

For all the following multiple-choice questions, circle your answers clearly. No partial credit will be awarded; any scratch work will be ignored.

1. Which of the following is true about the method of separation of variables?

- (a) Only the heat equation can be solved using separation of variables
- (b) The initial and boundary conditions are discarded and ignored
- (c) The PDE cannot be time-dependent
- (d) After finding eigenfunctions, superposition is used to construct a general solution
- (e) The solution to the PDE problem is always the constant function

2. Consider the eigenvalue problem

$$\begin{aligned}\phi''(x) + \lambda\phi(x) &= 0, & 0 < x < 1 \\ \phi(0) &= 0, & \phi(1) = 0\end{aligned}$$

Which of the following is true about an eigenvalue  $\lambda$  for this problem?

- (a)  $\lambda = 0$  is an eigenvalue with eigenfunction  $\phi(x) = 0$
- (b)  $\lambda = \pi^2$  is an eigenvalue with eigenfunction  $\phi(x) = \sin(\pi x)$
- (c)  $\lambda = -e^2$  is an eigenvalue with no eigenfunction
- (d) There are no eigenvalues for this problem

3. What is the solution  $u(x, t)$  to the following PDE problem?

$$\begin{aligned}u_t &= u_{xx}, & 0 < x < L \\ u(0, t) &= u(L, t) = 0 \\ u(x, 0) &= \sin\left(\frac{3\pi x}{L}\right)\end{aligned}$$

- (a)  $u(x, t) = 0$
- (b)  $u(x, t) = \sin\left(\frac{3\pi x}{L}\right) \exp\left(-\left(\frac{3\pi}{L}\right)^2 t\right)$
- (c)  $u(x, t) = \frac{1}{L} \int_0^L \sin\left(\frac{3\pi s}{L}\right) ds$
- (d)  $u(x, t) = \sum_{n=1}^{\infty} \sin\left(\frac{n\pi x}{L}\right) \exp(-t)$