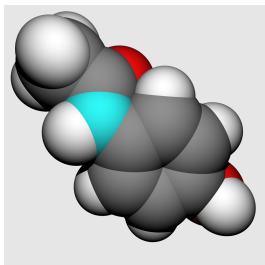


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# Ray Tracing Feature Lines

For each sample:

- Compute and shade *sample ray*

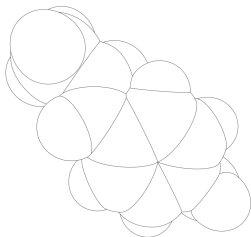
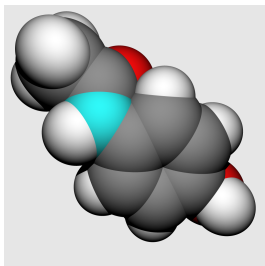




# Ray Tracing Feature Lines

For each sample:

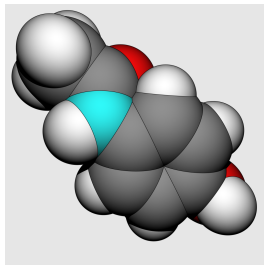
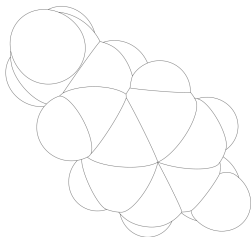
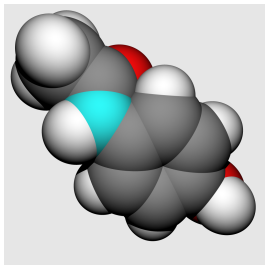
- Compute and shade *sample ray*
- Compute *edge strength*



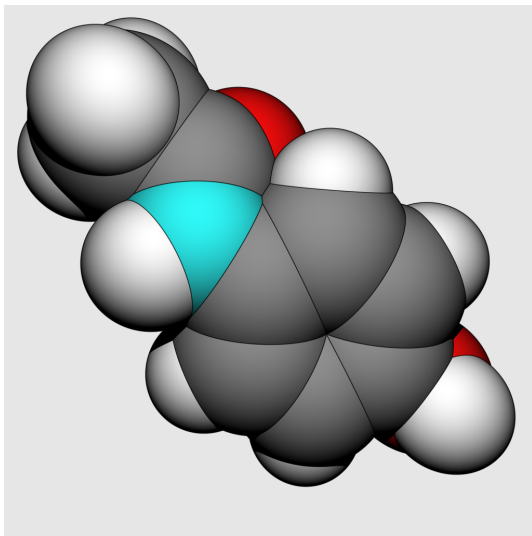
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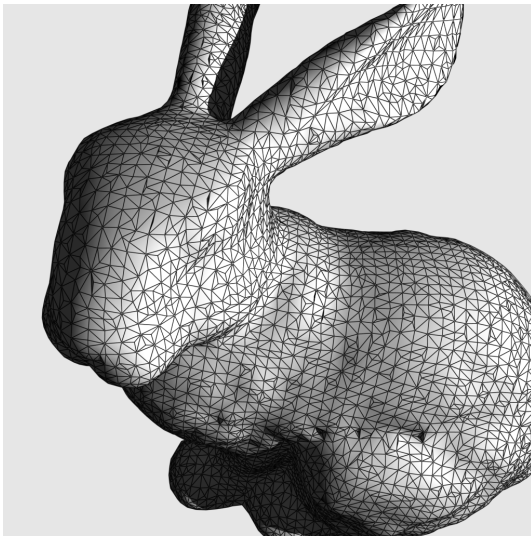
- Compute and shade *sample ray*
- Compute *edge strength*
- *Darken* shaded sample color according to edge strength  
( $e_s = 0$  results in sample color itself,  $e_s = 1$  results in black)



# Primitive Joints

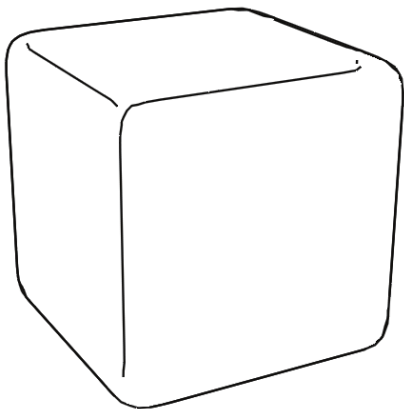


# Mesh Visualization



# Application to NPR Techniques

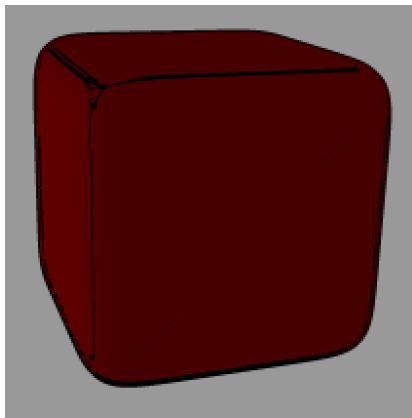
Apparent Ridges (Judd et al. 2007)



- *Apparent ridges*: lines along which the view-dependent curvature attains a local maximum
- Followed algorithm in paper, adapting to ray stencils framework
- Reproduced “hooks” on corners
- Very faint ridge on front face, corresponding to slight bulge in model

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**Thank You!**



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