

1 **Nascent adhesions differentially regulate lamellipodium velocity and persistence**

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22 **Abstract**

23 Cell migration is essential to physiological and pathological biology. Migration is driven
24 by the motion of a leading edge, in which actin polymerization pushes against the edge and
25 adhesions transmit traction to the substrate while membrane tension increases. How the actin
26 and adhesions synergistically control edge protrusion remains elusive. We addressed this
27 question by developing a computational model in which the Brownian ratchet mechanism
28 governs actin filament polymerization against the membrane and the molecular clutch
29 mechanism governs adhesion to the substrate (BR-MC model). Our model predicted that actin
30 polymerization is the most significant driver of protrusion, as actin had a greater effect on
31 protrusion than adhesion assembly. Increasing the lifetime of nascent adhesions also enhanced
32 velocity, but decreased the protrusion's motional persistence, because filaments maintained
33 against the cell edge ceased polymerizing as membrane tension increased. We confirmed the
34 model predictions with measurement of adhesion lifetime and edge motion in migrating cells.
35 Adhesions with longer lifetime were associated with faster protrusion velocity and shorter
36 persistence. Experimentally increasing adhesion lifetime increased velocity but decreased
37 persistence. We propose a mechanism for actin polymerization-driven, adhesion-dependent
38 protrusion in which balanced nascent adhesion assembly and lifetime generates protrusions with
39 the power and persistence to drive migration.

40

41 **Keywords:** actin polymerization, cell migration, computational model, lamellipodium, nascent
42 adhesions

43

44 **Introduction**

45 Cell migration emerges from the controlled assembly of macromolecules that generate
46 the mechanical forces of cell migration. Directional migration is specifically associated with the
47 velocity and persistence of outward motion of the leading edge, termed lamellipodium protrusion
48 [1, 2]. The edge protrusion is generated by actin filaments polymerizing against the plasma
49 membrane and the formation of adhesions to the substrate [3, 4]. Actin polymerization generates
50 pushing force that overcomes membrane tension and moves the cell edge forward [3, 5-7].
51 Counterforce from the membrane simultaneously induces actin retrograde flow away from the
52 membrane and towards the cell center [7]. The actin retrograde flow becomes physically
53 anchored to the substrate by adhesions, which transmit the flow to the substrate as traction force
54 [8, 9]. Adhesion-mediated traction force promotes edge protrusion, but induces edge retraction if
55 excessive [8, 10]. The pushing and traction forces are balanced for protrusive activity, but how
56 the individual molecular dynamics generate this balance remains unknown.

57 Actin polymerization against the plasma membrane has been described as a stochastic
58 Brownian ratchet [11]. In the Brownian ratchet model, fluctuations in the membrane and the
59 actin filaments that abut the membrane create gaps between the two structures, which allow for
60 the addition of new monomers that push against the leading edge [11]. The lamellipodium
61 harbors an excess of monomeric actin that polymerizes onto existing filaments [7]. The actin
62 nucleator ARP2/3 increases net actin polymerization by initiating new filaments off of the sides
63 of existing filaments [12, 13]. Thus, ARP2/3 increases the number of actin filaments abutting
64 and ratcheting against the membrane.

65 Fibroblasts and most epithelial cells move via cycles of edge protrusion, in which
66 protrusions progress through protrusion initiation, reinforcement, and retraction phases that result
67 from changes in membrane tension [14, 15]. Protrusions are initiated by the un-tethering of actin
68 filaments from the membrane [16-18]. As the protrusion progresses, the membrane is stretched
69 and membrane tension increases, which pushes back on the actin filaments and decreases the
70 likelihood of new monomer addition [14, 19-21]. The mechanism by which filament elongation
71 decreases with tension is explained by a force-velocity relationship in which actin filament
72 elongation stalls at high force [22]. ARP2/3 activity increases after protrusion initiation in the
73 reinforcement phase, which is also named the power phase in reference to the increased number
74 of actin filaments pushing against the membrane [23-26]. Despite the increased pushing force,
75 the mechanical feedbacks between membrane tension and actin polymerization cause edge
76 velocity to slow after protrusion initiation.

77 The formation of small, transient adhesions in the lamellipodium, termed nascent
78 adhesions, promotes and is required for protrusion velocity and persistence in protrusion-
79 retraction cycles [27, 28]. Nascent adhesions work a molecular clutch, engaging and anchoring
80 the actin filaments undergoing retrograde flow to the extracellular matrix on the substrate [3].
81 This decreases actin flow velocity [14, 29] and converts the motion into traction on the substrate
82 and cell edge motion [30]. Because anchoring actin filaments onto adhesions also maintains the
83 actin barbed ends against the membrane, the assembly rate of nascent adhesions correlates with
84 leading edge velocity [31]. Molecular clutch disassembly depends on the amount of traction on
85 the adhesions [14, 32]. Adhesion traction peaks along with the rate of actin retrograde flow in
86 the reinforcement phase of edge protrusion [14, 24, 33]. The lifetime of nascent adhesions
87 initially increases along with actin flow, but then decreases as actin flow increases further [10,

88 24], resulting in a stick and slip mechanism between actin filaments and adhesions. When
89 nascent adhesions disassemble, they disengage from both the substrate and actin filaments [10].

90 The difficulty in experimentally isolating actin polymerization without affecting adhesion
91 dynamics and vice versa has precluded a complete understanding of how lamellipodial actin
92 polymerization and adhesion assembly and disassembly work together to control lamellipodium
93 protrusion. In order to assess the contributions of actin and adhesion dynamics to edge motion,
94 we developed a computational model that incorporates the Brownian ratchet mechanism (BR)
95 and the molecular clutch mechanism (MC) [10, 34]. The model revealed that increasing the
96 lifetime of adhesions supports cell edge velocity, but it reduces motional persistence in the initial
97 phase of protrusion. Manipulation and computerized tracking of adhesion lifetime in live cells
98 confirmed that adhesion lifetime promotes protrusion velocity but decreases motional
99 persistence. Together, our findings suggest a previously unappreciated role for nascent adhesion
100 force-dependent clutch mechanism in the control of initial leading-edge motion.

101

102 **Results**

103 We developed a novel computational model of lamellipodium protrusion based on
104 Brownian dynamics. The model incorporates: explicit actin filaments represented as polar rods
105 of interconnected units; nascent adhesions represented as dynamic point particles that link
106 filaments to a fixed substrate; and a flexible membrane represented as a series of rigid rods
107 connected by springs (Figure 1). We designed a 2D domain of $2\ \mu\text{m} \times 0.5\ \mu\text{m}$ size, in which
108 actin filaments fluctuate under thermal motion, polymerize, branch and depolymerize, and link to
109 adhesions. Actin polymerization produces a force against the membrane (F_{Pol}), which pushes the
110 membrane forward. The displacement of the membrane produces an increase in membrane

111 tension (F_M), which pushes the filaments away from the membrane and results in actin
112 retrograde flow. F_M also decreases the actin polymerization rate according to the decreasing
113 exponential force-velocity relation characteristic of the Brownian ratchet (BR) mechanism [11,
114 22, 35-37]. Filaments can link to substrate adhesions, which convert their retrograde flow into
115 adhesion traction (F_A). The model ensures force balance between F_{Pol} , F_M , and F_A , resulting in
116 relative movements of filaments and membrane at every time step (Figure 1A). The model
117 simultaneously implements the Brownian ratchet mechanism of actin filament polymerization
118 (BR) and the molecular clutch mechanism of adhesion dynamics (MC). The BR is implemented
119 through the force-dependent velocity of filament elongation under membrane tension [11, 22, 35-
120 37] (Figure 1B). The MC is implemented with biphasic force-dependent unbinding of adhesion
121 clutches [38, 39] (Figure 1C).

122

123 **The BR-MC model reproduces physiological lamellipodium motion**

124 The BR-MC model produces continuous filament polymerization, filament branching
125 against the membrane, and nascent adhesion assembly and disassembly. Membrane
126 displacement, increased membrane tension after displacement, actin retrograde flow, and
127 adhesion-mediated anchoring of the flow emerge from the molecular dynamics (Figure 2A and
128 Figure 2 - movie supplement 1). We first tested that our model reproduces previous
129 experimentally measured properties of the lamellipodium: edge motion velocity, actin retrograde
130 flow velocity, and adhesion traction force [33, 40]. In order to verify how actin filament
131 polymerization alone affects edge motion, we initially set membrane tension to $k_m = 0.3$ pN/nm,
132 which is a value consistent with measurements in epithelial cells [41, 42]. We used a constant
133 rate of actin filament branching ($k_{branch} = 0.5$ s⁻¹) that corresponds to experimentally measured

134 ARP2/3 activation [43], and a constant rate of adhesion unbinding ($k_{off} = 0.1 \text{ s}^{-1}$) that matches the
135 unloaded lifetime of integrin-ligand bonds [44-46]. We found that individual membrane
136 segments exhibited initial velocity peaks of 30 - 40 nm/s and slower velocities as the protrusion
137 progressed (Figure 2B). Within the corresponding segments of the lamellipodium, actin
138 retrograde flow increased as the protrusion progressed (Figure 2C). Traction forces exhibited
139 peaks of 60 - 80 pN (Figure 2D), consistent with experimental measurements of individual
140 adhesions [32]. Plotting membrane and actin retrograde flow velocities as a function of traction
141 force showed that membrane velocity increased and actin retrograde flow decreased as traction
142 increased from 0 to 40 pN (Figure 2E), as previously described [30, 32].

143 We averaged the velocities and traction forces across the middle 1 μm membrane
144 segment to mimic the computerized measurements from experimental images limited by the
145 resolution of light microscopy. The mean protrusion velocity peaked at 24.3 nm/s at 10 s and
146 slowed to 17.0 nm/s at 120 s (Figure 2 - figure supplement 1A), consistent with published
147 measurements of PtK1 epithelial cells using ($\sim 25 \text{ nm/s}$ [24, 33]). Actin retrograde flow
148 increased after protrusion initiation, from a mean of 18.9 nm/s at 10 s to a mean of 26.7 nm/s at
149 120 s (Figure 2C and Figure 2 - figure supplement 1B), also consistent with PtK1 measurements
150 (11.7 - 21.7 nm/s [24, 33]). The differences in time at which maximum edge velocity and
151 maximum retrograde flow were reached are in quantitative agreement with the observed timing
152 of lamellipodia actin retrograde in areas lacking significant traction force [24, 32, 33, 40].

153 We also validated the effects of membrane tension on the force relationships. In order to
154 capture a greater range of edge velocity values, we modeled the nonmotile portion of membrane
155 in cells by fixing the side boundaries of the modeling domain. Similar to our observations with
156 unfixed edges, edge protrusion slowed and retrograde flow increased as the protrusion

157 progressed (Figure 2 –figure supplement 2A-B). Traction forces were stable, but high at the
158 edges due to the high concentration of actin filaments and adhesions in the unstretched, tethered
159 space (Figure 2 –figure supplement 2C). We ran the model with low membrane tension (0.03
160 pN/nm) to replicate the scenario of protrusion initiation and with high membrane tension (3
161 pN/nm) to represent the protrusion reinforcement phase [15, 30, 47]). We found that under low
162 membrane tension, actin retrograde flow positively correlated with protrusion velocity (Figure 2
163 –figure supplement 2D). In contrast, under high membrane tension, actin retrograde flow
164 negatively correlated with protrusion velocity (Figure 2 – figure supplement 2D). This is
165 consistent with experimental data that shows high retrograde flow from the high rate of actin
166 polymerization against the tense membrane, but slow protrusion velocity due to the high tension
167 [20, 31, 32, 52].

168

169 **Actin polymerization and adhesion assembly and disassembly control lamellipodium** 170 **velocity**

171 In order to decipher the contributions of actin filament polymerization and adhesion
172 dynamics to membrane velocity, we systematically varied the rates of actin branching, adhesion
173 assembly, and adhesion disassembly (k_{branch} , k_{on} , and k_{off}). For simplicity, we averaged the
174 velocity of the 101 membrane segments, including the fixed edges of the modeling domain,
175 which resulted in lower velocities than reported in Figure 2. We found that increasing k_{branch}
176 four-fold (from 0.2 to 0.8 s⁻¹), with fixed adhesion assembly and disassembly rates ($k_{on} = k_{off} =$
177 0.1 s⁻¹), resulted in a 30% increase in protrusion velocity (from 16.6 nm/s to 21.5 nm/s, Figure
178 3A). Increasing adhesion assembly rate k_{on} five-fold (from 0.1 to 0.5 s⁻¹), with fixed $k_{branch} = 0.5$
179 s⁻¹ and adhesion $k_{off} = 0.3$ s⁻¹, resulted in a 10% increase in protrusion velocity (from 17.8 nm/s to

180 19.6 nm/s, Figure 3B). Increasing the disassembly rate of adhesions five-fold decreased
181 protrusion velocity 10% (from 19.8 nm/s to 18.4 nm/s, Figure 3C). Together, these results
182 indicate that actin assembly is the main driver of edge velocity and that actin's control can be
183 augmented by adhesion formation and lifetime. We tested how actin filament polymerization
184 and adhesion dynamics together govern membrane motion by systematically varying k_{branch} and
185 k_{off} . Membrane velocity increased with k_{branch} and decreased with k_{off} (Figure 3D). We also
186 tested how adhesion formation and lifetime control protrusion velocity by simultaneously
187 varying k_{on} and k_{off} and found that protrusion velocity peaks with the highest adhesion assembly
188 rate and lowest adhesion disassembly rate (Figure 3E). This indicates that protrusion velocity
189 depends on both adhesion assembly and maintenance. We found that the traction force
190 transmitted by adhesions also peaked with the highest adhesion assembly rate and lowest
191 adhesion disassembly rate, suggesting that adhesion traction force promotes edge protrusion
192 (Figure 3F).

193

194 **The lifetime of nascent adhesions regulates the velocity of the membrane**

195 Adhesion traction determines the lifetime (τ) of adhesions, which is the inverse of
196 unbinding rate ($\tau = 1/k_{off}$). To test the role of adhesion lifetime in protrusion, we incorporated a
197 force-dependent molecular clutch mechanism into the computational model. The molecular
198 clutch bases the probability of adhesion-actin bond breakage on tension and thus creates a
199 variable rate of adhesion inactivation (k_{off}). We tested three different force-lifetime relations for
200 the adhesions, varying for maximum lifetime, τ_{max} (Figure 4A). The breaking point for the
201 actin-adhesion bond, or force corresponding to τ_{max} , was set at 30 pN [48-50]. The peaks in
202 lifetime were either 3 s, 7.5 s, or 12 s, typical behavior of integrin unbinding from fibronectin

203 under load [48]. We used these force-lifetime relationships to control the probability of
204 adhesion-actin bond breakage during simulations with variable actin polymerization rate. We
205 found that membrane velocity increased proportionally with both k_{branch} and τ_{max} (Figure 4B).
206 Increasing actin assembly 4-fold resulted in a 17% increase in edge velocity (from 13.3 to 15.6
207 nm/s, using $\tau_{max} = 3$ s), while increasing adhesion lifetime 4-fold resulted in about a 6%
208 increase in velocity (from 15.6 to 16.5 nm/s, using $k_{branch} = 0.8$ s⁻¹). This result matched our
209 findings on actin and adhesion-mediated control of edge motion in the absence of the molecular
210 clutch (Figure 3D).

211 Increasing adhesion lifetime can have the secondary effect of increasing adhesion
212 density, observed in Figure 3. Using $k_{branch} = 0.5$ s⁻¹, we found that increasing adhesion lifetime
213 from 3 s to 12 s increased mean adhesion density from 299 to 505/ μm^2 (Figure 4 – Figure
214 Supplement 1A). We identified the range of allowed adhesions in simulations with $\tau_{max} = 3$ s
215 that would generate adhesion density of ~ 300 to 500/ μm^2 (Figure 4 – Figure Supplement 1B).
216 We then varied the maximum allowed adhesions to test how increasing adhesion density alone
217 affects protrusion velocity, using the intermediate $k_{branch} = 0.5$ s⁻¹. We found that increasing
218 mean adhesion density from 310 to 513/ μm^2 , independent of adhesion lifetime, increased
219 protrusion velocity 2.3%, from 14.51 nm/s to 14.85 nm/s (Figure 4 – Figure Supplement 1C and
220 D). Under the same conditions, increasing adhesion lifetime from 3 to 12 s resulted in a 4.6%
221 increase in protrusion velocity, from 14.55 nm/s to 15.22 nm/s (Figure 4B and Figure 4 – Figure
222 Supplement 1D). Thus, increased adhesion density resulting from increased lifetime does not
223 fully explain adhesion lifetime's effects on edge velocity. These findings substantiate our
224 conclusions that actin polymerization rate is the most significant driver of edge velocity and
225 adhesion lifetime augments the velocity.

226 We evaluated the contribution of actin assembly and adhesion lifetime to pushing force
227 on the membrane and the retrograde flow that results from membrane counterforce. We found
228 that force on the membrane increased with both k_{branch} and τ_{max} , as peak force on the membrane
229 occurred at the highest k_{branch} and τ_{max} (Figure 4C). Actin assembly was the main driver. With
230 $\tau_{max} = 3$ s, a four-fold increase in k_{branch} (from $0.2 - 0.4$ s⁻¹) increased pushing force 21% (from
231 0.38 to 0.46 pN). With $k_{branch} = 0.2$ s⁻¹, four-fold increase in τ_{max} (from $3 - 12$ s) increased
232 pushing force 11% (from 0.38 to 0.42 pN). In contrast, actin retrograde flow increased with
233 k_{branch} but decreased with τ_{max} (Figure 4D). The reduction in retrograde flow with adhesion
234 lifetime is expected from previous experimental observations [14, 29]. These simulations with
235 the τ_{max} variable suggest a critical role for the lifetime of nascent adhesions in regulating force
236 against the membrane and the resulting edge velocity and actin retrograde flow.

237

238 **The lifetime of nascent adhesions controls the persistence of membrane motion**

239 Because pro-migratory signaling pathways promote the disassembly of nascent adhesions
240 [53], which limited protrusion velocity in our model, we hypothesized that adhesion disassembly
241 might promote the alternative edge protrusion output of protrusion persistence. We quantified
242 protrusion persistence as the time between the large oscillations in membrane velocity,
243 determined by Empirical Mode Decomposition (Figure 5 – figure supplement 1). While
244 adhesion lifetime promoted protrusion velocity at low membrane tension (0.03 pN and 0.3 pN,
245 Figure 5A and B), it decreased its motional persistence (Figure 5C and D). Under high tension,
246 adhesion lifetime promoted membrane velocity without inhibiting persistence (Figure 5E and F).
247 We tested the hypothesis that increasing the lifetime of nascent adhesions reduces protrusion
248 persistence by slowing the motion of actin filaments and shortening the time it takes for actin

249 polymerization to stall. We computed the motion of actin filaments within 1 micron of
250 adhesions and varying τ_{max} . Increasing τ_{max} decreased the actin filaments' mean displacements
251 (Figure 5 – figure supplement 2A). Similarly, the time to stall, or decay time, for actin
252 polymerization decreased with increasing τ_{max} (Figure 5 – figure supplement 2B). Thus,
253 adhesion lifetime can decrease protrusion persistence by controlling actin filament mobility and
254 polymerization.

255

256 **Integrin activation promotes lamellipodium velocity and decreases its persistence**

257 To experimentally test the finding that adhesion lifetime promotes lamellipodia
258 protrusion velocity but limits persistence, we labeled adhesions in COS7 epithelial cells using
259 transient expression of Paxillin-mApple and imaged adhesion and edge dynamics during 5 min
260 of steady-state migration. We segmented the adhesions using focal adhesion analysis software
261 for quantification of the adhesions' lifetime [51] and used morphodynamics software to track the
262 edge motion [52] (Figure 6A and B). We noted that protrusions exhibited adhesions with
263 heterogeneous lifetimes, in which clusters of short-living adhesions co-resided with a few
264 longer-lifetime adhesions. The range of long lifetimes varied per movie, which appeared to be
265 related with edge protrusion. For example, a cell in which the longest lifetimes are ~4.7 min
266 (orange-colored adhesions in Figure 6A) showed slow, persistent progression of the cell edge
267 (Figure 6A). On contrary, a cell in which the longest lifetimes are ~10.6 min (yellow-colored
268 adhesions in Figure 6B) showed fast and more fluctuating protrusion behavior (Figure 6B).
269 Accordingly, we sampled the lifetimes of the top 1 percentile of long-living adhesions per movie
270 and obtained the corresponding protrusion velocities and persistent times of the closest edge
271 segments. Plotting edge velocity and persistence as a function of adhesion lifetime showed that

272 cell protrusions with longer mean adhesion lifetimes were associated with faster protrusion
273 velocity but shortened protrusion persistence (Figure 6C and D).

274 We also treated COS7 cells with Mn^{+2} , which increases adhesion lifetime and density
275 [44-46, 48]. Mn^{+2} stabilizes nascent adhesions by promoting integrins' structural shift to high-
276 affinity conformations for binding to extracellular matrix [10, 53, 54]. The cells transiently
277 expressed Emerald-Lifeact to label the cell edge. We imaged the cells' steady-state protrusion-
278 retraction cycles and quantified protrusion velocity and persistence with morphodynamics
279 software. We found that integrin activation with Mn^{+2} increased mean protrusion velocity but
280 decreased persistence when compared to untreated cells (Figure 6E and F). Together, these
281 results support our model that longer adhesion lifetimes are associated with faster protrusion
282 velocity but reduced protrusion persistence.

283

284 **Discussion**

285 Using our novel particle-based BR-MC model, we discovered that actin polymerization is
286 the main driver of lamellipodium velocity and that the force-dependent clutch mechanism of
287 nascent adhesions differentially controls lamellipodium velocity and persistence. Experiments in
288 migrating epithelial cells substantiated that nascent adhesion lifetime promotes protrusion
289 velocity and limits persistence. Directional migration requires persistent edge motion [1, 2],
290 which is optimal at intermediate extracellular matrix density and nascent adhesion concentration
291 [55]. Our findings suggests that in addition to extracellular matrix density, the strength of the
292 adhesion-actin interaction controls protrusion persistence.

293 Our study clarifies the contributions of lamellipodium actin polymerization and nascent
294 adhesions to overall edge motion. Previous models have indicated both that actin polymerization

295 is sufficient to drive edge protrusion and that adhesion promotes protrusion [28, 31, 56-59]. In
296 the recent model by Garner et al., filament polymerization alone generated stable protrusion [60],
297 which resembles the lamellipodia of fish keratocytes that glide with a static cell shape [61]. Yet,
298 the density of adhesion activation has been shown to promote and be required for protrusion
299 velocity and persistence in protrusion-retraction cycles [28, 59]. We showed that increasing
300 actin polymerization most significantly enhances protrusion velocity and that increasing the
301 nascent adhesion lifetime further supports edge velocity through the molecular clutch
302 mechanism. However, we found that increasing nascent adhesion lifetime reduced the edge
303 motional persistence when membrane tension was moderate, as in the initiation phase of
304 membrane motion. In live cells cycling through the phases of protrusion initiation,
305 reinforcement, and retraction, nascent adhesion lifetime associated with and promoted
306 lamellipodium protrusion velocity but limited persistence. This suggests that the nascent-
307 adhesion mediated regulation in the beginning of edge protrusion dictates the overall protrusion
308 activity.

309 We propose a mechanism for nascent adhesion lifetime's differential control of edge
310 velocity and persistence: the increase in edge velocity emerges from the traction that the
311 adhesions exert on the substrate to convert actin retrograde flow into edge motion, while the
312 decrease in persistence arises from the force-velocity relation of actin filaments polymerizing
313 against the plasma membrane. In the initial phase of lamellipodium protrusion, increasing
314 adhesion lifetime tethers the actin filament tips in proximity of the edge, which supports actin
315 filament pushing against the membrane until membrane tension stalls polymerization. The
316 longer the time of filament anchoring, the faster this effect is reached, resulting in decreased
317 protrusion persistence with increasing τ_{max} . However, when membrane tension has increased,

318 such as at the end of the reinforcement phase, the increase in membrane tension that results from
319 polymerization is too nominal to affect the duration of actin filament polymerization. This
320 model, developed from our computational simulations, is supported by our experimental studies
321 and a complementary study in HT-1080 fibrosarcoma cells migrating slowly on aligned fibers of
322 extracellular matrix [62]. Our tracking of COS7 cell adhesion lifetime and edge motion found
323 that a few long-living adhesions govern edge protrusion. In the HT-1080 study, adhesion
324 lifetime was experimentally controlled by fiber orientation such that adhesions aligned with the
325 matrix had longer lifetimes and more persistent protrusions. When mature adhesions were
326 removed through inhibition of myosin II, the remaining nascent adhesions did not control
327 persistence. Rather, extracellular matrix fibers biased protrusion persistence along the fibers
328 through contact guidance [62].

329 Our BR-MC model revealed this critical and differential role of nascent adhesions in
330 supporting membrane motion because it incorporated the Brownian ratchet and molecular clutch
331 mechanisms without imposing feedback relations between the actin, adhesion, and membrane
332 dynamics. Prior models of lamellipodial protrusion at the sub micrometer length scale probed
333 the role of actin polymerization using the Brownian ratchet force-velocity relationship of actin
334 filament elongation pushing the membrane [60, 63, 64], or probed actin and adhesion
335 interactions by representing the actin as a gel with the molecular clutch adhesion lifetime-
336 traction force relationship [27, 28, 30]. However, none of the previous models [28, 56, 57, 65-
337 67], to the best of our knowledge, simultaneously incorporated the Brownian ratchet and
338 molecular clutch mechanisms without predetermined relations between membrane motion and
339 actin filament concentration or actomyosin contractility. In our model, lamellipodium dynamics
340 emerge spontaneously from interactions and force balance between actin filaments, membrane,

341 and adhesions. Because we focused on the roles of nascent adhesion dynamics and myosin-
342 independent actin flow, the BR-MC model does not incorporate effects from load adaptations
343 within the actin network or actomyosin contractility. Thus, we cannot exclude that membrane
344 tension feedback to actin network geometry and density [68-71] or traction force feedback to
345 actomyosin contractility and adhesion stabilization [29, 72] influences nascent adhesion
346 regulation of protrusion. Nevertheless, our experiments in cells detected the model's relationship
347 between adhesion lifetime on protrusion velocity and persistence. This suggests that nascent
348 adhesions also drive lamellipodium velocity and limit persistence in the context of other complex
349 interactions.

350 In summary, we establish an unexpected role for nascent adhesion lifetime in the
351 differential regulation of protrusion velocity and persistence. We previously showed that
352 integrin subunits have distinct flexibilities and conformations that affect the affinity and avidity
353 of interaction with the matrix [73]. The resulting strength of the integrin-actin molecular clutch
354 interaction controls adhesion lifetime, which controls lamellipodium actin assembly. Thus,
355 while actin polymerization is needed for nascent adhesion formation in edge protrusion [29, 31],
356 our findings indicate that integrin adhesions also control actin assembly. Future studies are
357 needed to determine which integrin-extracellular matrix interactions promote intermediate
358 adhesion lifetime for directed migration in heterogenous environments and how biochemical and
359 mechanical signaling affects adhesion lifetime to alter cell migration.

360

361

362 **Materials and Methods**

363 **Model of lamellipodium protrusions based on Brownian Ratchet and Molecular Clutch** 364 **(BR-MC)**

365 We developed a 2D model of lamellipodium protrusion based on combining the
366 Brownian ratchet mechanism for actin filament polymerization against a cell edge [11, 22, 35,
367 37] with the molecular clutch mechanism for adhesions [38, 39]. The model domain is $2\ \mu\text{m}$ x
368 $0.5\ \mu\text{m}$ rectangular domain, with a moving boundary at the top that mimics the flexible cell edge
369 membrane (Figure 1A). Explicit elements in the domain are actin filaments modeled as rigid
370 rods of interconnected units, a flexible membrane of 101 elastically interconnected units, and
371 adhesions modeled as single point particles that create dynamic anchor points for the filaments.
372 Within the domain, actin filaments fluctuate in Brownian motion, polymerize at their barbed
373 ends, depolymerize at their pointed ends, create branches against the membrane and become
374 capped. Actin filaments polymerize against the edge membrane at assembly rate k_{pol} and
375 branching rate k_{branch} , which generates pushing force that induces outward membrane motion
376 (Figure 1A). Integrins undergo cycles of activation and deactivation, which correspond to their
377 addition to and removal from the simulation domain. These mechanisms are governed by kinetic
378 rates (Table 1). Filaments and integrins interact by establishing potential energies, and filaments
379 push the edge membrane by exerting force on it. The membrane motion increases membrane
380 tension, F_M , which results in retrograde flow of the actin filaments. Through the retrograde flow,
381 the F_M is transmitted to the adhesions in the form of traction force. In response to the traction
382 force, adhesions dynamically unbind at a force dependent rate, k_{off} . Displacements of actin
383 filaments and membrane are calculated over the course of the simulation as a function of the
384 forces acting on them, using the overdamped Langevin Equation as:

$$\frac{dr}{dt} = \frac{F_{TOT}}{\gamma}$$

385

386 where F_{TOT} is the sum of deterministic and stochastic forces, r is a position vector for the
387 elements in the system, γ is the environment drag coefficient (assuming cytoplasm viscosity),
388 and dt is the simulation time step. A complete description of the model, including the
389 implementation scheme and relative interactions between actin, adhesions and membrane, is
390 below.

391 Model initialization. During the initialization of the model, a membrane is placed on the
392 top boundary and the actin filaments are randomly distributed within the domain. Each actin
393 filament is initialized with a length of n units, with each unit representing 5 monomers or 15 nm.
394 The n number of units is randomly selected from a normal distribution with a mean of 15,
395 corresponding to an average filament length of 225 nm, a standard deviation of 2, and a
396 minimum n of 1. The concentration of actin filaments is maintained at a steady state of 9000
397 filamentary units in the simulation domain. This creates a buildup of actin filaments during the
398 first second of simulations, with the occasional addition of filaments thereafter in order to
399 maintain a steady concentration of filaments.

400 A finite number of integrins are allowed to activate and deactivate according to their
401 kinetic rates, until they reach a steady state concentration. Allowed adhesions = 1000 when
402 simulations are run using a force-independent k_{off} . Allowed adhesions = 2000 with force-
403 dependent k_{off} . The effective concentration of integrins emerges in the model from the relative
404 magnitudes of k_{off} and k_{off} .

405 Model iterations. The model is developed using MATLAB R2020b, using the explicit
406 Euler implementation scheme for performing each model iteration, which consists of kinetics,

407 force balance, and position updates. The kinetic events occur following sequential steps:
408 polymerization, depolymerization, capping and branching of the actin filaments, and adhesion
409 activation and deactivation. Then, interactions between actin filaments and membrane and
410 between filaments and adhesions are evaluated and the corresponding forces are calculated.
411 Last, based on the force balance between interacting elements, the relative positions between
412 actin filaments and membrane, and between actin filaments and adhesions are calculated, and the
413 boundary conditions applied.

414 Actin filament representation and dynamics. In the model, actin filaments are
415 represented as rigid and polar rods of interconnected units (Figure 1A). Their polymerization
416 occurs as addition of units at the filament barbed ends, with rate k_{polym} . Depolymerization occurs
417 as removal of units from the pointed ends, at a rate $k_{depolym}$. Actin filaments within a branch
418 window of 15 nm from the membrane can also form branches at a rate k_{branch} . Branching occurs
419 as elongation of new filaments from existing (mother) filaments in the direction towards the
420 membrane and at an angle θ relative to the mother filament. θ is randomly selected from a
421 normal distribution with a mean of 70 deg and standard deviation of 10 deg. Filaments capping
422 occurs at a rate k_{cap} , which stops filaments polymerization and branching.

423 Actin filament polymerization follows the Brownian ratchet mechanism. In order to
424 account for the effects of membrane tension on actin filaments polymerization, filaments
425 presenting barbed ends within 15 nm from the membrane slow their polymerization rate
426 depending on the force on them. For these filaments, the probability of polymerization is
427 calculated as $P_{polym} = C_p k_{polym} dt$, where the polymerization coefficient, C_p , varies between 0 and
428 1:

$$C_p = e^{-(F_M + F_B)/k_B T}$$

429 where F_M is membrane tension, F_B is a confining boundary which ensures a reflective boundary,
430 and $k_B T = 4.11$ pN nm.

431 Actin filament connection to adhesions. When a filamentary unit is within a distance
432 r_{thresh} from integrin, a harmonic interaction potential is established between the filament and
433 integrin, with force: $F_A = r_{0,A} k_A$, where k_A is the integrin-filament spring constant, and $r_{0,A}$ is the
434 distance from the equilibrium, resulting from actin retrograde flow. When an integrin switches
435 its state from active to inactive, the connection with the actin filament is lost and integrin
436 disappears.

437 Filament motion follows Langevin dynamics. The total force on each actin filaments is
438 computed as: $F_{TOT} = F_T + F_A + F_M + F_B$, where F_T is a Brownian, stochastic force following the
439 fluctuation dissipation theorem, F_A is the force from one or more bound integrins, F_M is the force
440 exerted by the membrane, and F_B is the boundary force which acts as a repulsive potential
441 preventing the filaments from crossing. When one filament presents one or more branches
442 and/or branches on branches, the interconnected filaments are treated as a rigid structure.

443 Filaments positions are calculated over time following Langevin equation in the limit of
444 high friction: $r_i(t) = r_i(t_0) + \frac{F_{TOT,i}}{\gamma_F} dt$ for $i = 1, 2, 3, \dots, N$, where N is the total number of
445 filaments and filament structures, γ_F is the frictional coefficient and dt is the simulation time
446 step.

447 Integrin representation and dynamics. Integrins are represented as single point particles
448 existing in two functional states: active or inactive, as they undergo cycles of activation and
449 deactivation at rates k_{on} and k_{off} , respectively. When active, integrins are placed in random
450 positions in the simulation domain and provide anchor points for filaments motion. When

451 inactive, they are removed from the domain. While integrin activation is governed by k_{on} , their
 452 de-activation occurs through one of two mechanisms: force-independent or force-dependent
 453 unbinding. In the first case, k_{off} has a constant value (Table 1). In the second case, k_{off} depends
 454 biphasically on the tension between actin filament and integrin, F_A . According to the catch-bond
 455 model for integrin unbinding, the unbinding rate is a sum of two exponentials with opposite signs
 456 (Figure 4A):

$$k_{off} = Ae^{as_1F_A} + Be^{bs_2F_A}$$

457 Three lifetimes versus force relations were used in the model (lifetime $\tau = 1/k_{off}$) and they are
 458 here referenced according to their maximum τ values (τ_{max}):

	$\tau_{max} = 3$	$\tau_{max} = 7.5$	$\tau_{max} = 12$
A	2.0	0.5	0.25
B	0.5E-5	0.5E-5	0.5E-5
a	-9.727E-3	-7.286E-3	-6.12E-3
b	0.3	0.3	0.3
s_1	6.8	6.8	6.8
s_2	1.0405	0.9228	0.8606

459 Membrane representation and dynamics. The edge membrane is represented with
 460 consecutive rigid rods, each 18 nm long, interconnected by harmonic interaction potentials of
 461 stiffness k_m and equilibrium separation $r_{0,M}$. Each membrane segment experiences two forces: the
 462 filaments pushing against it, and the pulling from neighboring membrane segments.

463 Over the course of the simulations, positions of membrane segments are updated
 464 following the Langevin equation, as: $r_s(t) = r_s(t_0) + (F_{pol,s} + F_{M,s}) \frac{dt}{\gamma_M}$ for $s = 1, 2, 3, \dots, 101$,
 465 where F_{pol} is the force from filaments, and F_M is the elastic force contribution from the
 466 connection with neighboring membrane segments. γ_F is the drag coefficient from the fluid in
 467 front of the membrane (outside the cell).

468 Determination of traction force. Mean traction force is the average of all adhesion-
469 filament connections over all time points and positions. All force values greater the 500 pN
470 resulted from motion too fast for the 1 ms timestep and were excluded ($F_A < 500$ pN).

471 Extraction of protrusion persistence. Velocity data for each membrane segment was
472 decomposed into its Intrinsic Mode Functions (IMF) using Empirical Mode Decomposition. The
473 first 7 IMFs were subtracted so that thermal noise oscillations in membrane velocity were on the
474 scale of real cell protrusion oscillations, in which change in velocity is at least 5 nm/s (Figure 5 -
475 figure supplement 1).

476

477 **Key resources table**

Reagent type (species or resource)	Designation	Source or reference	Identifiers	Additional Information
Cell line (<i>Chlorocebus sabaeus</i>)	COS7	ATCC	CCL-81.2	
Transient expression vector	pcDNA3-mApple Paxillin	Smith et al. 2013 PMID: 23990882		Dr. Mary Beckerle (University of Utah, Salt Lake City, UT)
Transient expression vector	mEmerald-Lifeact	Addgene	#54148	Emerald-Lifeact-7

478

479 **Cell culture**

480 COS7 cells were obtained from ATCC, cultured in Dulbecco's Modified Eagle Medium
481 (DMEM) with 4.5 g/L D-glucose, L-glutamine, and sodium pyruvate (Gibco 11965092)
482 containing 5% Fetal Bovine Serums (FBS, Avantor Seradigm 97068-085), and tested for
483 micoplasma every 3-6 months. Micoplasma-negative COS7 cells were plated on acid-treated 1.5
484 coverslips within 35 mm glass-bottom dishes (MatTek P35G-1.5-14-C), and transfected the
485 following day with pcDNA3.1/Paxillin-mApple or mEmerald-Lifeact at 20% confluency using
486 TransIT-LT1 (Mirus MIR 2304) following the manufacturer's instructions. Two days post-
487 transfection, medium was replaced with FluoroBrite DMEM (Gibco #) supplemented with 10%
488 FBS and 20 mM HEPES.

489

490 **Live cell TIRF imaging of adhesions**

491 For adhesion imaging, cells were imaged on an automated Nikon Ti inverted microscope
492 with motorized total internal reflection fluorescence (TIRF), Perfect Focus 3 to maintain laser-

493 based identification of the bottom of the substrate during acquisition, a CFI Apo TIRF 100x oil
494 Apo 1.49 NA objective, 561 solid-state laser (Vortran), ET620/60m emission filter (Chroma),
495 and Photometrics Prime 95B camera configured at a 100 MHz readout speed to decrease readout
496 noise with Metamorph. Images were taken every 3 s for 5 min, with sequential images at every
497 time point with the TIRF angle set to optimal TIRF and with the TIRF angle set as vertical for
498 effective widefield imaging. The acquired images had an effective pixel size of 45 nm. Imaging
499 was performed at 37°C, 5% carbon dioxide, and 70% humidity. Laser powers were decreased as
500 much as possible and the exposure time set at 200-400 ms to avoid phototoxicity.

501

502 **Adhesion segmentation, detection, and tracking**

503 Nascent adhesions were detected and segmented using point source detection as
504 previously described in [51, 74]. Briefly, fluorescence images were filtered using the Laplacian
505 of Gaussian filter and then local maxima were detected. Each local maximum was then fitted
506 with an isotropic Gaussian function (standard deviation: 2.1 pixels, i.e. ~180 nm) and outliers
507 were removed using a goodness of fit test ($p=0.05$). The point sources detected for nascent
508 adhesions were tracked over the entire frames of the time-lapse images using uTrack [75].
509 Lifetimes of adhesions were calculated from lifetimes of individual tracked trajectories. A GUI-
510 based MATLAB software for the edge analysis is from Danuser lab [52]. Due to the noise in
511 edge motion from the 3 s framerate, IMFs were removed in the edge motion data.

512

513 **Live cell confocal imaging of cell edge and analysis**

514 For cell edge imaging, cells expressing mEmerald-Lifeact were imaged on a Nikon Ti
515 inverted microscope with a CFI Apo TIRF 60x oil, 1.45 NA objective employing Perfect Focus,

516 a Yokagawa CSU-10 spinning disk confocal with Spectral Applied Research Borealis
517 modification, a 488 solid-state laser, Chroma ET525/50m filter, and Photometrics Myo CCD
518 camera with Metamorph. Images were taken every 10 s for 5 min, with 400-700 ms exposures.
519 For experiments with prolonged adhesion lifetime, cells were treated with 1 mM MnCl₂ 2 h prior
520 to imaging. Time-lapse images were analyzed for cell edge protrusion dynamics in MATLAB
521 software as described previously [76]. A GUI-based MATLAB software for the edge analysis is
522 from Danuser lab [52]. A two-sample nonparametric Kolmogorov–Smirnov test at 5%
523 significance tested for population distribution equality. IMFs were not removed from this edge
524 motion data.

525

526 **Statistics**

527 Models were run until additional iterations no longer changed the result output.
528 The non-parametric Mann-Whitney U test was used to test for difference in the means for all
529 modeling data and adhesion-edge analyses. Experiment sample size was chosen based on a
530 minimum of three independent biological replicates and hundreds to thousands of
531 adhesions and protrusion events analyzed, respectively, within each replicate. The
532 Kolmogorov-Smirnov test was used to test for difference in the distribution of edge motion
533 upon Mn⁺² treatment. Unless otherwise mentioned in each figure caption, * $p < 0.05$, ** $p < 0.01$,
534 *** $p < 0.001$, **** $p < 0.0001$.

535

536 **Software availability**

537 MATLAB software for the computational model is shared via GitHub at

538 <https://github.com/KRCSLC/ProtrusionModel>.

539 A GUI-based MATLAB software for the adhesion analysis is shared via GitHub at
540 <https://github.com/HanLab-BME-MTU/focalAdhesionPackage.git>; [Han, 2021](#); copy archived at
541 [swh:1:rev:6aeb3593a5fd3ace9b0663d1bf0334decfb99835](https://www.swh.io/rev/6aeb3593a5fd3ace9b0663d1bf0334decfb99835).

542

543

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552

553 **Competing Interests**

554 The authors declare no competing interests.

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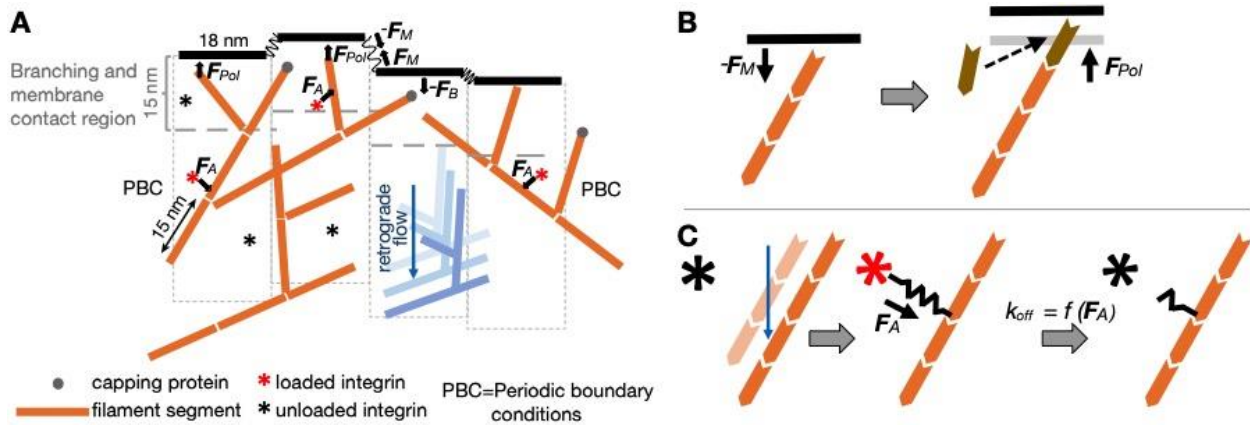
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750

751

752 **Figure 1**

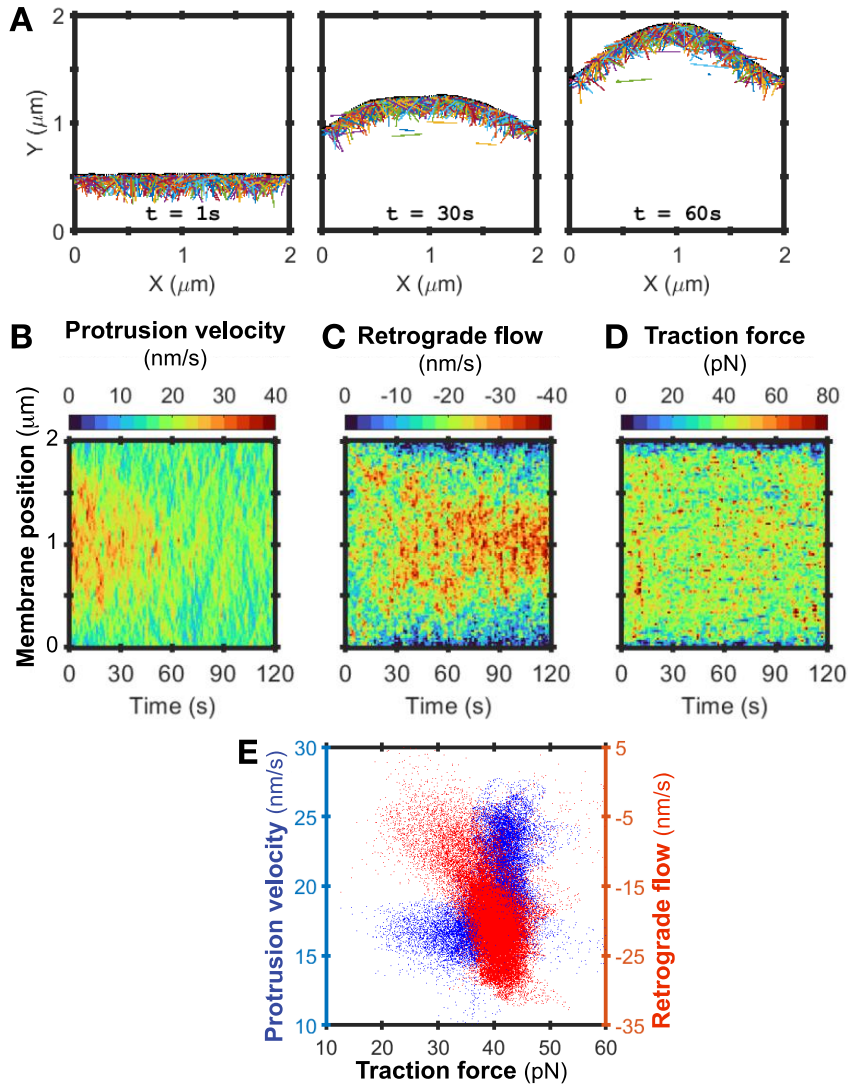


753

754 **BR-MC model of lamellipodium protrusion.** (A) Elements and interactions in the 2D
 755 computational model. Actin filaments are represented as polarized rigid rods of consecutive 15
 756 nm units with each unit representing 5 actin monomers. Capping proteins bind the filaments
 757 with rate k_{cap} and prevent further polymerization. Each actin filament can form branches at a 70°
 758 angle within 15 nm from the edge membrane (k_{branch}). Polymerization with rate k_{pol} against the
 759 membrane pushes the membrane forward (F_{Pol}). The membrane is represented as rods
 760 interconnected by harmonic potential energies with defined stiffness k_m , which create tension
 761 upon displacement, F_M . A boundary force (F_B) prevents the filaments from crossing the
 762 membrane. The membrane and boundary forces restrain actin polymerization and induce
 763 retrograde flow. Adhesions are represented as integrins that undergo cycles of activation and
 764 deactivation, with k_{on} and k_{off} , respectively. When active (black star), the adhesions connect actin
 765 filaments if within a proximity of 15 nm (red star). Adhesion engagement is represented as a
 766 spring and builds tension against the substrate in response to actin retrograde flow (adhesion
 767 tension, or traction force, F_A). Adhesion density is maintained within the physiological range
 768 ~ 500 integrins/ μm^2 [77]. A periodic boundary condition wraps the model edges and creates an
 769 infinite domain in which all the membrane segments experience spring tension on both sides.

770 For each time step, the new position for each actin filament is computed from the sum of
771 Brownian forces, F_B , F_M , and F_A . The new position for each membrane segment is computed
772 from the sum of F_{Pol} , F_M , and F_A . **(B)** The BR mechanism. Polymerized actin filaments (orange)
773 undergo thermal motion in the 2D domain near the membrane. Addition of a new monomer
774 (brown) against the membrane pushes the membrane outward with F_{Pol} . **(C)** The MC
775 mechanism. Actin undergoes retrograde flow (blue arrow) and integrins are activated (black
776 star). Activated integrins bind to an actin filament to create adhesions with traction force (F_A ,
777 red star) that slows the filament's flow and controls adhesion unbinding.
778

779 **Figure 2**



780

781 **Model reproduces physiological rates of edge protrusion and retrograde flow.**

782 (A) Snapshots from model simulations over run times in seconds (s). Individual filaments are

783 depicted in different colors. Parameters listed in Table 1. Membrane movement in Y from the

784 sum of forces (F_{Pol} , F_M , and F_A). (B) Heatmap of mean edge velocity at each 20 nm membrane

785 position (18 nm rod + 1 nm of spring on each side). 2 minute (min) simulation with $k_m = 0.3$

786 pN/nm, $k_{branch} = 0.5\text{ s}^{-1}$, $k_{on} = 1\text{ s}^{-1}$, $k_{off} = 0.1\text{ s}^{-1}$, and periodic boundary conditions. Sampling

787 every 0.001 s, averaged over 1 s intervals. Representative of $n=10$ iterations. (C) Heatmaps of

788 retrograde flow and **(D)** traction force, computed from simulations, sampling, and averaging as
789 in B, and smoothening using a 2-D Gaussian filter with $SD = 0.5$. **(E)** Edge protrusion velocity
790 and actin retrograde flow plotted as a function of traction force. Data from 3 model runs under
791 conditions in B, but smoothened using a Gaussian smoothing kernel with standard deviation
792 $(SD) = 2$. Points are values for individual membrane segments. Retrograde flow values within
793 ± 1000 nm/s were plotted, $\geq 94\%$ of values.

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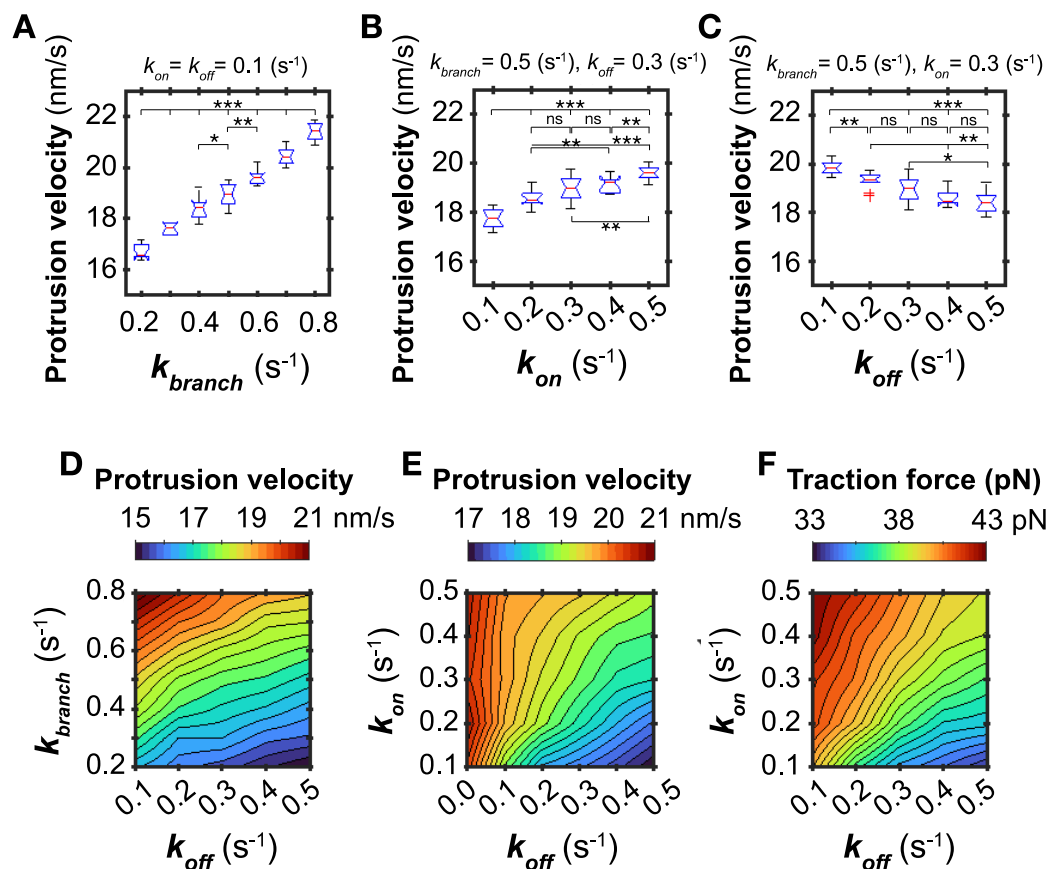
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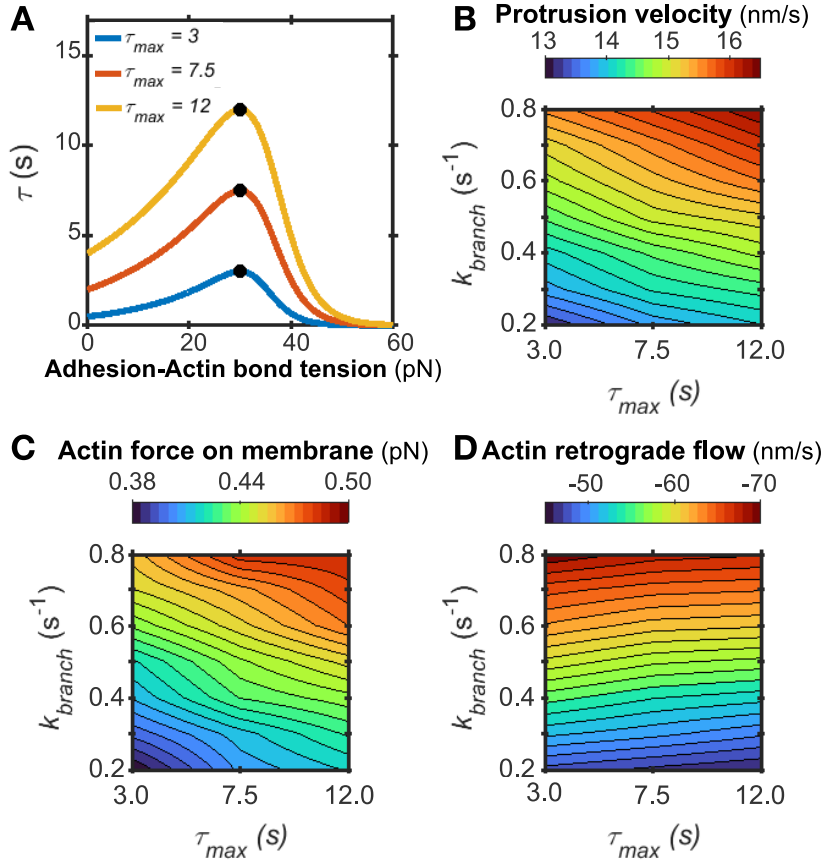
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801 **Figure 3**
802



803
804 **Actin assembly more significantly promotes protrusion velocity than adhesion assembly.**
805 (A-C) Distribution of lamellipodium velocity as a function of actin assembly rate k_{branch} ,
806 adhesion k_{on} and adhesion k_{off} . 10 s simulations with $k_m = 0.3 \text{ pN/nm}$, maximum allowed
807 adhesions = 1000 and periodic boundaries. Box plots' red line is median velocity and notches
808 95% CI, from $n = 10$ simulations. Significance is Mann-Whitney U test of mean. Adhesion
809 density ranged around 500, (A) $493 - 505/\mu\text{m}^2$, (B) $246 - 626/\mu\text{m}^2$, (C) $758 - 378/\mu\text{m}^2$. (D)
810 Heatmap of mean protrusion velocity that results from variable actin k_{branch} , adhesion $k_{on} = 0.1 \text{ s}^{-1}$
811 $^{-1}$, and variable adhesion k_{off} . (E) Mean protrusion velocity resulting from $k_{branch} = 0.5 \text{ s}^{-1}$ and
812 variable k_{on} and k_{off} . (F) Mean traction force resulting from $k_{branch} = 0.5 \text{ s}^{-1}$ and variable k_{on} and
813 k_{off} . Force computed from identical conditions as in A-E, except simulations were 20 s.

814 **Figure 4**
815



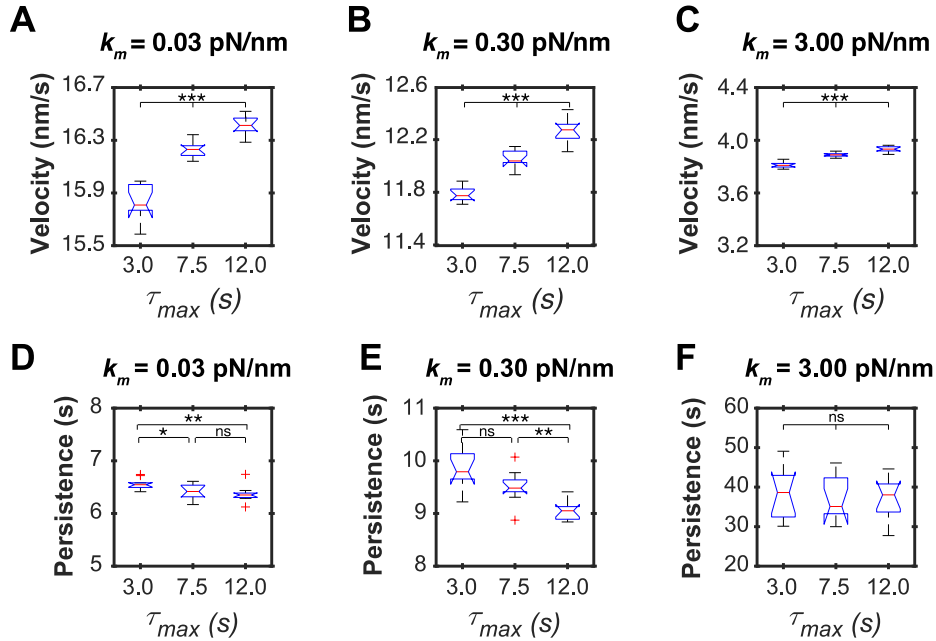
816
817

818 **The molecular clutch mechanism contributes to leading edge motion.** (A) Force-dependent
819 relationship of the molecular clutch: adhesion lifetime (τ) versus adhesion-filament bond tension
820 where $\tau = 1/k_{off}$. Under high tension (50 pN), $k_{off} = 2 \text{ s}^{-1}$ and k_{off} increases exponentially with
821 increased tension. (B-D) Mean protrusion velocity, actin force on membrane, and actin
822 retrograde flow velocity that results from variations in τ_{max} and k_{branch} . 10 s simulations with $k_m =$
823 0.3 pN/nm, $k_{on} = 1.0 \text{ s}^{-1}$, molecular clutch engaged with $\tau_{max} = 3.0, 7.5,$ and 12.0 s with
824 intermediate values interpolated, maximum allowed adhesions = 2000, boundaries fixed, $n = 10$.
825 Because inactivated adhesions are removed from the modeling domain, k_{on} and the number of
826 allowed adhesions were increased to obtain 500 adhesions/ μm^2 [77]. Membrane force calculated

827 as the mean membrane spring tension for all membrane springs and all time points. All flow
828 velocities are plotted.

829

830 **Figure 5**



831

832 **Adhesion lifetime promotes lamellipodia velocity but inhibits persistence.** Model

833 simulations in which membrane tension and molecular clutch τ_{max} varied, $k_{branch} = 0.5$ s⁻¹, $k_{on} =$

834 1.0 s⁻¹, boundaries fixed, 2 min run time. (A-C) Mean velocity measurements of the middle

835 micron region of the membrane for each τ_{max} and each membrane tension. (D-F) Persistence

836 measurements of the middle micron region of the membrane versus τ_{max} for each membrane

837 tension. Persistence defined as the time between minimums in membrane segment velocities

838 with minimums ≥ 5 nm/s. Box plots with red line marking medians and notches 95% CI.

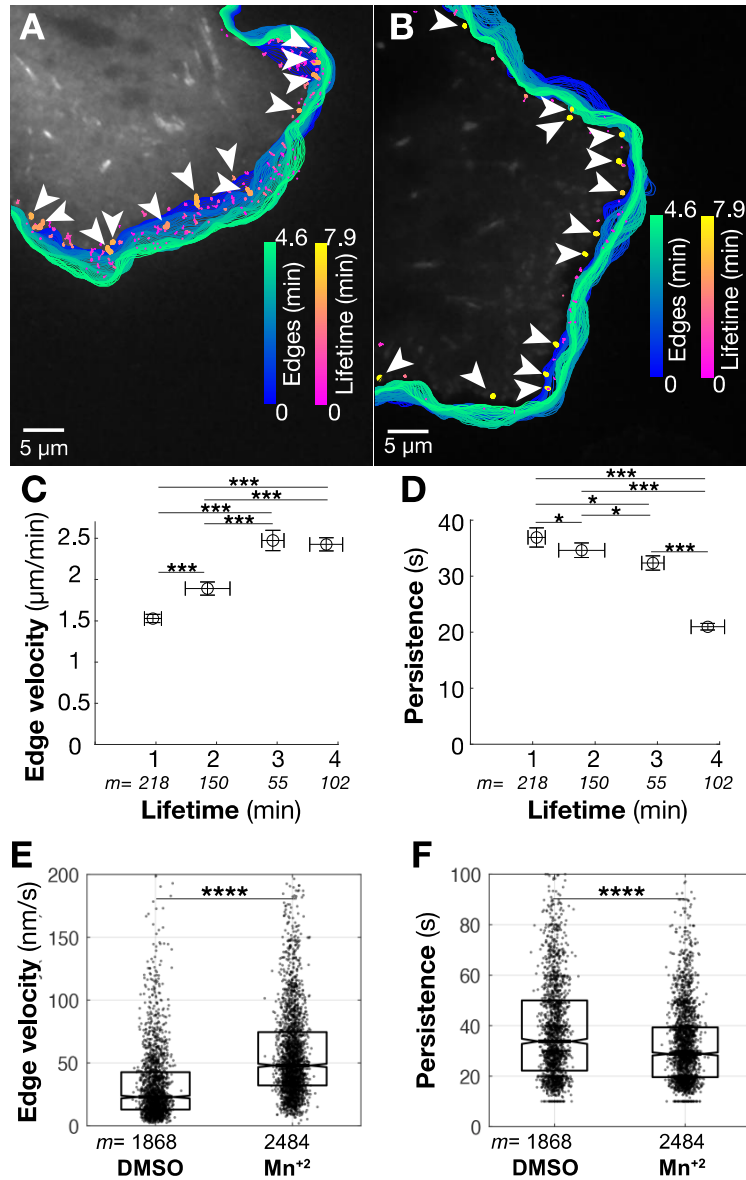
839 Significance is Mann-Whitney U test of means from $n = 10$ simulations.

840

841

842

843 **Figure 6**



844

845 **Longer adhesion lifetime is associated with larger edge velocity and shorter persistence.**

846 (A, B) Tracked adhesions and segmented cell edges of COS7 cells with shorter lifetime (A) and

847 longer lifetime (B). Adhesions and cell edges are color-coded for lifetime and frame with $\Delta t = 3$

848 s, respectively. White arrowheads depict longer-living adhesions per each cell movie. (C) and

849 (D) Error bar plots of velocity (C) and persistent time (D) of edge protrusion in cells with

850 different overall lifetime. Error bar: standard error of mean. * $p < 0.05$, *** $p < 10^{-15}$. p value

851 from Man-Whitney's U test. **(E, F)** Distribution of protrusion velocity (E) and persistence (F),
852 from m significant protrusion events in $n = 7$ cells treated with DMSO and $n = 8$ cells with
853 Mn^{+2} . Boxes span the 25th to 75th percentile. The central horizontal line is median and notches
854 are 95% CI. p
855 value from Kolmogorov–Smirnov test.
856

857 **Table 1. List of model parameters**

Model parameter name	Symbol	Default value	Reference
Time step	dt	$0.001 s$	858 859
Actin Filaments			
Polymerization rate (barbed end)	k_{polym}	$13 s^{-1}$	[5, 860]
Depolymerization rate (pointed end)	$k_{depolym}$	$12 s^{-1}$	[79]
Branching rate (barbed end)	k_{branch}	$0.5 s^{-1}$	[43]
Capping rate (barbed end)	k_{cap}	$0.6 s^{-1}$	[80]
Filament force vector magnitude		$1 pN$	[81, 82]
Gamma (drag coefficient)	γ_F	$\sim 0.01 pN s/nm$	
Filament mass threshold		$9000 units$	[5] [17, 60, 83, 84]
Average filament starting length		$225 nm$	
Filament unit length		$15 nm$	
Branch window height		$15 nm$	
Mean filament branch angle		$70 degrees$	[85-87]
Filament branch angle normal distribution SD		$10 degrees$	
Membrane			
Membrane spring constant	k_m	$0.3 pN/nm$	[41, 42]
Boundary force spring constant	k_b	$10 pN/nm$	
Gamma (drag coefficient)	γ_M	$0.1 pN s/nm$	
Membrane spring equilibrium length	$r_{0,M}$	$2 nm$	
Boundary spring equilibrium length	$r_{0,B}$	$0 nm$	
Membrane-filament contact region width		$15 nm$	
Segment width		$18 nm$	
Membrane length (at initialization)		$2000 nm$	
Adhesions			
Activation rate	k_{on}	$0.1-0.5 s^{-1}$	[31]
Deactivation rate	k_{off}	$0.1-0.5 s^{-1}$	[88]
Adhesion-filament spring constant	k_a	$10 pN/nm$	[24, 32, 74]
Adhesion-filament spring equilibrium length	$r_{0,A}$	$2 nm$	[89]
Filament connection threshold	r_{thresh}	$15 nm$	