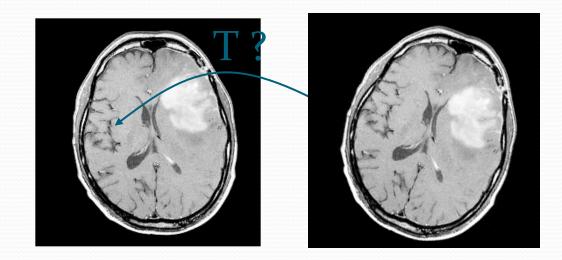
Registration - I Shashidhar Reddy Puchakayala (Shashi)

Apr 15, 2010



- What is registration?
- Why registration ?



Formulation of problem

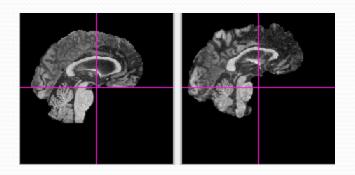
Find feasible transformations φ ,

$$\varphi \in \prod_{1}^{d} (\mathbb{R}^{d})$$
, such that $D[\varphi] = min$

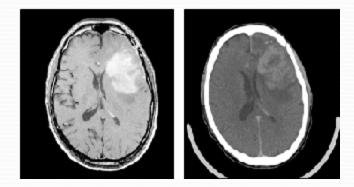
 $D[R,T;\varphi] = D[R,To\varphi]$

Distance Measures?

- Uni Modality
 - Intensity based.
 - Correlation



- Multi Modality
 - Mutual Information and joint Entropy
 - Maximum Likelihood
 - Kullback-Leibler Divergence



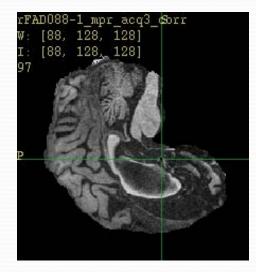
Intensity Based

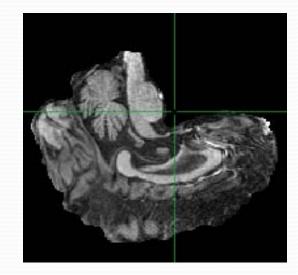
Minimisation of squared differences

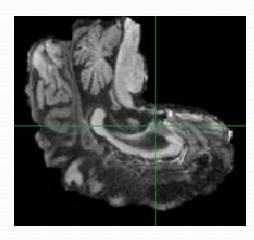
$$D^{SSD}[R,T] \coloneqq \frac{1}{2} ||T - R||_{L_2}^2$$
$$\frac{1}{2} \int_{\mathbb{R}^d} (T(x) - R(x))^2 dx$$

 $D^{SSD}[R,T;\varphi] = D^{SSD}[R,To\varphi]$

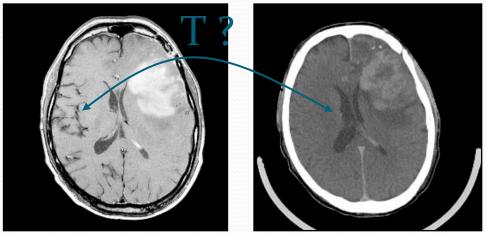
Results

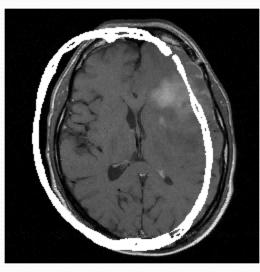






Mutual Information





2-D Histogram

• How does a 2-D histogram of two same images look like ?

Image 1

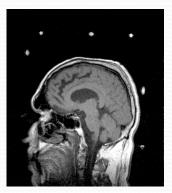
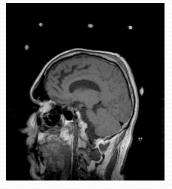


Image 2

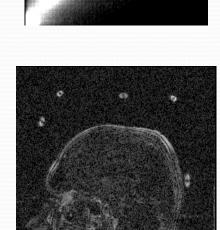


sagittal slices 256 x 256 x 9 1.2 x 1.2 x 4mm

Registration compensates for different head position at acquisition.

unregistered





registered

Histogram

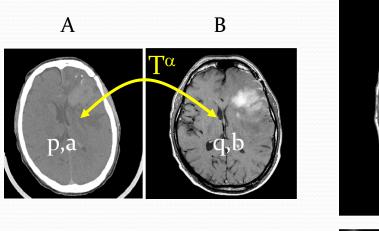
Difference image

Histogram dispersion

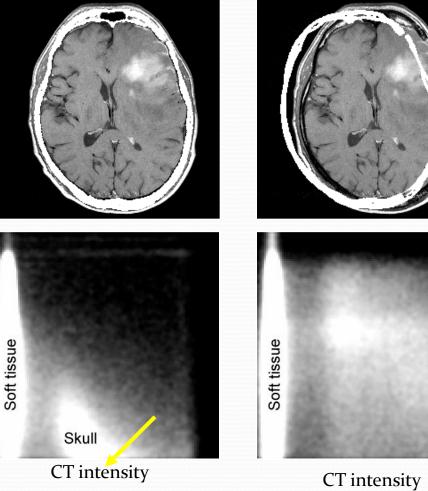
2-D histogram

MR

intensity

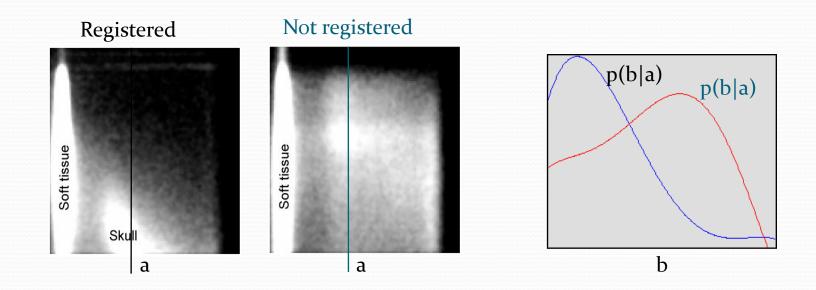


Registered



Not registered

Registration criterion



the statistical dependence of corresponding voxel intensities is maximal at registration

Maximization ofMaximization ofmutual information of A and B, respectively $H_A(\alpha), H_B(\alpha)$ marginal entropy of A and B, respectively $H_{AB}(\alpha)$ joint entropy of A and B $I_{AB}(\alpha)$ mutual information of A and B

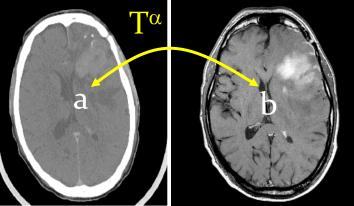
$$I_{AB}(\alpha) = H_A(\alpha) + H_B(\alpha) - H_{AB}(\alpha)$$

"Find as much of the complexity in the separate datatests (maximizing H_A and H_B) such that at the same time they explain each other well (minimizing H_{AB})."

$$I_{AB}(\alpha) = H_A(\alpha) - H_{A|B}(\alpha)$$

"Find as much of the complexity in datatet A (maximizing H_A) while minimizing the residual complexity of A knowing B (minimizing $H_{A|B}$)."

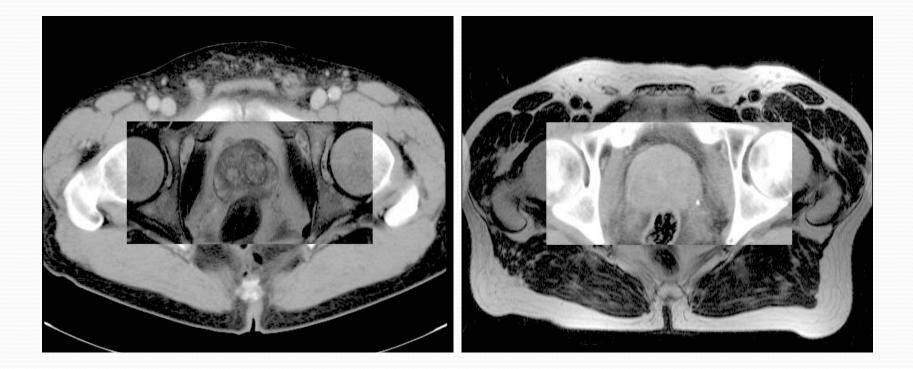
Maximization of mutual information



$$I(A, B) = \sum_{a,b} p_{AB}(a, b) \log_2 \frac{p_{AB}(a, b)}{p_A(a) \cdot p_B(b)}$$

$$\boldsymbol{\alpha}^* = \arg \max_{\boldsymbol{\alpha}} I(A,B)$$

Application Radiotherapy treatment planning of the prostate from CT and MR images (Oyen et al.)





Groups

