

Snakes: Active Contour Models

CS 6640

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(some material from Zoltan Kato <http://www.cab.u-szeged.hu/~kato/variational/>)

Materials

- Kass, Witkin, Terzopoulos, Int. Journal of Computer Vision, 321-331, 1988
- Trucco and Verri, Introductory Techniques for 3-D Computer Vision, Chapter 5
- Bryan Morse, Lecture 21 Image Understanding

Websites

- Andy Witkin's homepage:
<http://www.cs.cmu.edu/~aw/>
- Terzopoulos: <http://www.cs.ucla.edu/~dt/vision.html>
→ Snakes: Active Contour Models
- Original snake demo: Kass, Witkin, Terzopoulos
1988: <http://www.cs.ucla.edu/~dt/videos/deformable-models/snakes.avi>
- Other Demos:
 - Xu/Prince: <http://www.iacl.ece.jhu.edu/static/gvf/>
 - http://users.ecs.soton.ac.uk/msn/book/new_demo/
 - <http://www.markschulze.net/snakes/index.html>

Snake's Energy Function

- Position of the snake $v(s) = (x(s), y(s))$
- $E_{\text{snake}} = \int [E_{\text{int}} v(s) + E_{\text{image}} v(s) + E_{\text{con}} v(s)] ds$
 - Internal: Internal energy due to bending. Serves to impose piecewise smoothness constraint
 - Image: Image forces pushing the snake toward image features (edges, etc...)
 - Constraints: External constraints are responsible for putting the snake near the desired local minimum

Internal Energy

- $E_{\text{int}} = [\alpha(s) |v_s(s)|^2 + \beta(s) |v_{ss}(s)|^2]$
 - First order term: membrane, $\alpha(s)$: “elasticity”
 - Second order term: thin plate, $\beta(s)$: “rigidity, stiffness”
 - If $\alpha(s)=\beta(s)=0$, we allow breaks in the contour

Image Forces

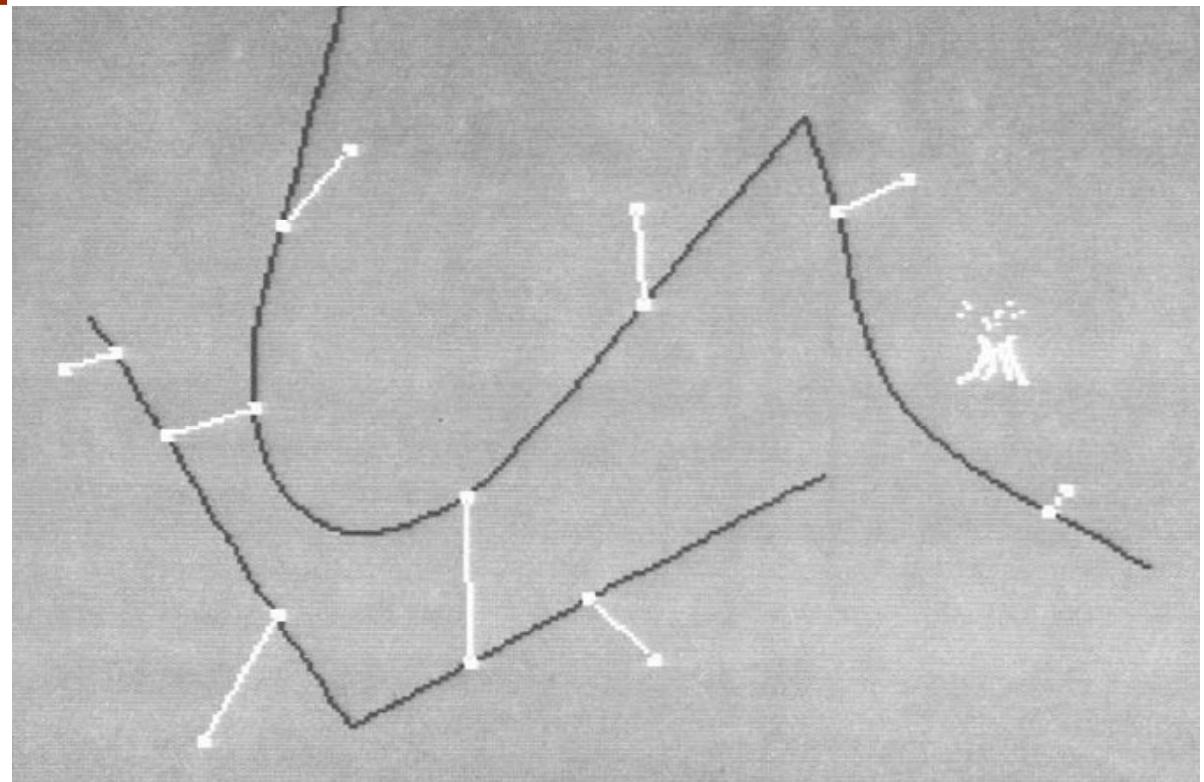
- Edge Functional : negative gradient magnitude: $E_{\text{edge}} = - |\nabla I(x,y)|^2$
- Better: negative gradient magnitude of Gaussian-smoothed image:

$$E_{\text{edge}} = - |\nabla G(\sigma) \otimes I(x,y)|^2$$

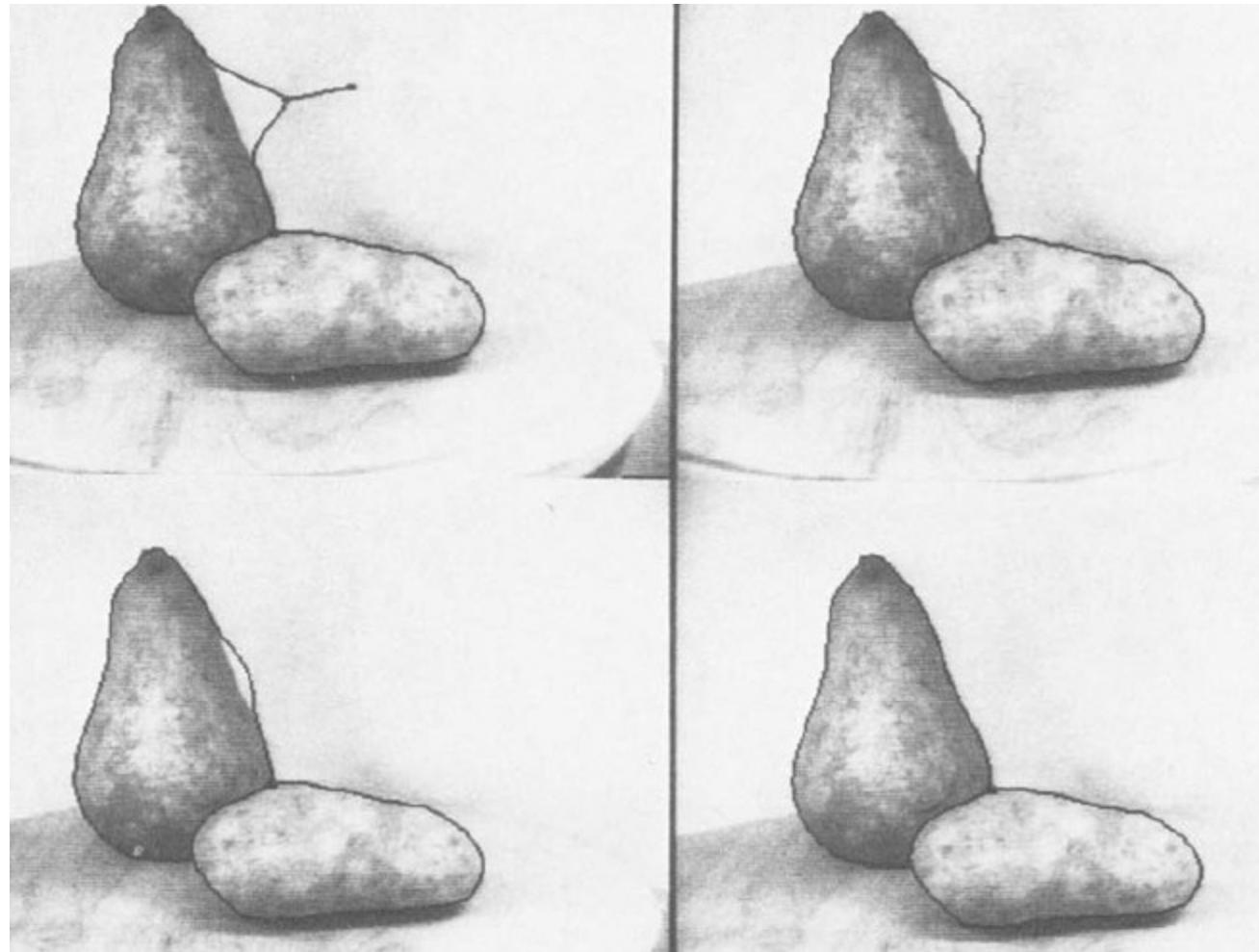
→ Attracts the snake to locations of large gradients = strong edges

External Constraint Forces

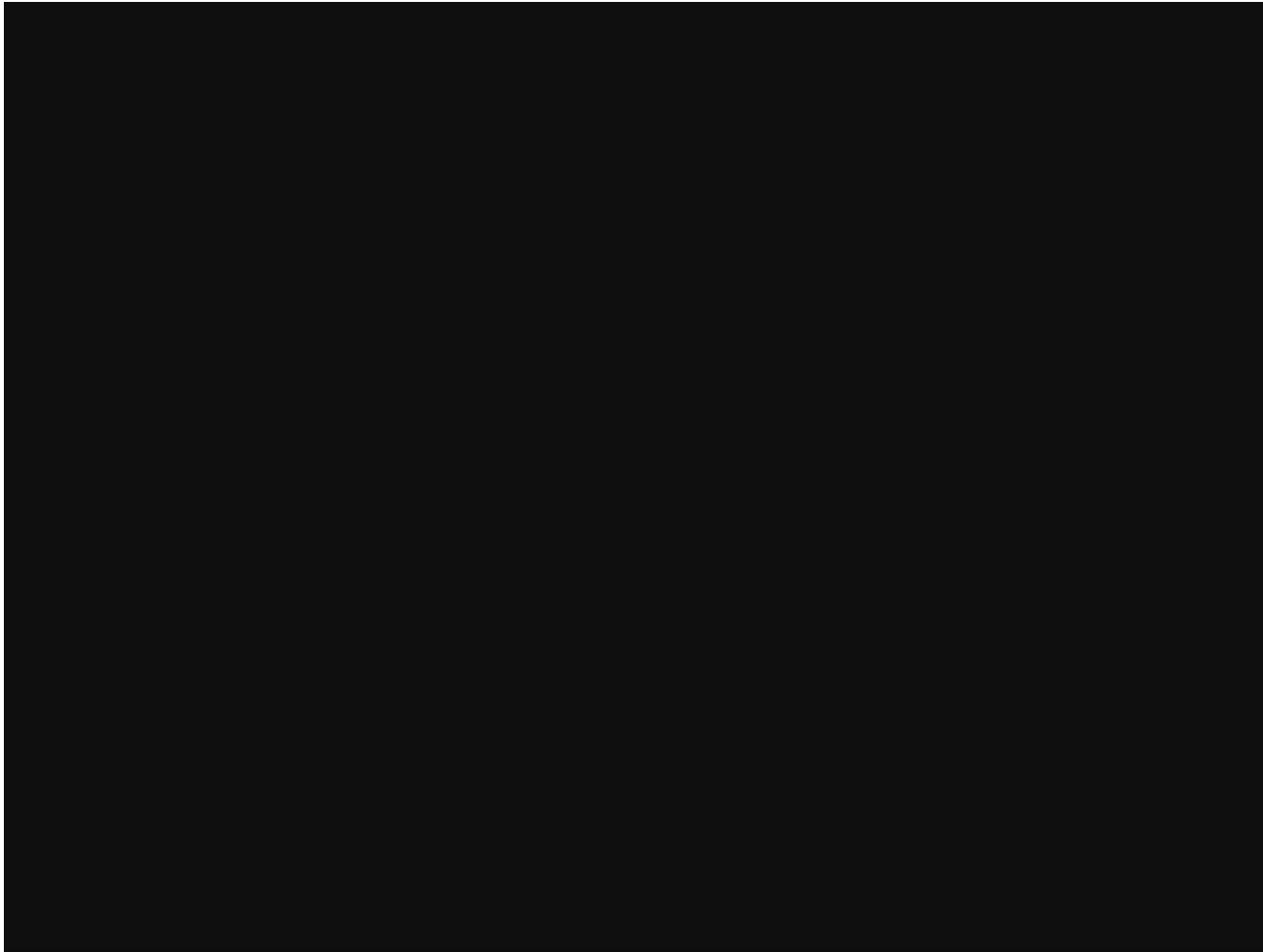
- Springs: add $-k(x_1-x_2)^2$ to E_{con}
- Volcano: $1/r^2$ repulsion force, combine with image potential



External Constraint Forces: Spring



Original Demo Kass et al., 1988



Click to
run

<http://www.cs.ucla.edu/~dt/videos/deformable-models/snakes.avi>

Numerical Solutions

$$-\frac{d^2}{ds^2} \left(\frac{\partial E}{\partial \left(\frac{d^2 x}{ds^2} \right)} + \frac{\partial E}{\partial \left(\frac{d^2 y}{ds^2} \right)} \right) + \frac{d}{ds} E_{v_s} - E_v = 0$$

Numerical Solutions

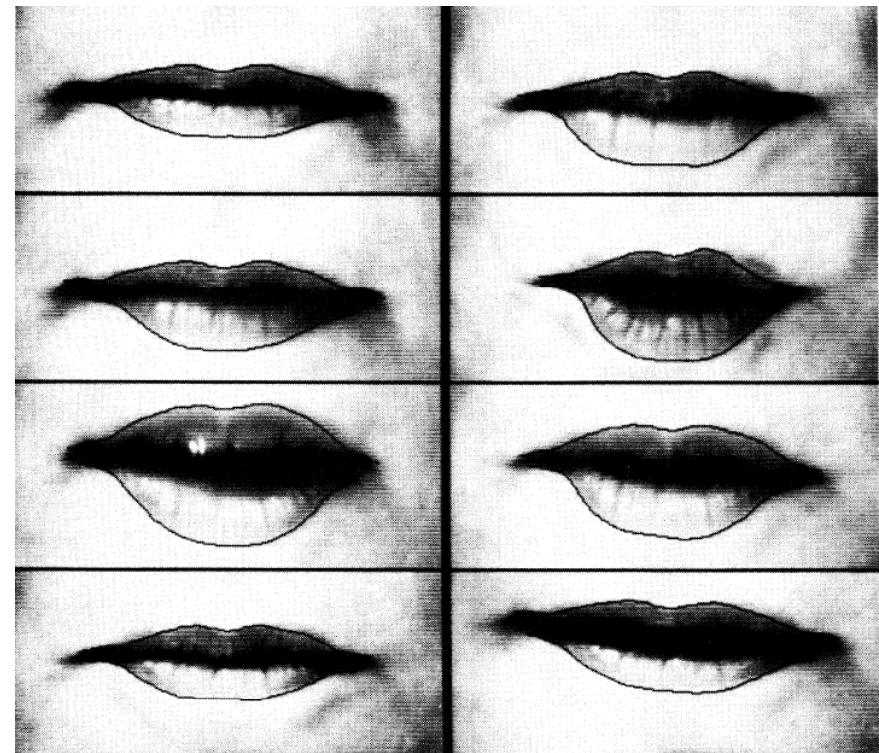
- The spline $v(s)$ which minimizes E^*_{snake} must satisfy

$$-\frac{d^2}{ds^2} \left(\frac{\partial E}{\partial \left(\frac{d^2 x}{ds^2} \right)} + \frac{\partial E}{\partial \left(\frac{d^2 y}{ds^2} \right)} \right) + \frac{d}{ds} E_{v_s} - E_v = 0$$

- Solutions: Greedy local updates, Euler Lagrange etc. (see handouts)

Using Snakes for Dynamic Scenes

- Once a snake finds a feature, it „locks on”
- If feature begins to move, the snake will track the same local minimum
- Fast motion could cause the snake to flip into a different minimum



Example Movie Sequences

