





Colored Isosurfaces









Colormapped slices

Properties of Isocontours

- Preimage of scalar value
 - Concept generalizes to any dimension
 - Manifolds of codimension 1
- Closed (except at boundaries)
- Nested–different values don't cross
 - Can consider the zero-set case (generalizes)
 - F(x, y) = k < -> F(x, y) k = 0
- Normals given by gradient vector of F





Contours in 2D

 Assign gometric primitives to "cells" consisting of 2x2 grid points

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 - Signs of the values of corners of cells
- How do we know the position of the primitives?
 - Interpolate along grid points



Questions

- How many grid lines with crossings can there be?
- What are the different configurations (adjacencies) of +/- grid points?

Cases							
Case	Polarity	Rotation	Total				
No Crossings	x2		2				
Singlet	x2	x4	8	(x2 for polarify)			
Double adjacent	x2	x2 (4)	4				
Double Opposite	x2	x1 (2)	2				
			16 = 2 ⁴				

Ambiguities Right or wrong? 								
	144 - 444 -							

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Isosurfacing

- You're given a big 3D block of numbers
- Make a picture
- Slicing shows data, but not its 3D shape
- Isosurfacing is one of the simplest ways



A little math

- Dataset: v = f(x,y,z)
- f: R³ |-> R
- Want to find $S_v = \{(x,y,z) | f(x,y,z) = v\}$
- · All the locations where the value of f is v
- S_v: isosurface of f at v
 - In 2D: isocontours (some path)
 - In 3D: isosurface
- Why is this useful?

Surface Extraction (Isosurfacing)

- Surface Extraction
 - SLICING Take a slice through the 3D volume (often orthogonal to one of the axes), reducing it to a 2D problem
 - Contour in 2D
 - Form polygons with adjacent polylines

Note analogous techniques in 2D visualization: 1D cross-sections, and contours (=isolines)





Data Enrichment - Nearest Neighbour Interpolation





f000

f100



7



Lobster - Increasing the Threshold Level















Isosurface Construction

- One can work through all 256 cases in this way although it quickly becomes apparent that many cases are similar.
- For example:
 - -2 cases where all are positive, or all negative, give no isosurface
 - 16 cases where one vertex has opposite sign from all the rest
- In fact, there are only 15 topologically distinct configurations

Canonical Cases for Isosurfacing

The 256 possible configurations can be grouped into these 15 canonical cases on the basis of complementarity (swapping positive and negative) and rotational symmetry

The advantage of doing this is for ease of implementation - we just need to code 15 cases not 256



















Case 14

Isosurface Construction

- In some configurations, just one triangle forms the isosurface
- In other configurations ...
 - -...there can be several triangles
 - -...or a polygon with 4, 5 or 6 points which can be triangulated
- A software implementation will have separate code for each configuration