

DEPARTMENT OF MATHEMATICS, UNIVERSITY OF UTAH
Introduction to Optimization
MATH 5770/6640, ME EN 6025 – Section 001 – Fall 2021
Homework 2
Optima and optimality conditions

Due September 21, 2021

Submit your homework assignment in hard copy, in-class on the due date.

Text: *Introduction to Nonlinear Optimization*, Amir Beck,

Exercises: # 2.1,
2.2,
2.4,
2.6,
2.11,
2.13(i, ii),
2.15(i, iii, iv, vii),
2.17(i,iii,vi,vii),
2.18

Additional problems:

P1. Define

$$\mathbf{A} = \begin{pmatrix} 1 & 2 \\ 2 & 4 \end{pmatrix}.$$

Using your favorite software, visualize a plot of the Rayleigh quotient $f(\mathbf{x}) = R_{\mathbf{A}}(\mathbf{x})$ for $\mathbf{x} \in [-3, 3]^2 \setminus \{\mathbf{0}\}$, and generate a contour plot for f . Use this visualization to verify the maximum and minimum values of f , as well as the set of \mathbf{x} that are maximizers and minimizers.