

For all the following multiple-choice questions, circle your answers clearly. No partial credit will be awarded; any scratch work will be ignored.

1. An equilibrium solution u_e for the heat equation (with appropriate initial and boundary conditions) satisfies which of the following properties in general?

- (a) u_e does *not* respect the boundary conditions.
- (b) $u_e = 0$.
- (c) u_e does *not* depend on time t .
- (d) u_e is a quadratic function.
- (e) u_e cannot be computed.

2. Suppose that $u_1(x, t)$ and $u_2(x, t)$ are two solutions to the linear, homogeneous heat equation. Which of the following results from the principle of superposition applied to the linear homogeneous heat equation?

- (a) There are no other solutions to this equation.
- (b) $u(x, t) = u_1(x, t)u_2(x, t)$ is a solution to this equation.
- (c) $u(x, t) = u_1(x, t) + u_2(x, t)$ is a solution to this equation.
- (d) Either $u_1(x, t)$ or $u_2(x, t)$ must equal the equilibrium solution $u_e(x)$.
- (e) Both $u_1(x, t)$ and $u_2(x, t)$ must be constant functions.

3. With u_1 and u_2 arbitrary functions, c_1 and c_2 arbitrary constants, and L an operator, which of the following is the definition of linearity of L ?

- (a) $L[c_1c_2u_1u_2] = c_1c_2u_1u_2$
- (b) $L[c_1u_1 + c_2u_2] = c_1L[u_1] + c_2L[u_2]$
- (c) $c_1L[u_1] = c_2L[u_2]$
- (d) $c_1L[u_1] + c_2L[u_2] = 0$
- (e) $c_1 + c_2 = L[u_1] + L[u_2]$