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# Introduction Image Analysis & Computer Vision

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Guido Gerig  
CS/BIOEN 6640 FALL 2010  
August 23, 2010

# Courses and Seminars related to Research in Image Analysis

NEW in 2010: SoC Image Analysis Track (Director Tom Fletcher) ([click](#))

Fall 2010:

- Image Processing CS 6640/ BIOEN 6640

Spring 2011:

- 3D Computer Vision CS 6320
- Advanced Image Processing CS 6640
- Mathematics of Imaging BIOEN 6500

Fall 2011:

- Image Processing Basics CS 4961
- Image Processing CS 6640

On demand:

- Special Topics Courses: Non-Euclidean Geometry, Non-Param. Stats, ..

Seminars:

- Seminar Imaging "ImageLunch" CS 7938: weekly  
Mondays 12 to 1.15, WEB 3670

# CS/BIOEN 6640 F2010

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For class:

- 1) Go to the web-site  
page: <http://www.sci.utah.edu/~gerig/CS6640-F2010/CS6640-F2010.html>
- 2) Look over the instructions and syllabus
- 3) Follow the link to "mailing lists" and join the cs6640 mailing lists as in the instructions. Remind them to use a mail address that they actually read (COMING SOON)
- 4) Look at the final and midterm exam dates and mark those on your calendar
- 5) Purchase the book
- 6) Do the first 2 reading assignments.

# CS/BIOEN 6640 F2010

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For class:

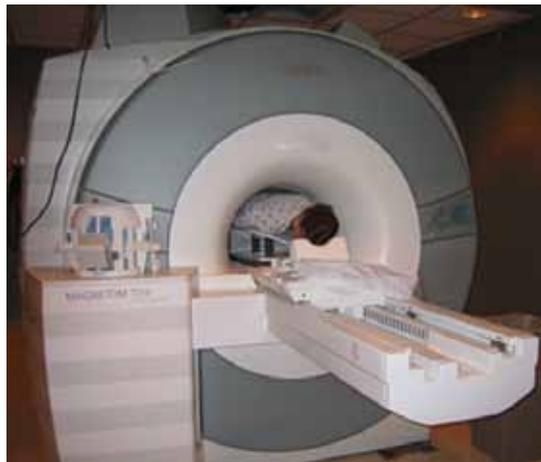
- We will use the uxxxxxxx email address for communication, please forward the u-email to your personal email if you use another account.
- The web-site provides downloads for additional materials and handouts.
- The syllabus is not completely rigid and fixed, and some topics will develop as the class continues.
- We will primarily use MATLAB (no extensions and additional libraries) for the projects. You can use CADE lab licenses or purchase a personal student license. C++ is an option (see web-page).
- Etc.

# Goals

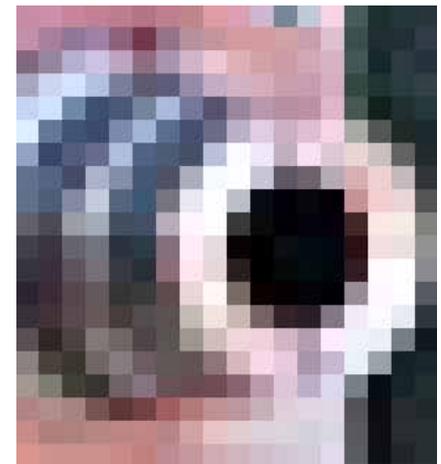
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- to tell you what you can do with digital images
- to show you that doing research in computer vision and image analysis is fun and exciting
- to demonstrate that image processing is based on strong mathematical principles, applied to digital images via numerical schemes
- to show you that you can solve typical image processing tasks on your own

# Image Sensors



# Digital Image



# Digital Image

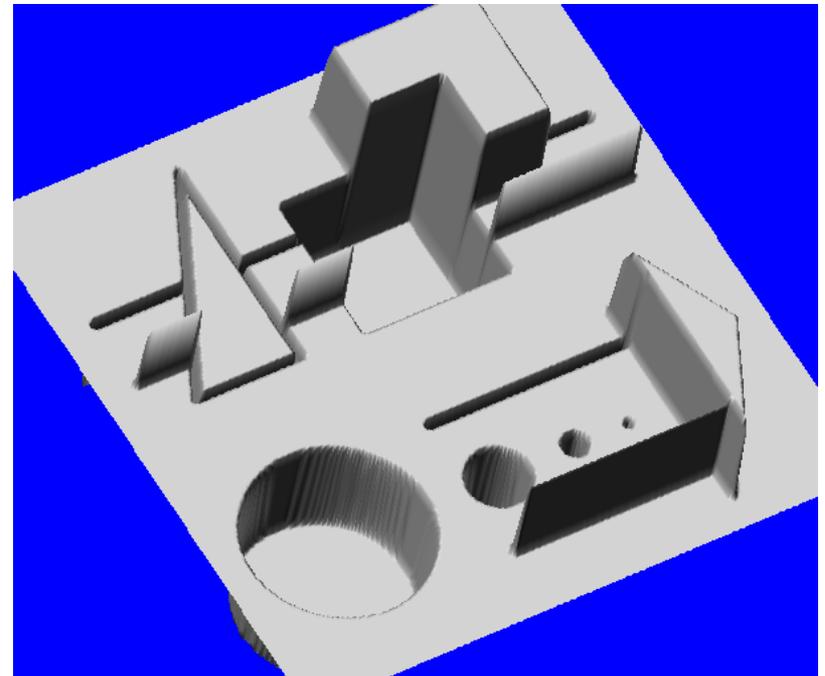
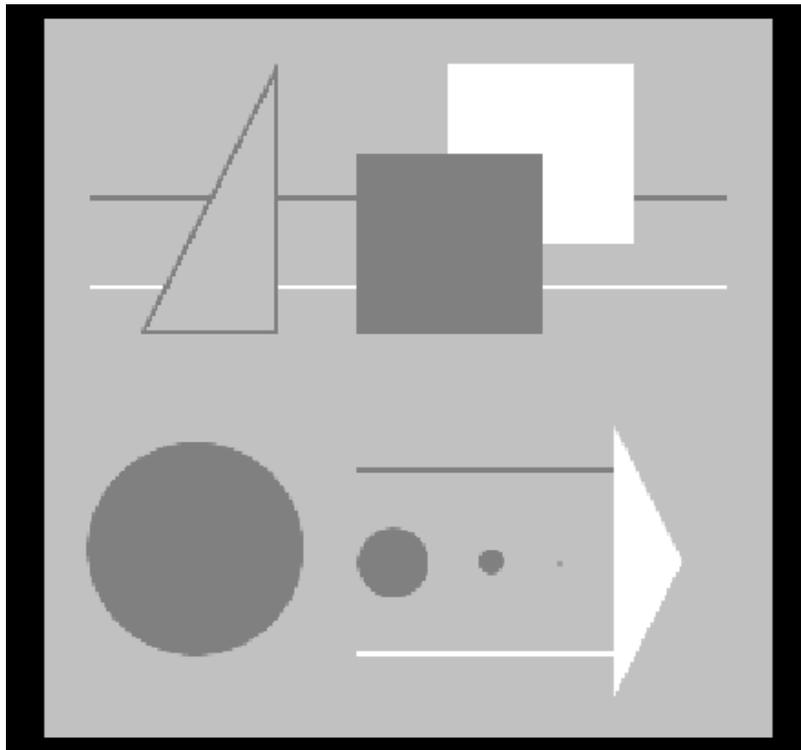


Each cell has number, either a scalar (black and white) or a vector (color).

Discrete representation of continuous world (sampling with aperture).

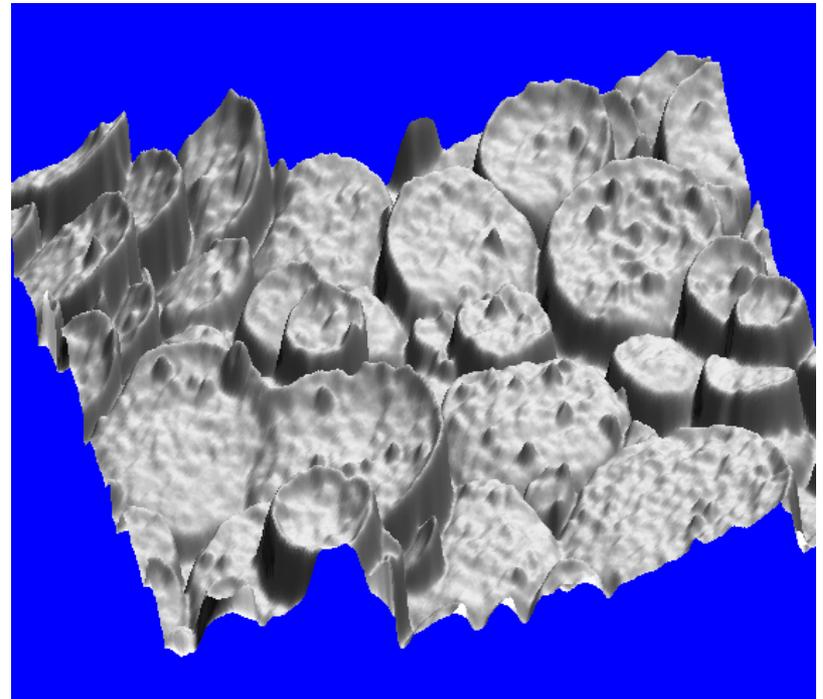
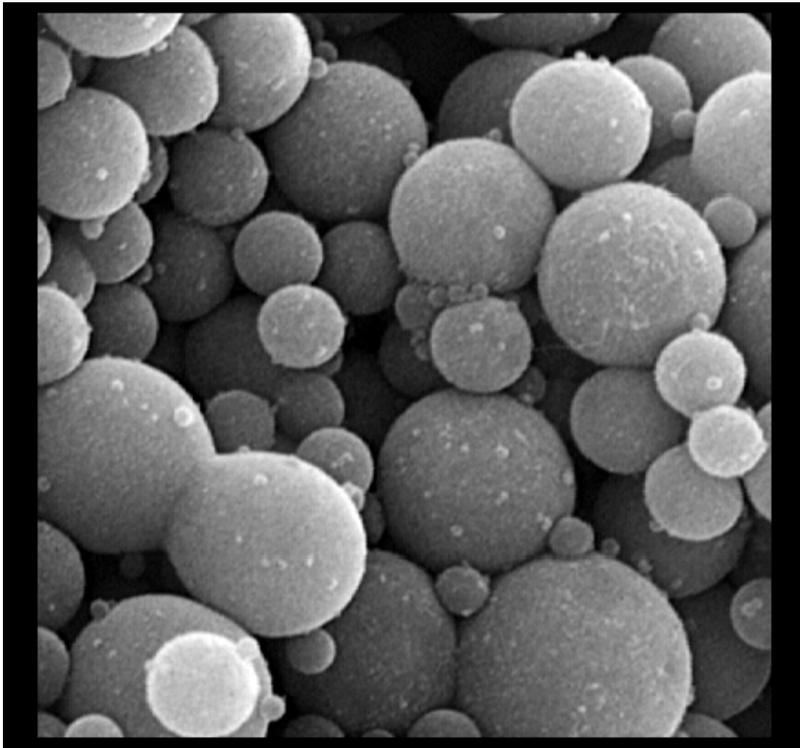
# Digital Images

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# Digital Images

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# Edges: Sudden change of intensity $L$

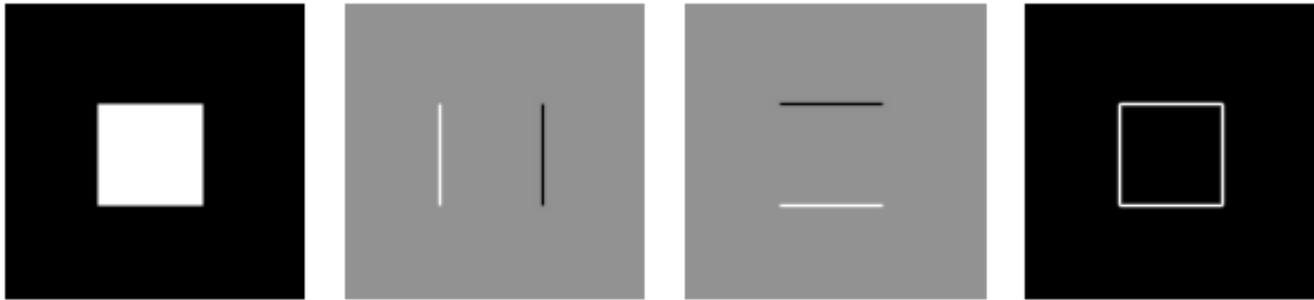
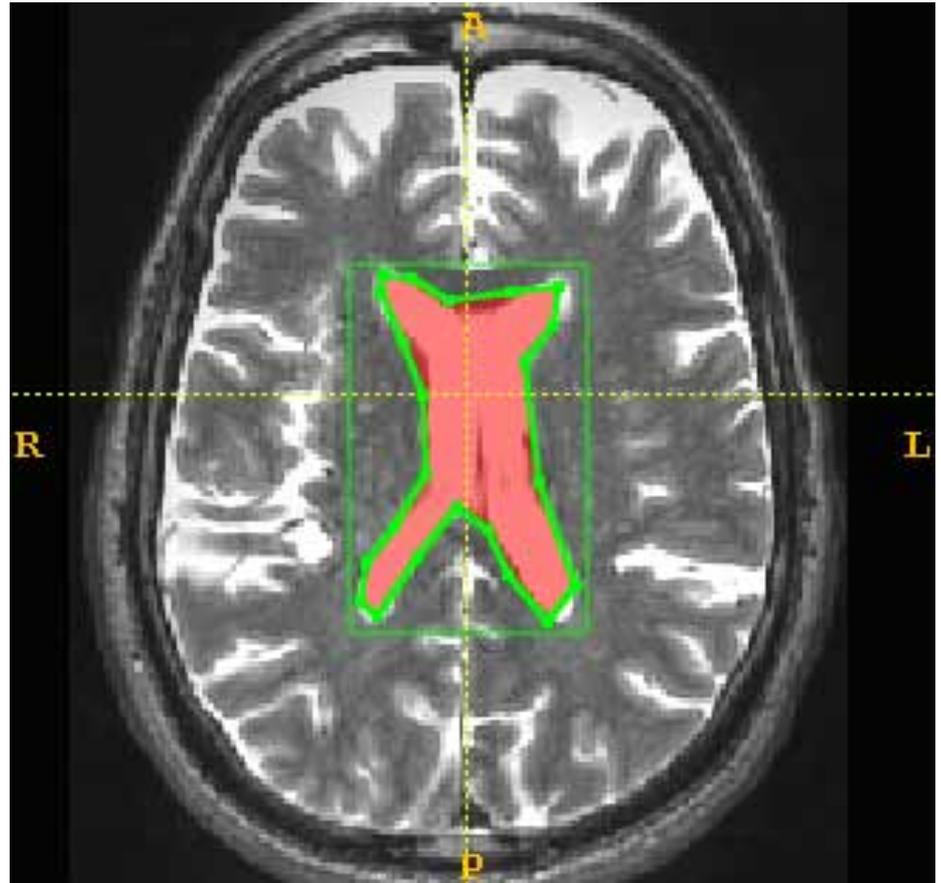


Figure 2.11 The first order derivative of an image gives edges. Left: original test image  $L(x, y)$ , resolution  $256^2$ . Second: the derivative with respect to  $x$ :  $\frac{\partial L}{\partial x}$  at scale  $\sigma = 1$  pixel. Note the positive and negative edges. Third: the derivative with respect to  $y$ :  $\frac{\partial L}{\partial y}$  at scale

# Segmentation of structures

- User painting/drawing on 2D images (“photoshop”)
- Tedious, time consuming, limited precision
- **Demonstrate Tool**



# Deformable Models: SNAKES

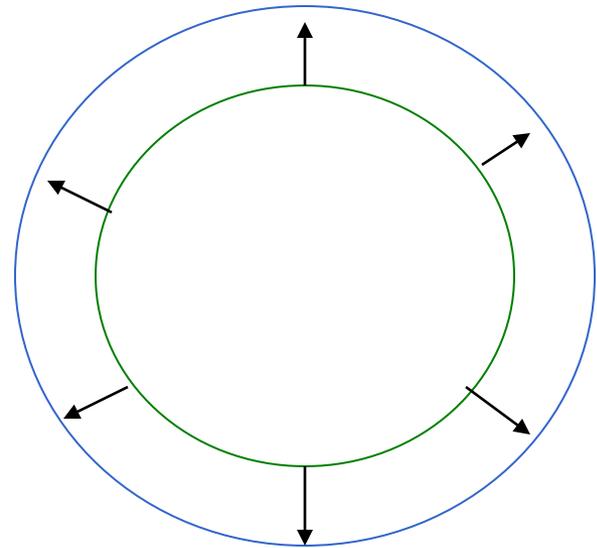
Geodesic Snake  
formulated as PDE

$$\frac{\partial c(x, t)}{\partial t} = [a] N^{\otimes 2}$$

Curve evolves  
over time

Speed

Normal direction  
to curve



# Deformable Models: SNAKES

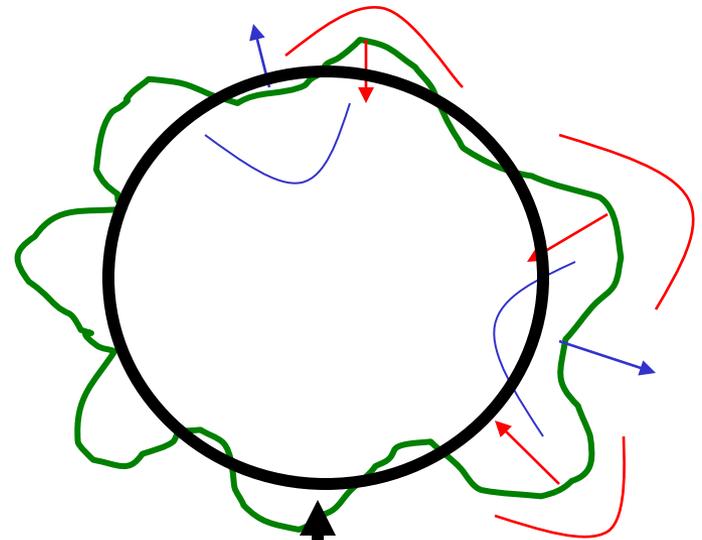
Geodesic Snake:

$$\frac{\mathcal{E}c(x, t)}{\mathcal{E}t} = [k]^\circledast N$$

Curve evolves  
over time

Curvature (convex,  
concave)

Normal direction  
to curve



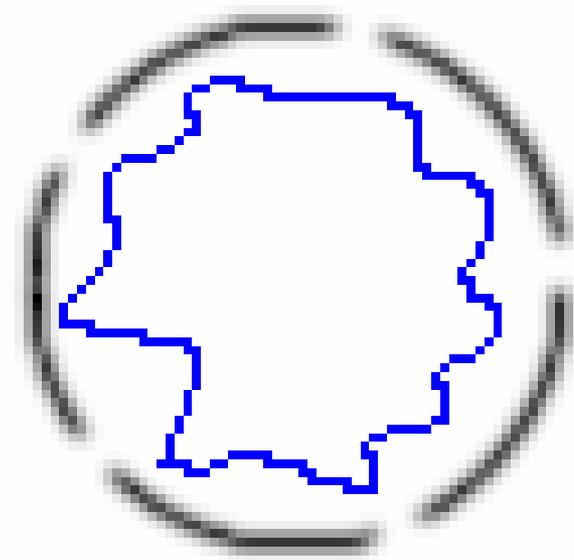
Mathematical  
solution is circle

# Deformable Models: SNAKES

Geodesic Snake:

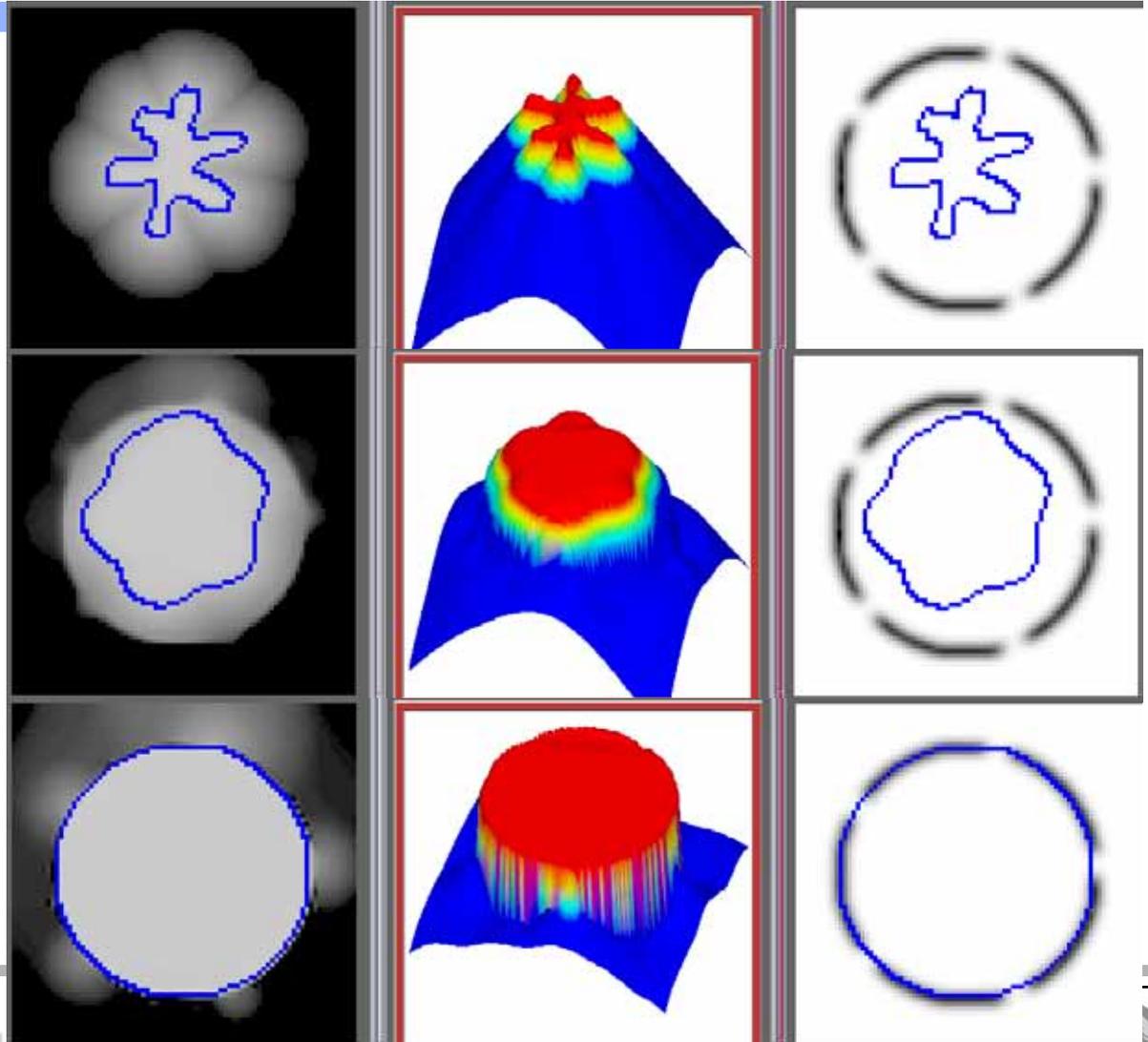
$$\frac{\partial c}{\partial t} = [k + a]N$$

Plus: add a term that stops at boundaries



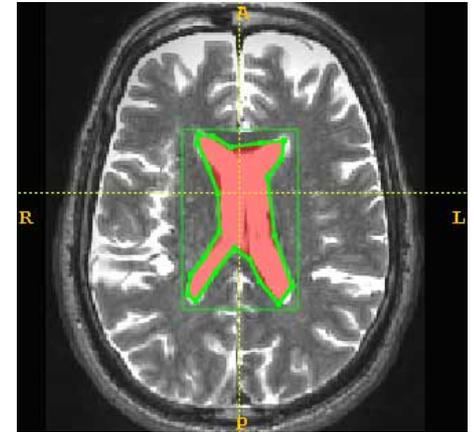
# Concept of level-set evolution

Implementation:  
Curve  $C$   
embedded as  
zero-level of  
higher order  
function  $j$

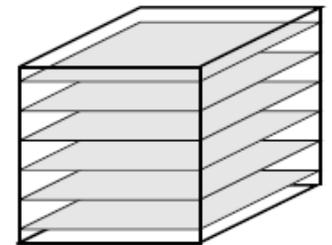
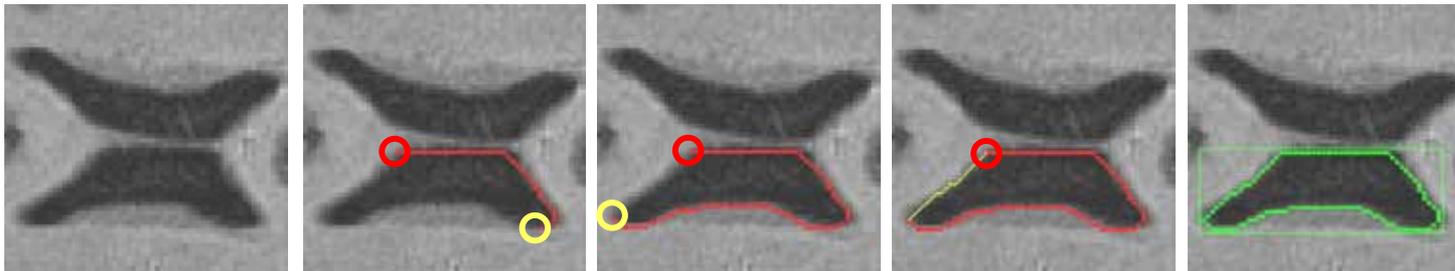


# Segmentation tool

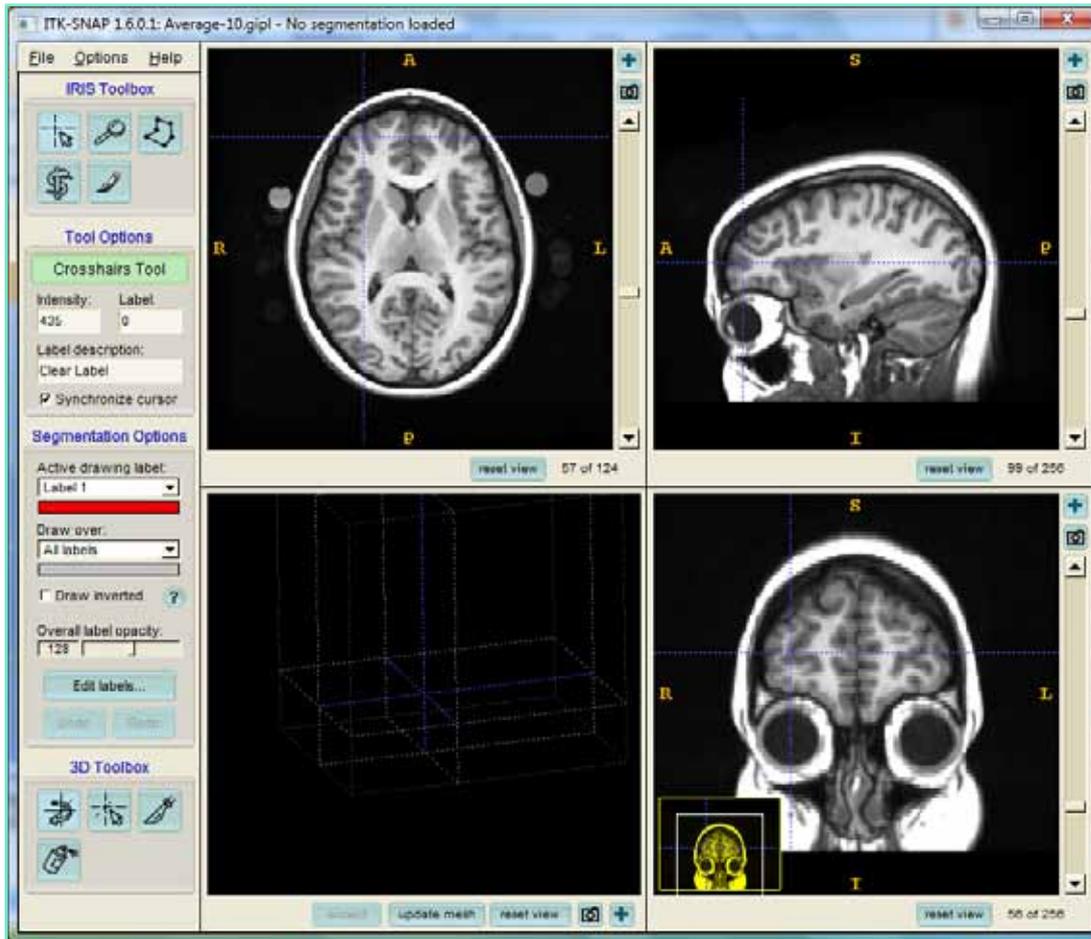
- User painting slice by slice (“photoshop”)
- Tedious, time consuming, limited reproducibility
- Painting in 2D intuitive, but what about 3D?



So far: Slice-by-slice contouring



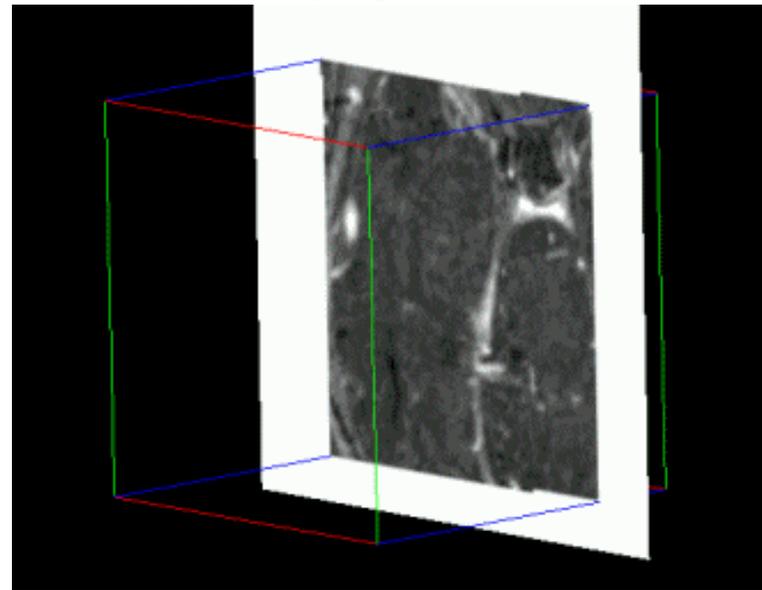
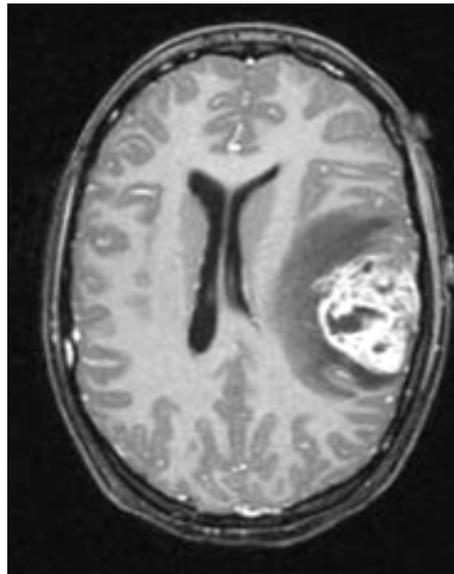
# Demo itkSNAP tool



# 3D Geodesic Snake

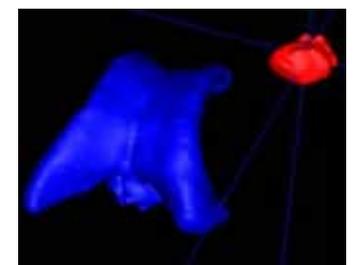
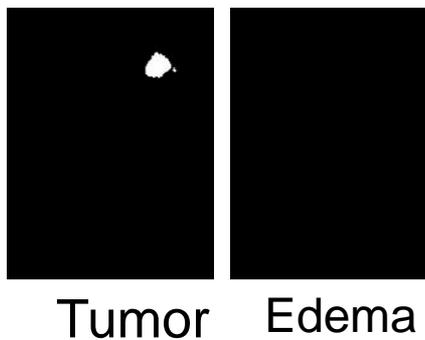
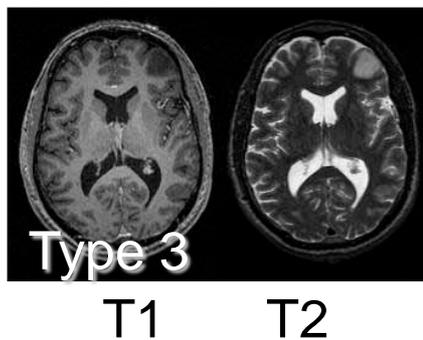
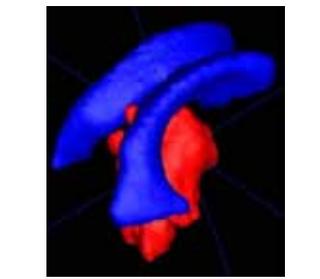
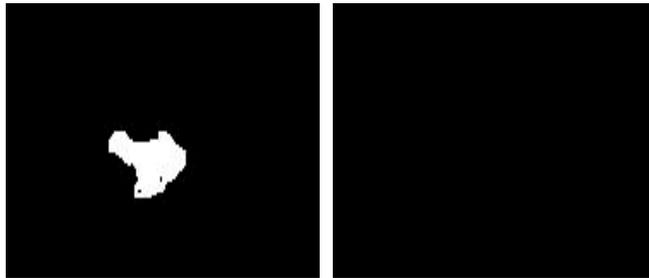
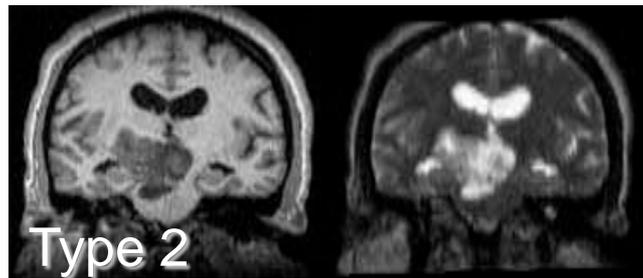
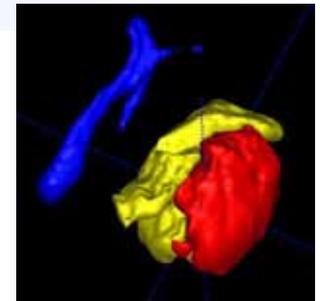
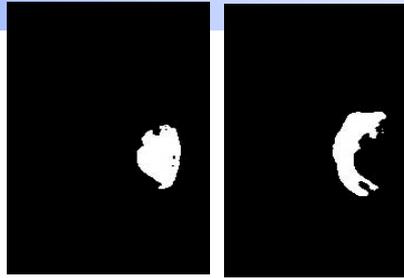
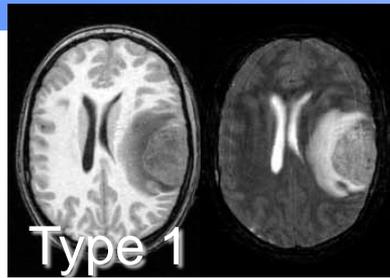
## Challenges:

- efficient, stable 2D/3D implementation (implicit, fast marching,..)
- appropriate image match function to stop propagation



$$\frac{\partial V}{\partial t} = (g)^{r_{MCF}+1} \tilde{N} \times \frac{\partial \tilde{N}^j}{\partial t} + (g)^{r_{Ng}} (\tilde{N}g) \times \tilde{N}^j + (g)^{r_c} a |\tilde{N}^j| + c_s \times (g)^{r_s} \tilde{N}^{2j}$$

# Results Brain Tumor Segmentation



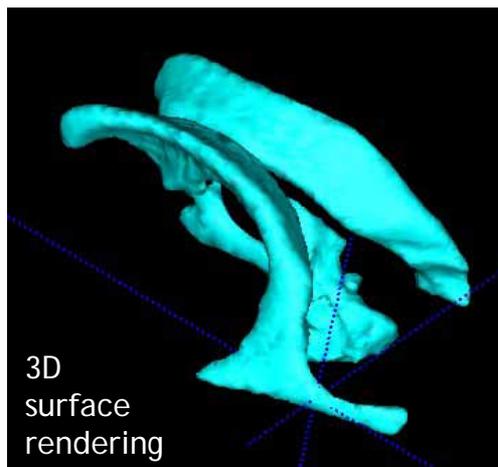
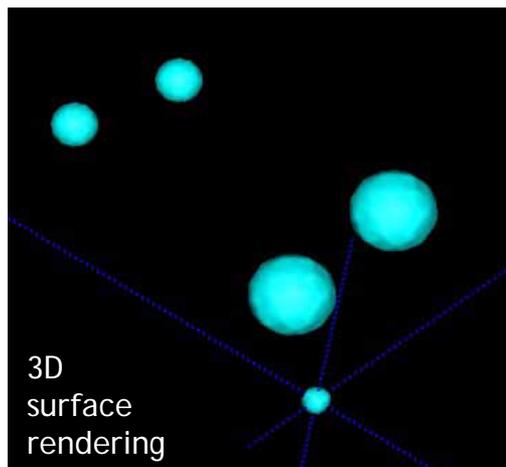
Prastawa et al., Media 2004

# Ventricle Segmentation by 3D Snakes: UNC SNAP Tool

Initial-  
ization  
by  
bubbles



Final  
Segmen-  
tation (10  
seconds)



Reliability: 0.99

Efficiency: 2 Min

Download:

<http://www.ia.unc.edu/dev>

# Use of deformable models in Vision I

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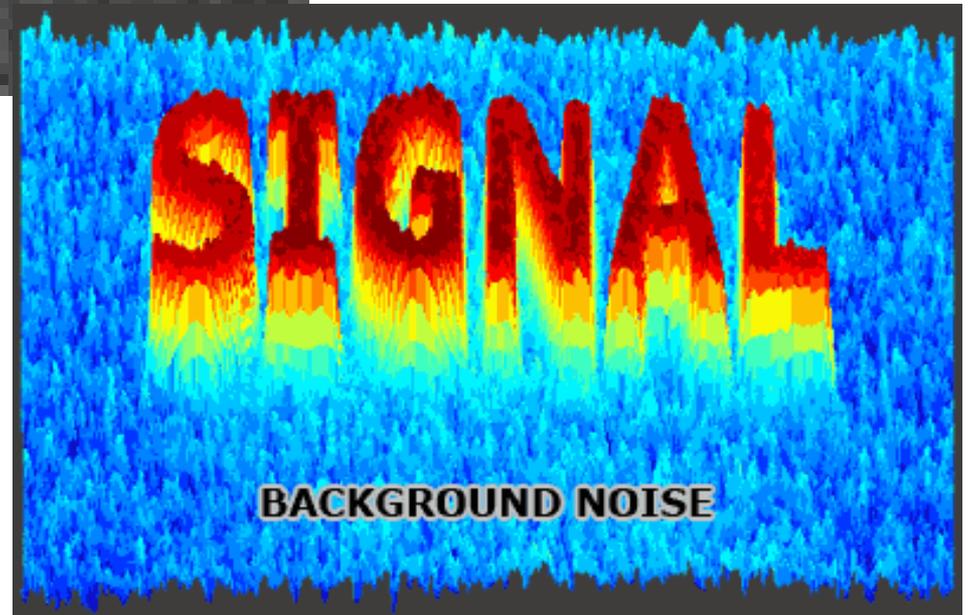
# Use of deformable models in Vision II

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**Unifying Boundary and  
Region-based information for  
Geodesic Active Tracking**



# Image Noise



# Blurring is diffusion

Linear isotropic diffusion,  $D$  is diffusion constant

$$\frac{\partial u}{\partial t} = \operatorname{div}(D \nabla u) = \nabla \cdot (D \nabla u)$$

$$1\text{-dim} : \frac{\partial u}{\partial t} = \frac{\partial}{\partial x} \left( D \frac{\partial u}{\partial x} \right)$$

$$D = \text{const} : u_t = D u_{xx}$$

# Blurring of images

- Reduction of noise and small details
- Blurring is diffusion

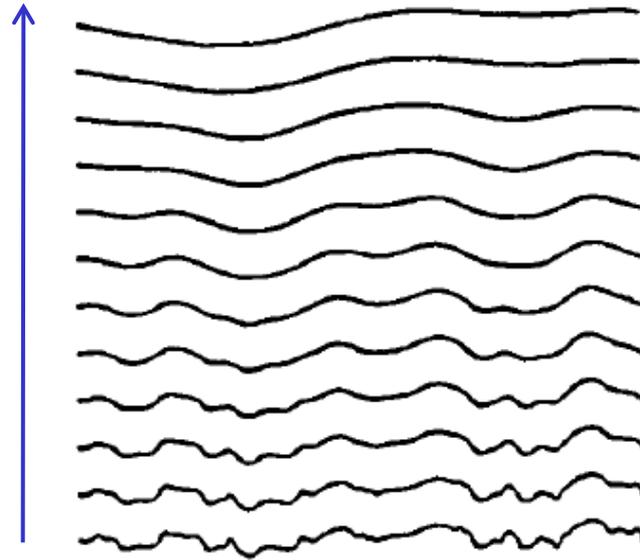
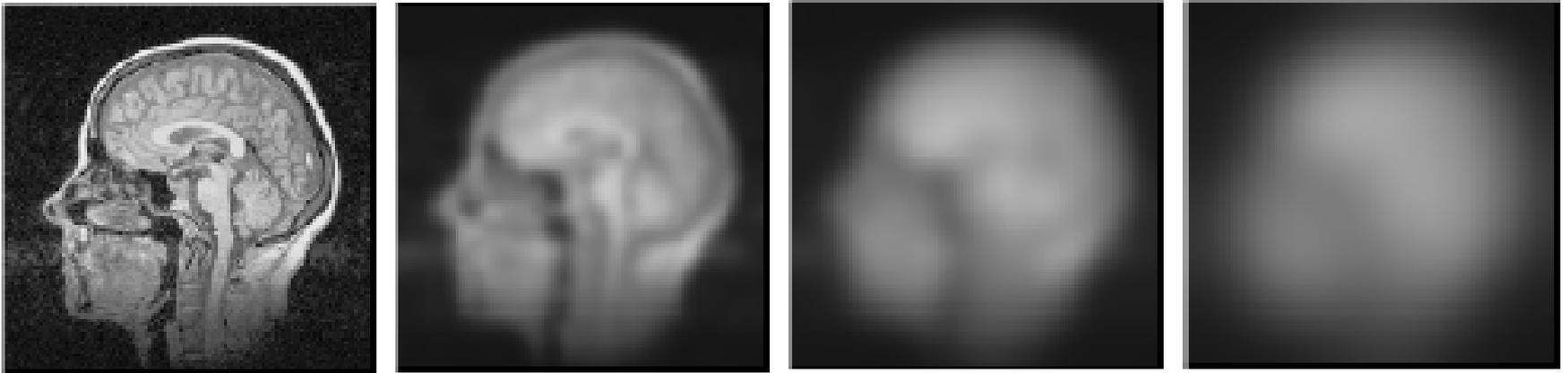


Fig. 1. A family of 1-D signals  $I(x, t)$  obtained by convolving the original one (bottom) with Gaussian kernels whose variance increases from bottom to top (adapted from Witkin [21]).

# Linear Diffusion

- Edge locations not preserved
- Region boundaries are preserved
- Gaussian blurring is local averaging operation and does not respect natural boundaries



Source: <http://www.csee.wvu.edu/~tmcgraw/cs593spring2006/index.html>

# We want noise reduction while keeping structure boundaries

Trick: Diffusion constant  $D$  becomes locally adaptive:

$D \rightarrow D(x,t)$ , i.e.  $D$  varies locally

e.g.: switch  $D$  to 0 near important image boundaries

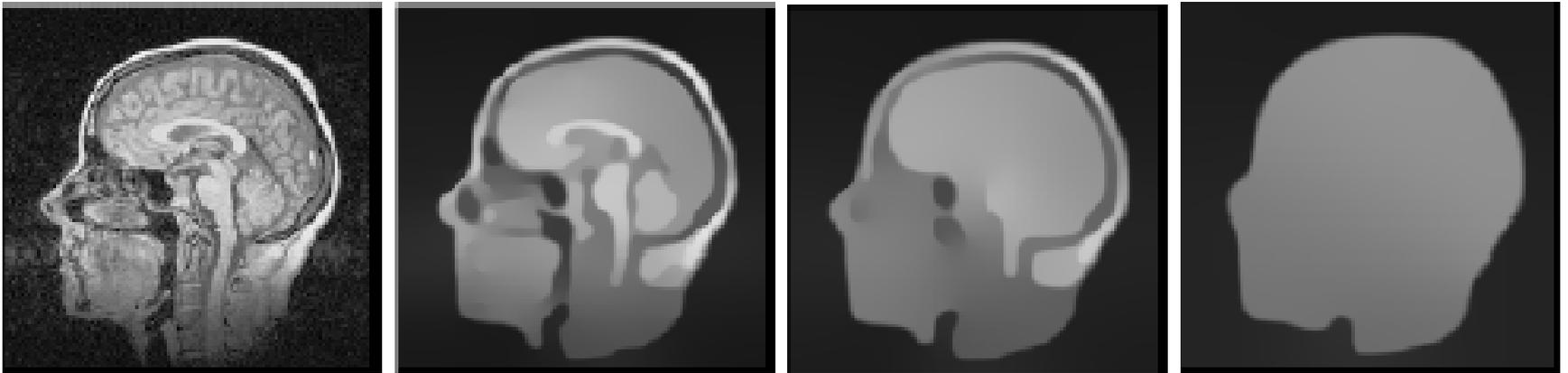
$$\partial_t u = \partial_x (\mathbf{D}(|\partial_x u|) \partial_x u)$$

[DemoMathematica](#)

Magic: This results in “inverse blurring”, or blurring with negative time, which is physically not possible.

# Nonlinear Diffusion

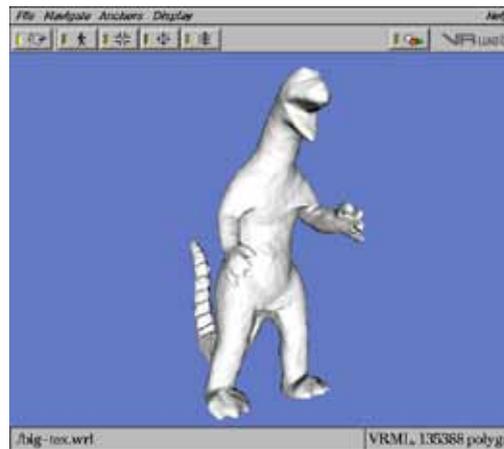
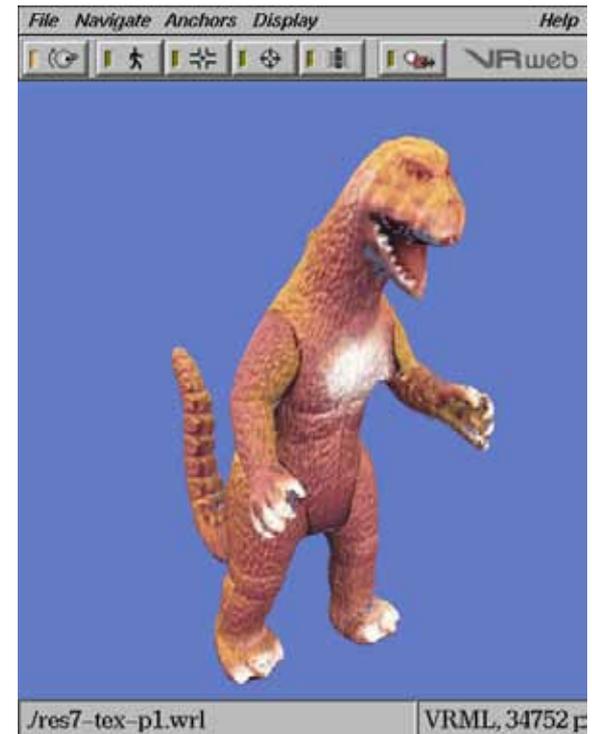
Multiscale image representation: Controlled blurring of structures by preserving wanted boundaries.



Source: <http://www.csee.wvu.edu/~tmcgraw/cs593spring2006/index.html>



# Shape from silhouettes

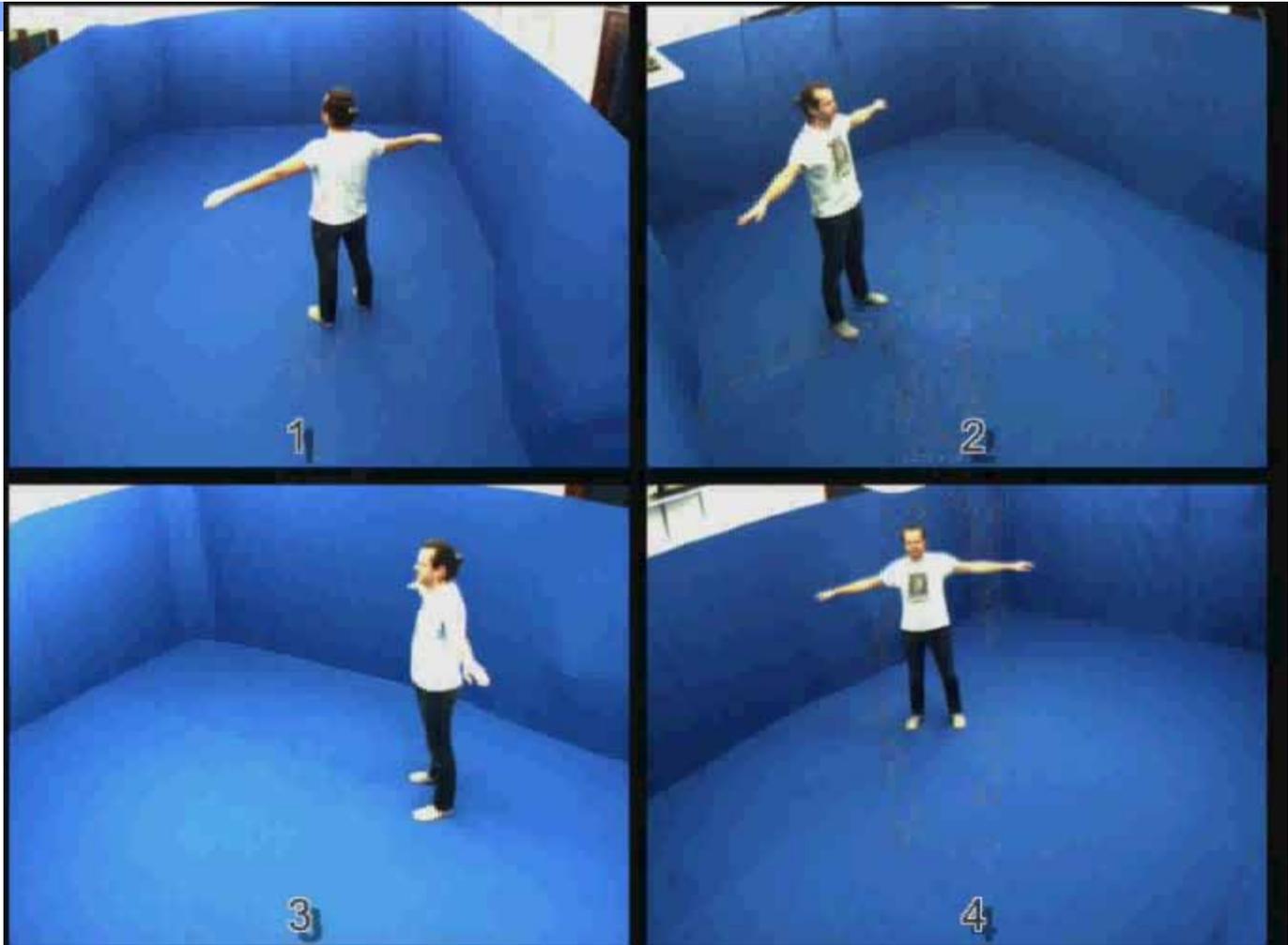


Slides from  
Lazebnik,  
Matusik  
Yerex  
and others

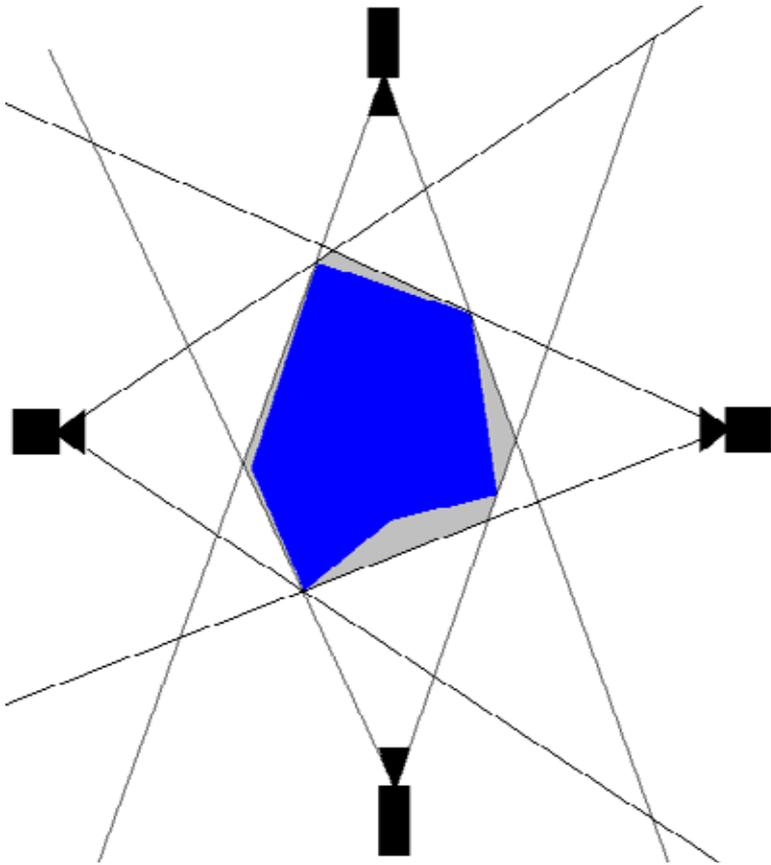
Automatic 3D Model Construction for Turn-Table  
Sequences, A.W. Fitzgibbon, G. Cross, and A.  
Zisserman, SMILE 1998



# Motivation: Movies



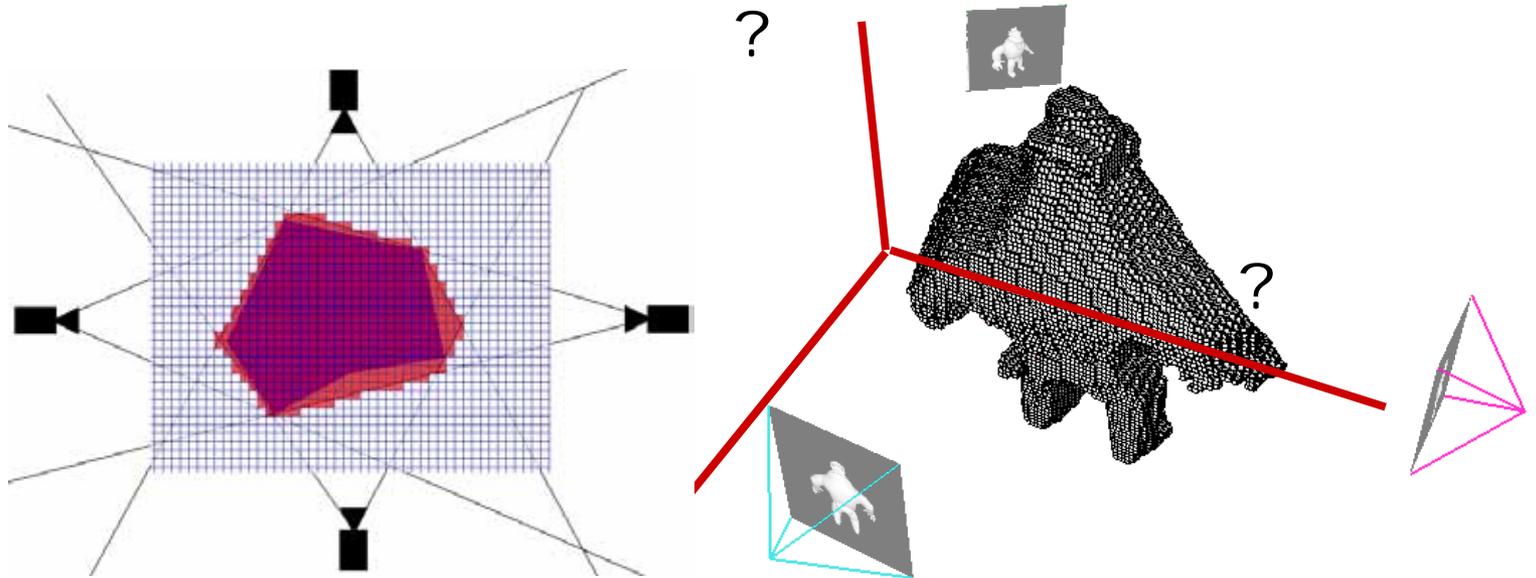
# What is shape from silhouette?



- With multiple views of the same object, we can intersect the *generalized cones* generated by each image, to build a volume which is guaranteed to contain the object.
- The limiting smallest volume obtainable in this way is known as the *visual hull* of the object.

# Visual hull as voxel grid

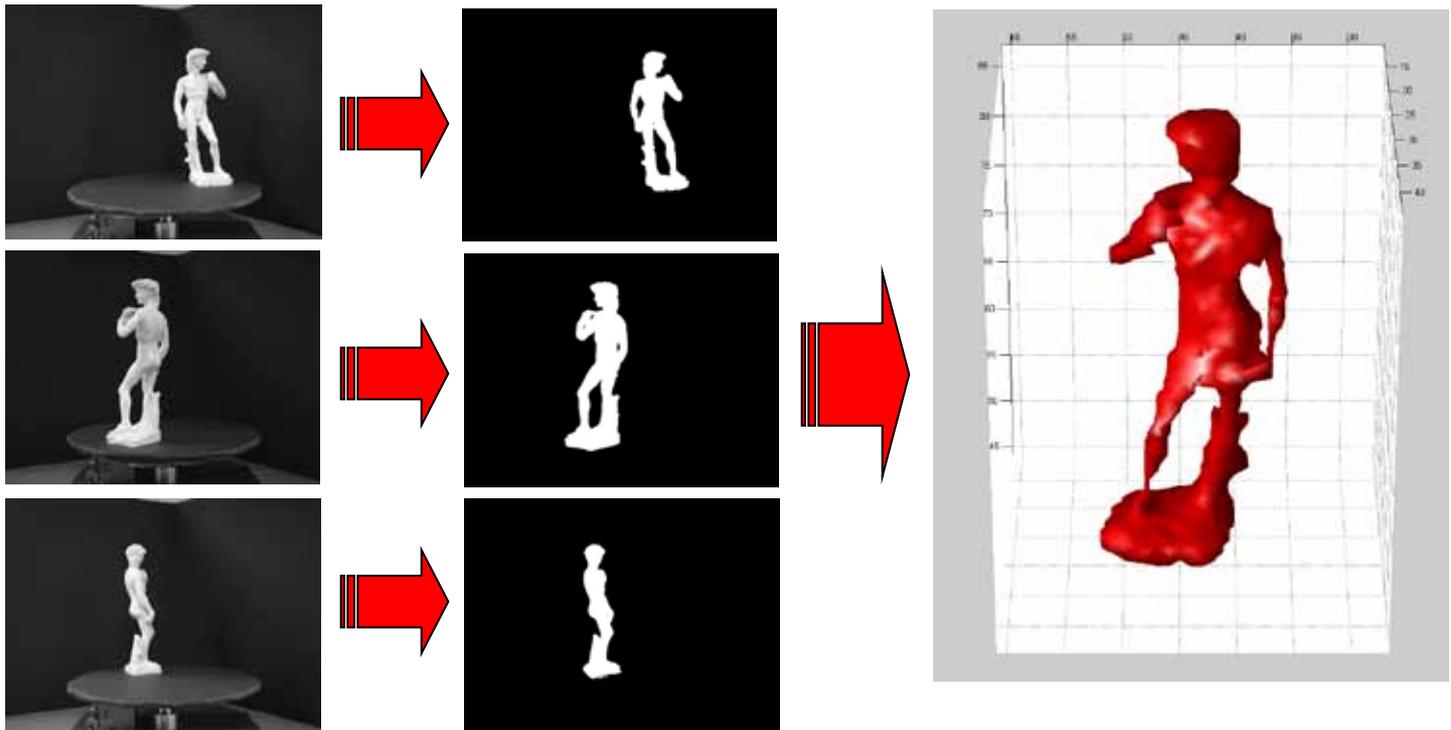
- Identify *3D region* using voxel carving
  - does a given voxel project inside all silhouettes?



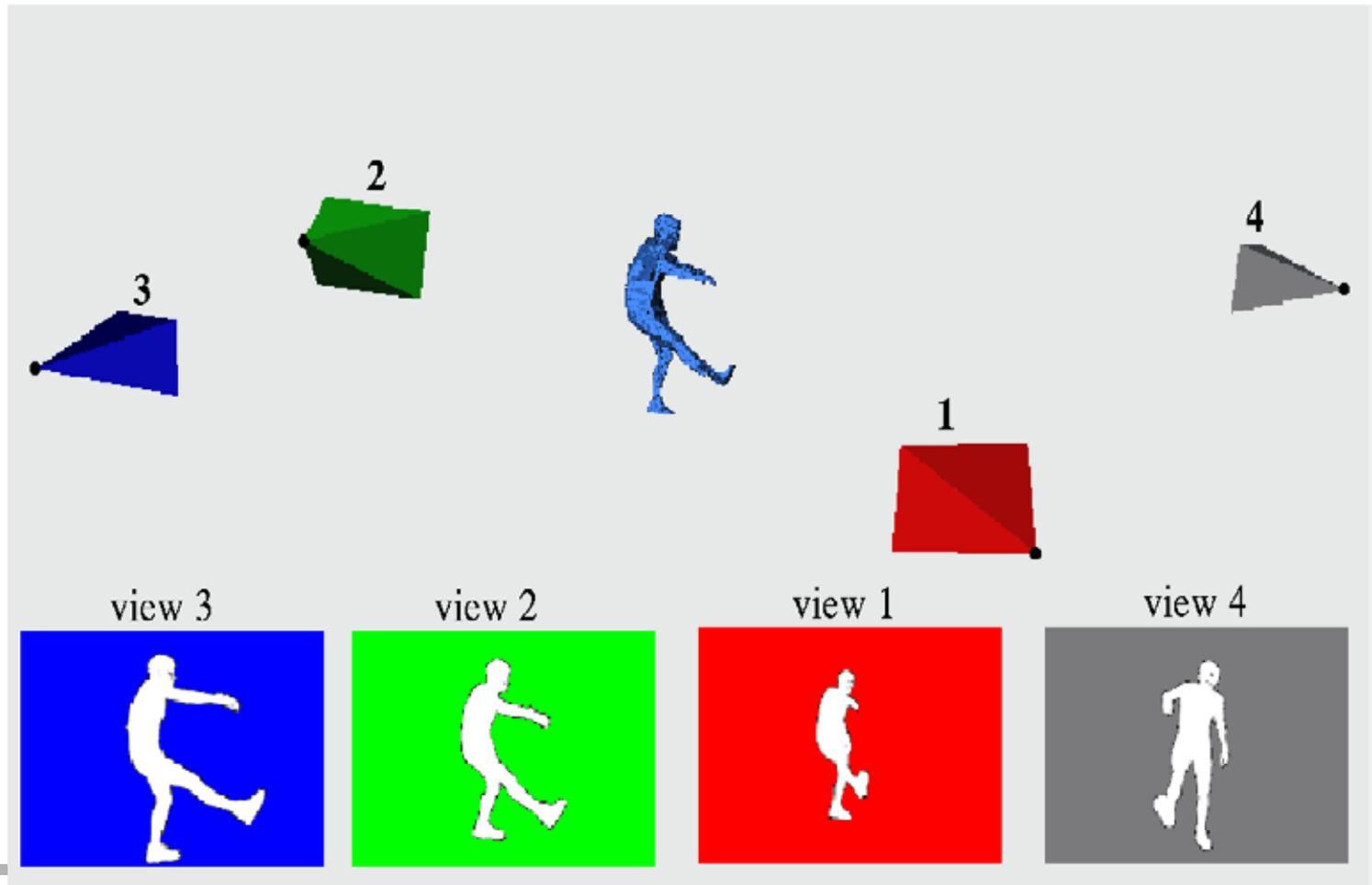
- pros: simplicity
- cons: bad precision/computation time tradeoff

# Example Student Project

- Compute visual hull with silhouette images from multiple calibrated cameras
- Compute Silhouette Image
- Volumetric visual hull computation
- Display the result



# Metric Cameras and Visual-Hull Reconstruction from 4 views



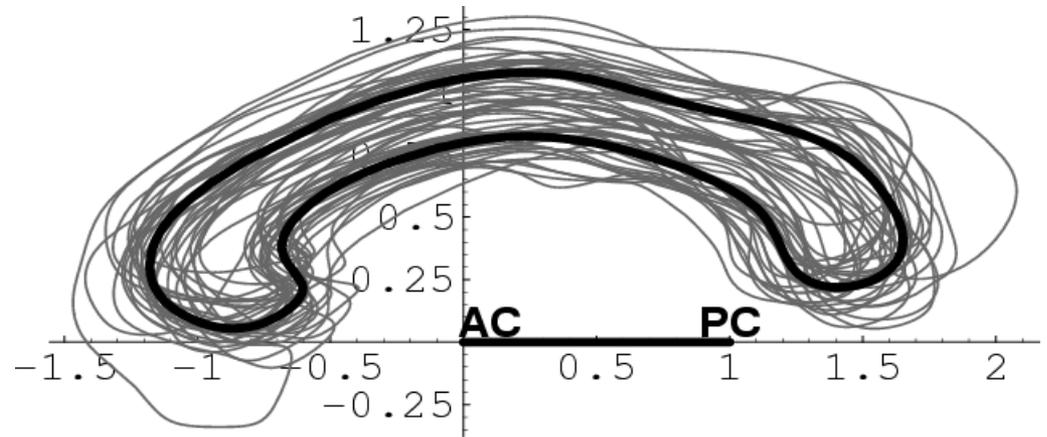
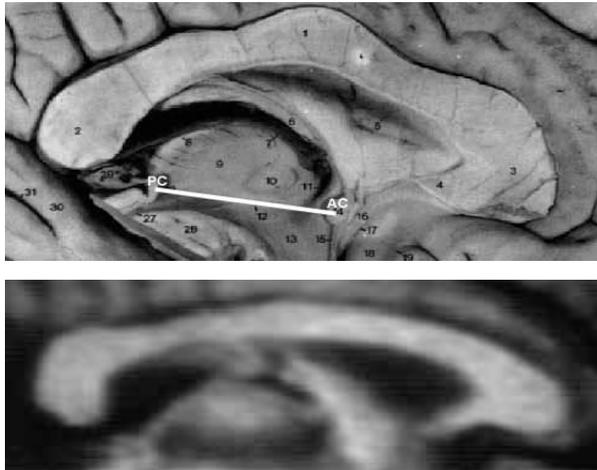


# Using probabilistic shape models

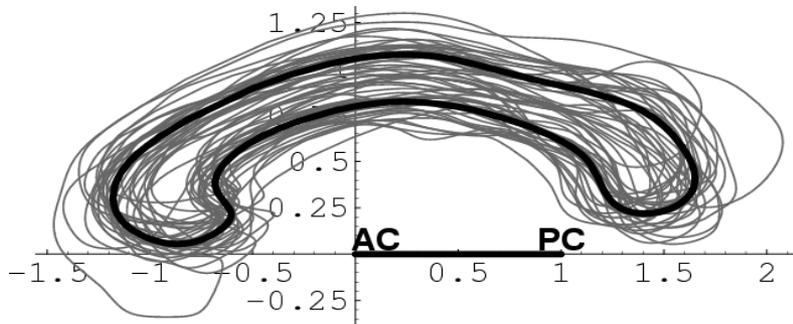
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- Segmentation could be improved if we know the shape to be extracted.
- Idea: Using shape models:
  - Typical shape template -> Deformation
  - Statistical shape models -> Describe “shape space”, ensure that deformation stays within space of meaningful shapes

# Natural Shape Variability



# Notion of Shape Space



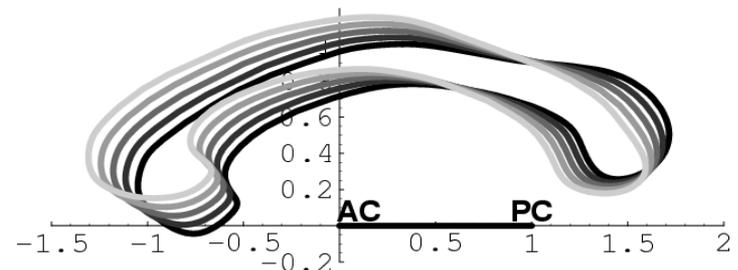
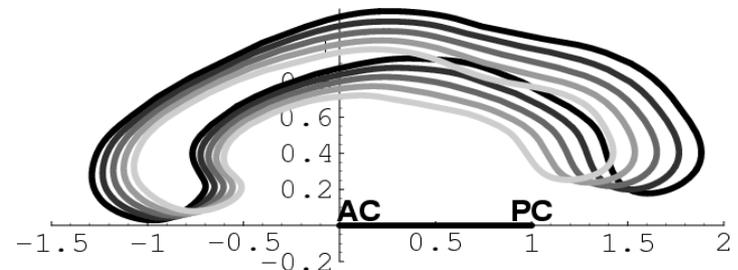
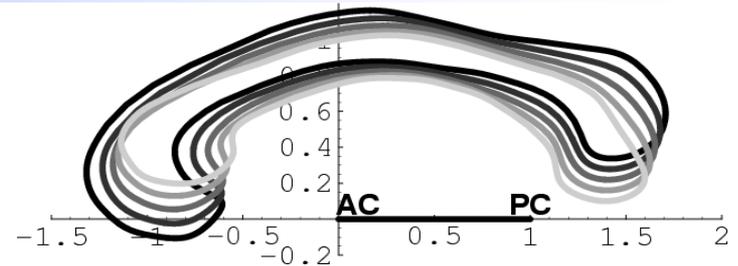
Outlines of the 71 corpora callosa (fine) and the computed average corpus callosum (bold).

Alignment

Parametrization (arc-length)

Principal component analysis

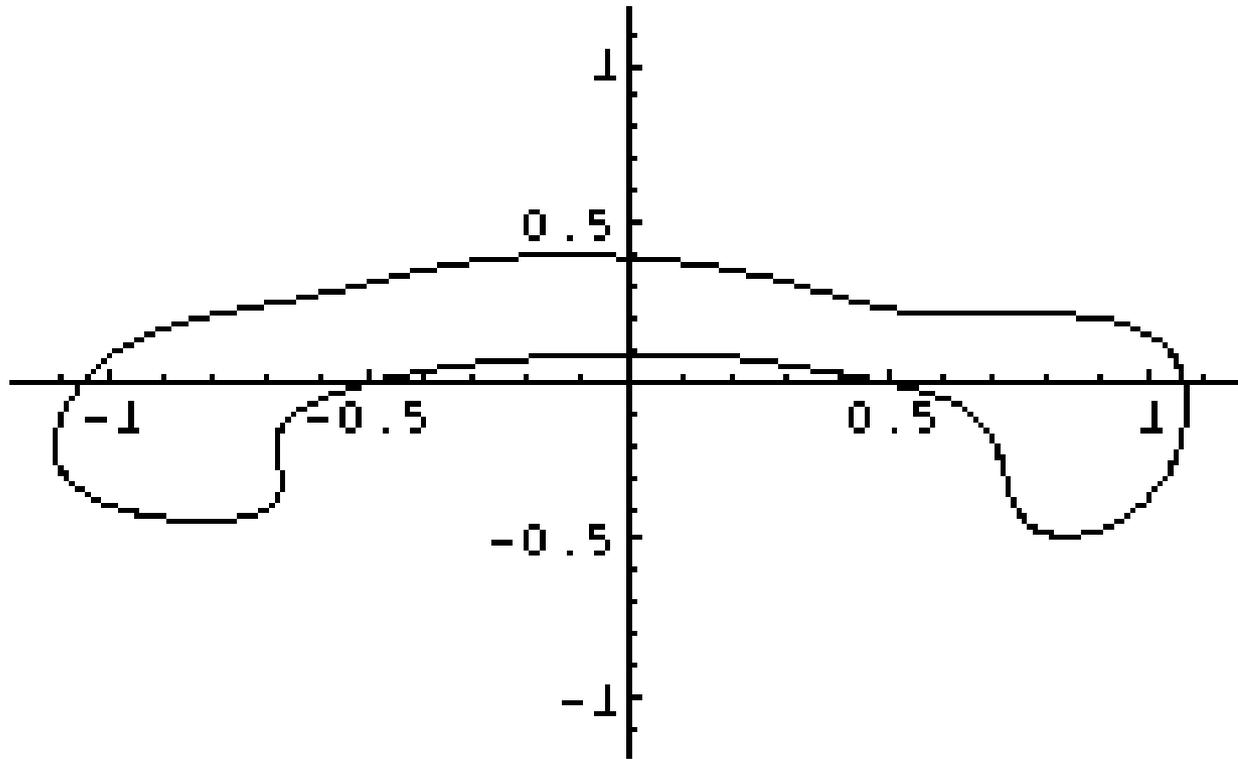
▷ Average and major deformation modes



The computed major modes of shape variation (top to bottom: modes 1,2 and 3).

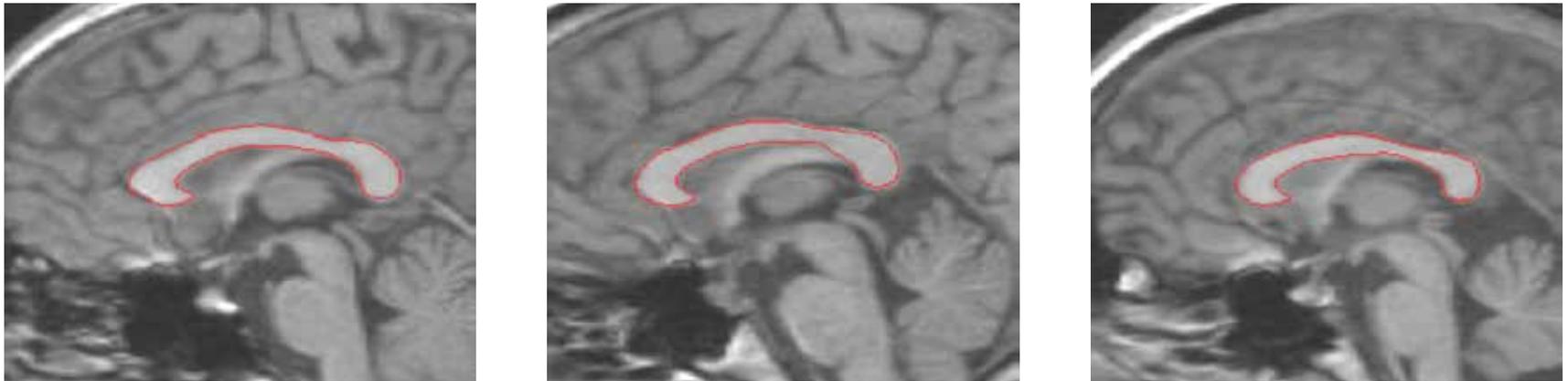
# First Eigenmode of Deformation (CC)

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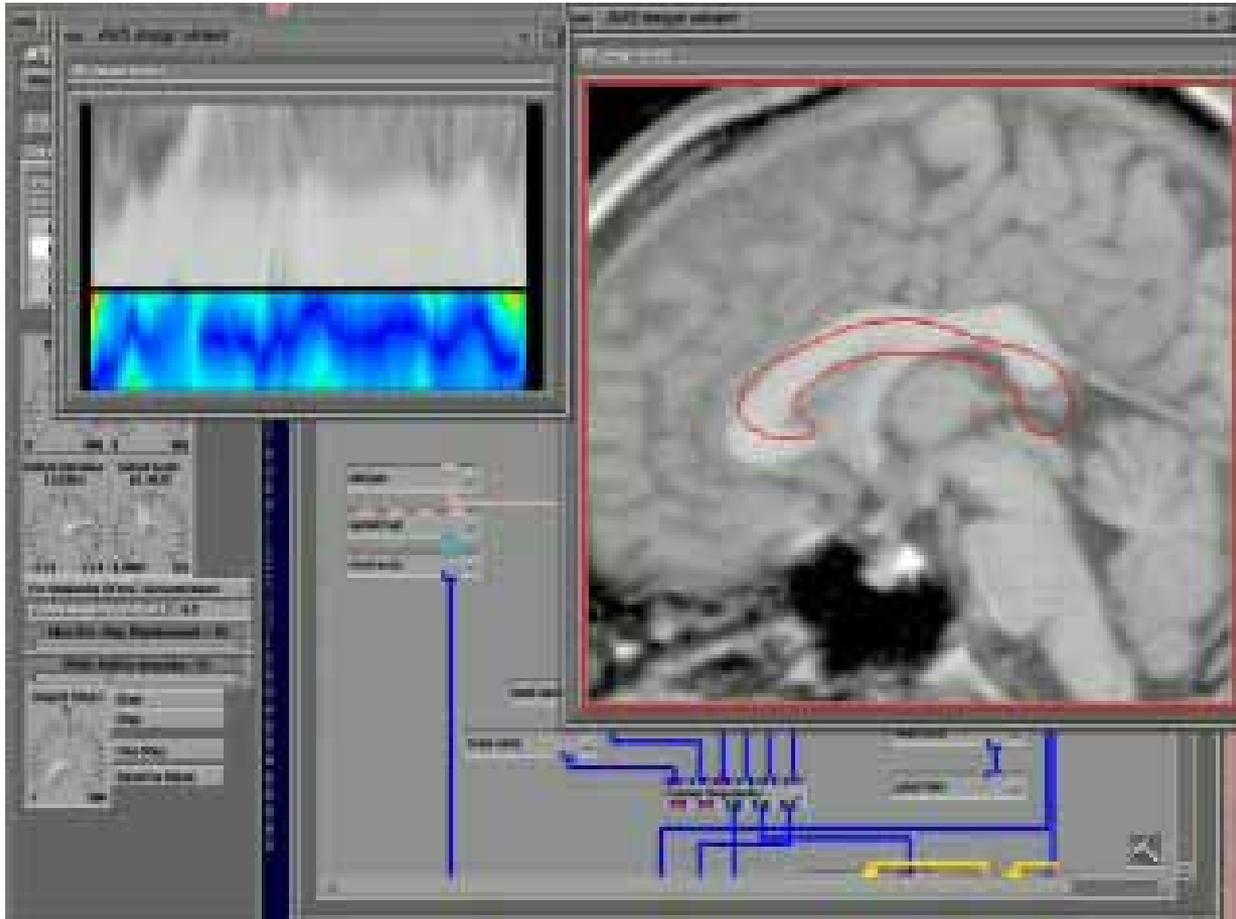
# Segmentation by deformable models

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*Fig. 1: Visualization of 3 MRI mid-hemispheric slices and the final positions (in red) of the automatic corpus callosum segmentation algorithm using deformable shape models.*

# Automatic deformable model based 2D segmentation



Example of model-based segmentation that uses a statistical shape model and a model of the boundary transition information.

# Image Processing

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- Input: Digital images
- Output: set of measurements, models, morphometric measurements, objects in abstract representation
- Key procedures:
  - Preprocessing, filtering, correction for artefacts
  - Geometric transformations (image registration)
  - Feature detection (edges, lines, homogeneous patches, texture)
  - Grouping of features to objects
  - Model-based versus data-driven segmentation
- Needs:
  - Math, Algorithms
  - Numerical implementations
- Excellent material: <http://homepages.inf.ed.ac.uk/rbf/CVonline/>

# Why Image Analysis?

- Image Analysis and Computer Vision offer exciting research projects.
- Ideal area for CS (algorithms, math, coding, visualization, data structures ...), ECE (robotics, pattern recognition, signal processing), BioEng (medical image analysis, and ME (robotics)
- Faculty at SCI from SoC, ECE, BioEng:
  - Ross Whitaker, Sarang Joshi, Guido Gerig, Tolga Tasdizen, Tom Fletcher, Marcel Prastawa, Rob MacCleod
- **Weekly “ImageLunch” Seminar CS 7938: Mondays 12:15-1:25, WEB 3760 Evans and Sutherland Room**
- **Main courses:** Image Processing (CS 6640, Fall), Computer Vision (CS 6320/6968, Spring), advanced courses

# Next Lecture Thu Aug 25

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- Read Preface and Chap 1 of the G&W book (pdf's on web-page).
- Get familiar with class web-page.
- Purchase class book.
- others