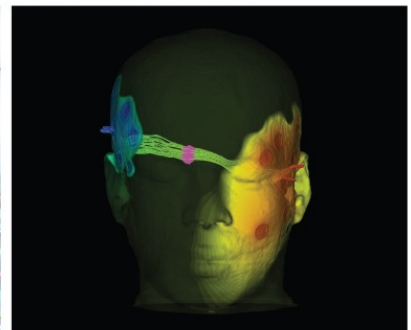
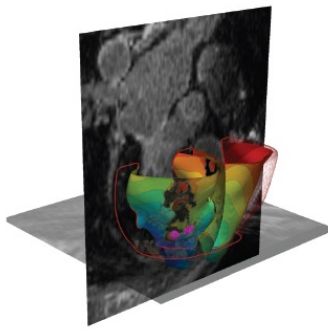
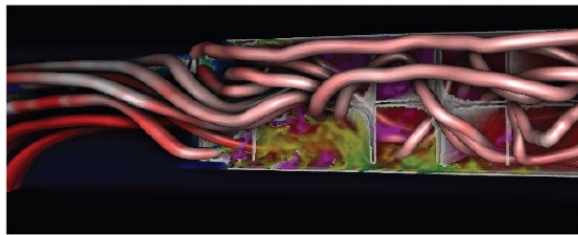
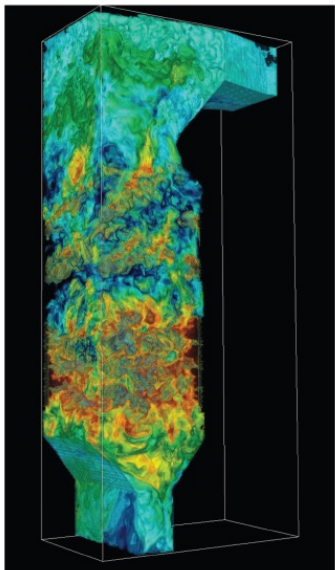
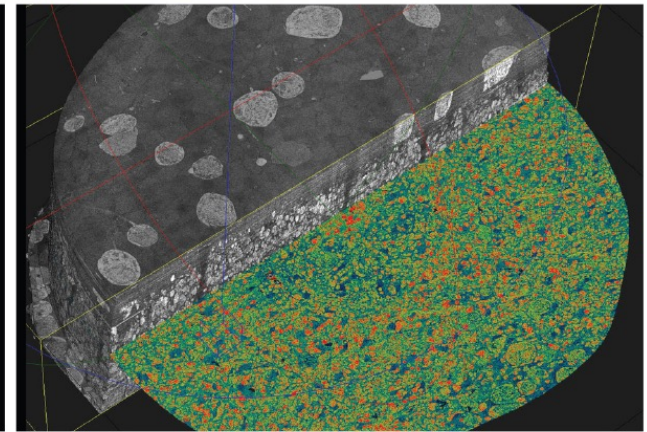
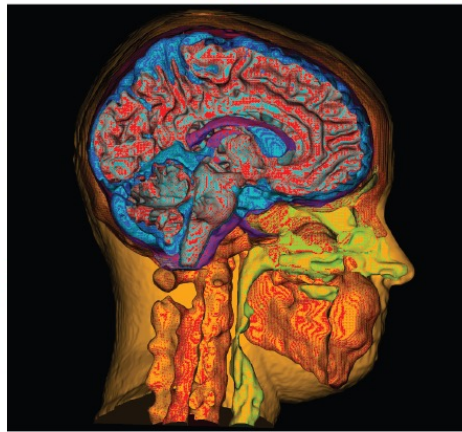
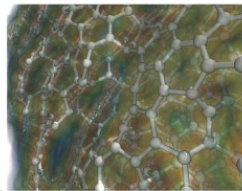
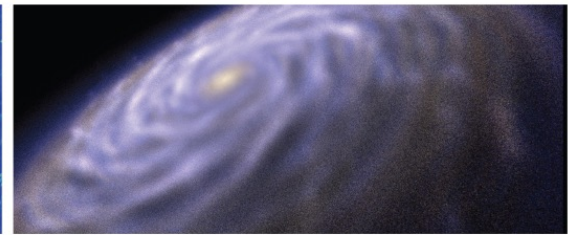
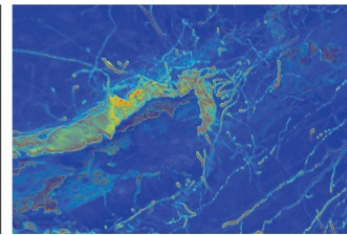
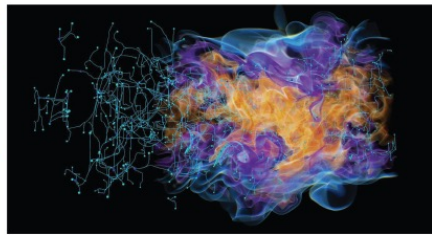


Uncertainty Visualization



Scientific Computing and Imaging (SCI) Institute Faculty



Manish
Parashar



Chris
Johnson



Orly
Alter



Amir
Arzani



Martin
Berzins



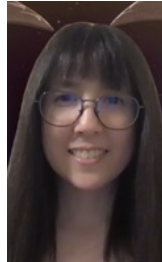
Tamara
Bidone



Shireen
Elhabian



Chuck
Hansen



Kate
Isaacs



Sarang
Joshi



Mike
Kirby



Alex
Lex



Rob
MacLeod



Akil
Narayan



Valerio
Pascucci



Paul
Rosen



Tolga
Tasdizen



Bei
Wang



Bao
Wang



Jeff
Weiss



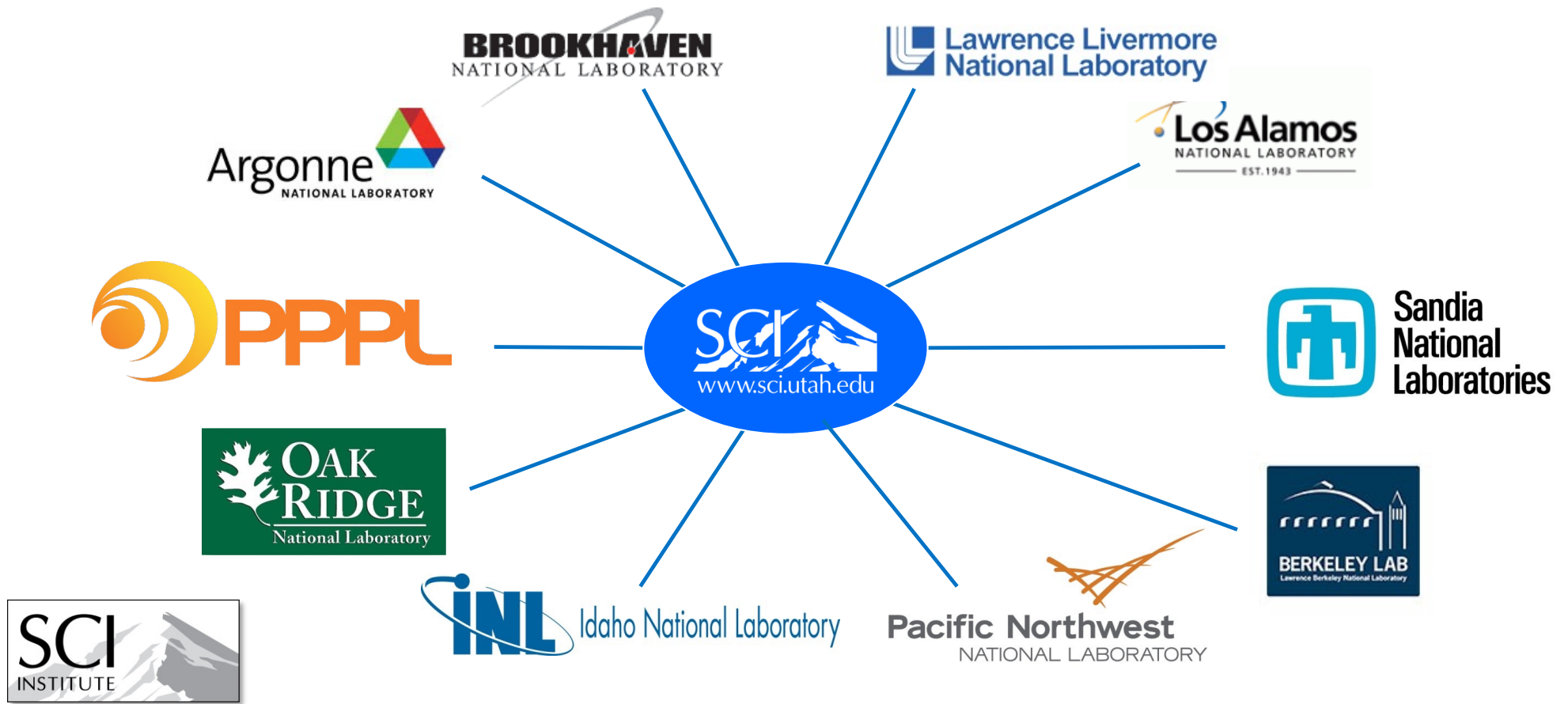
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Whitaker



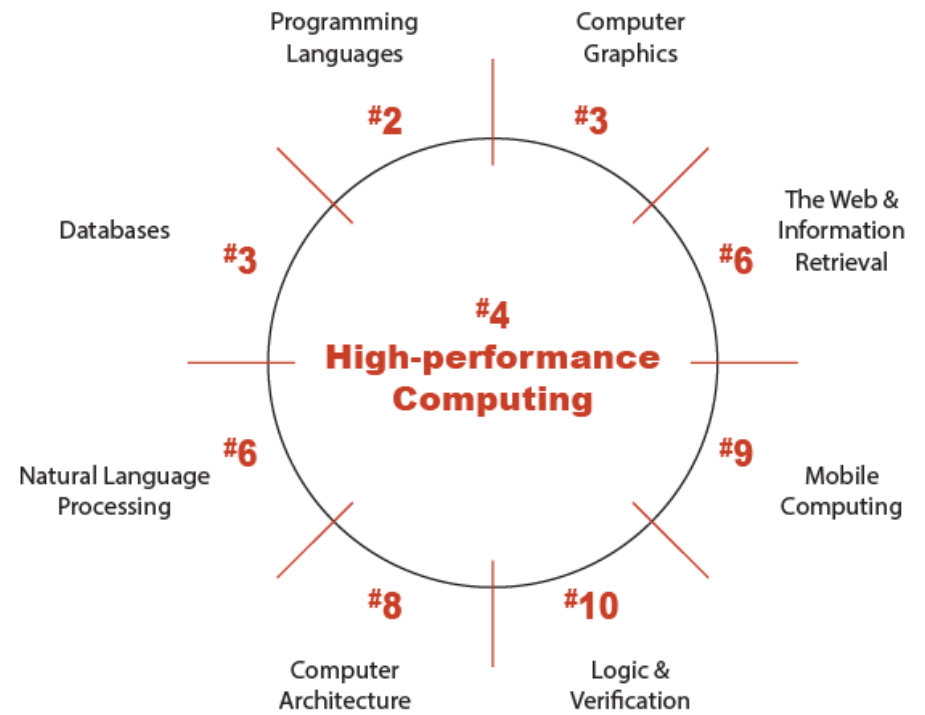
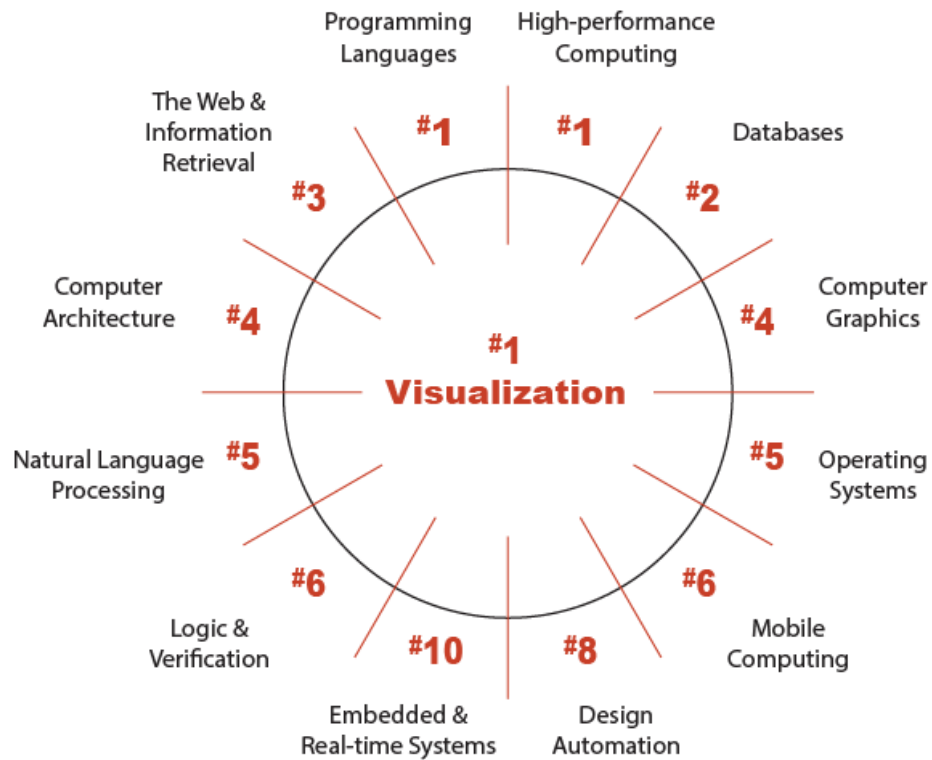
Benjamin
Ellis

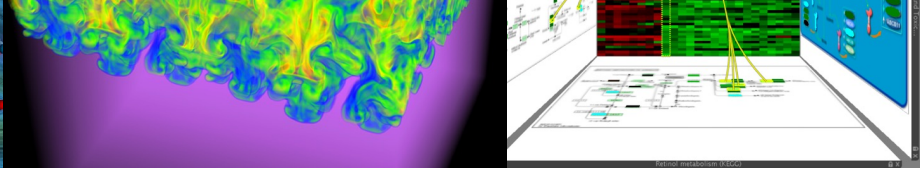
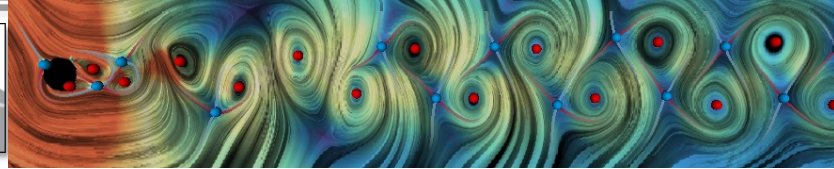
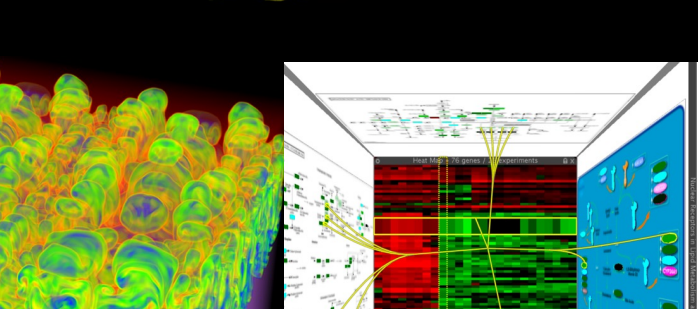
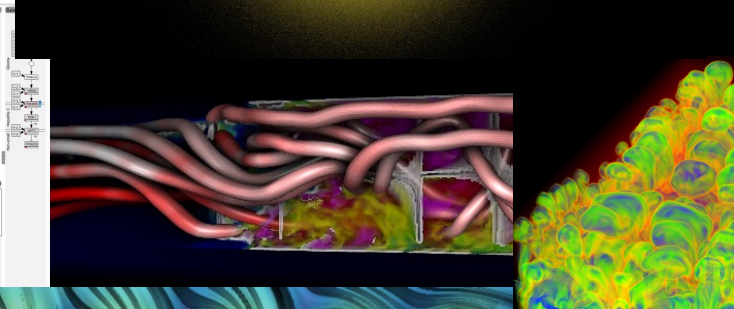
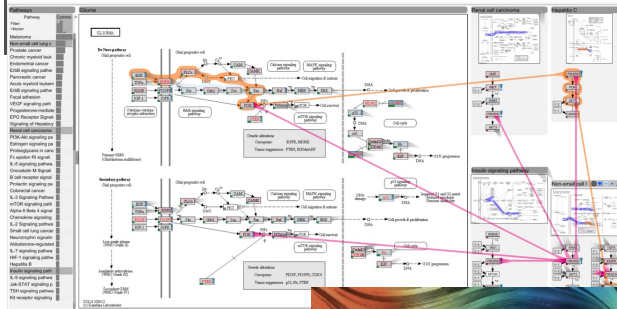
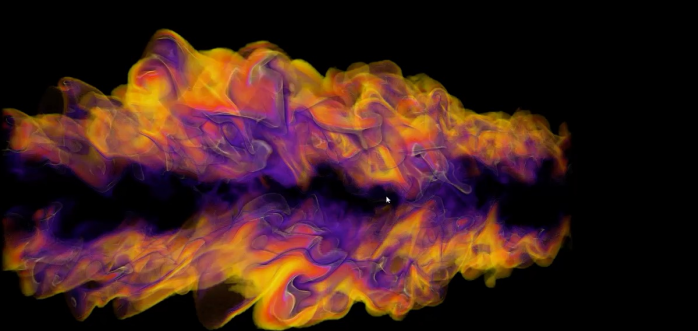
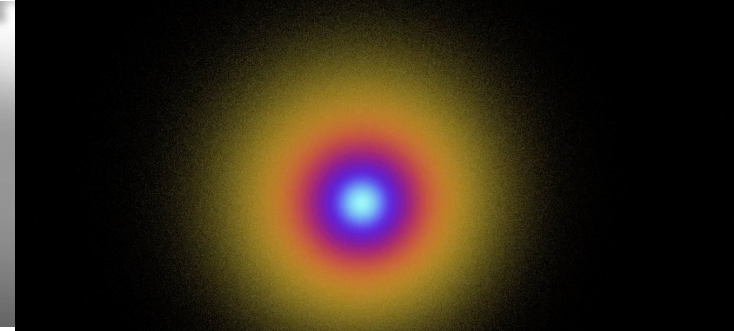
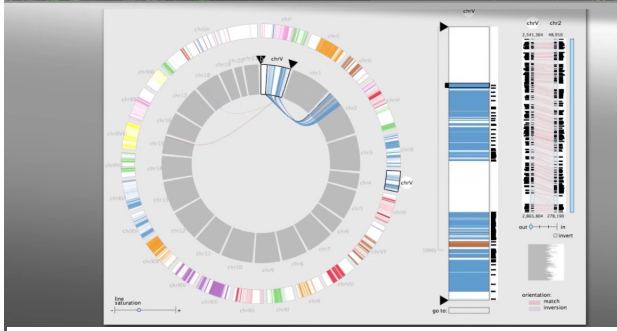
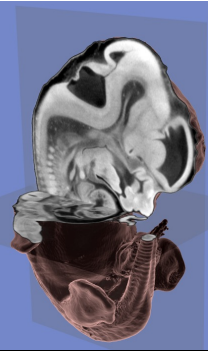
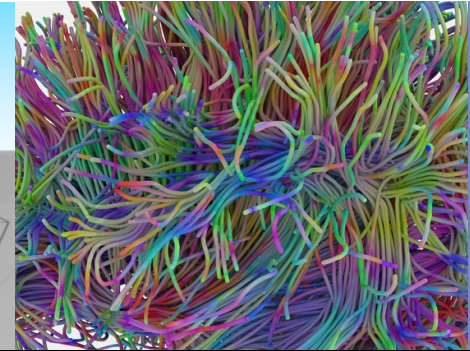
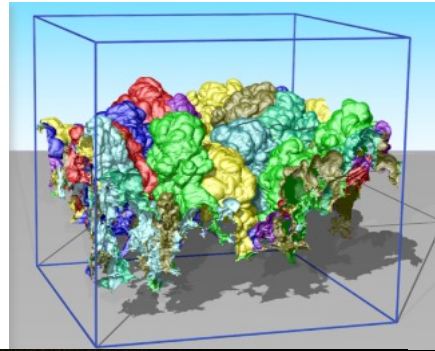
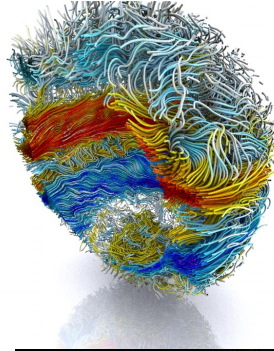
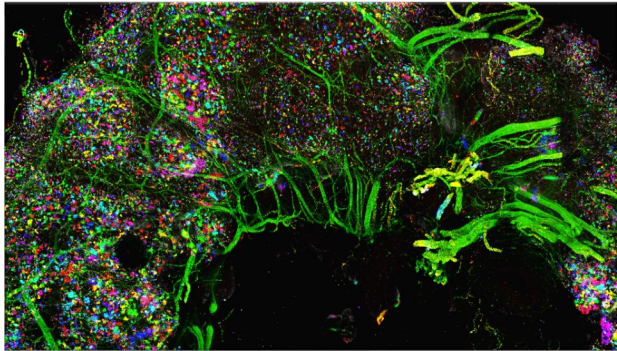


SCI: Collaboration With National Labs



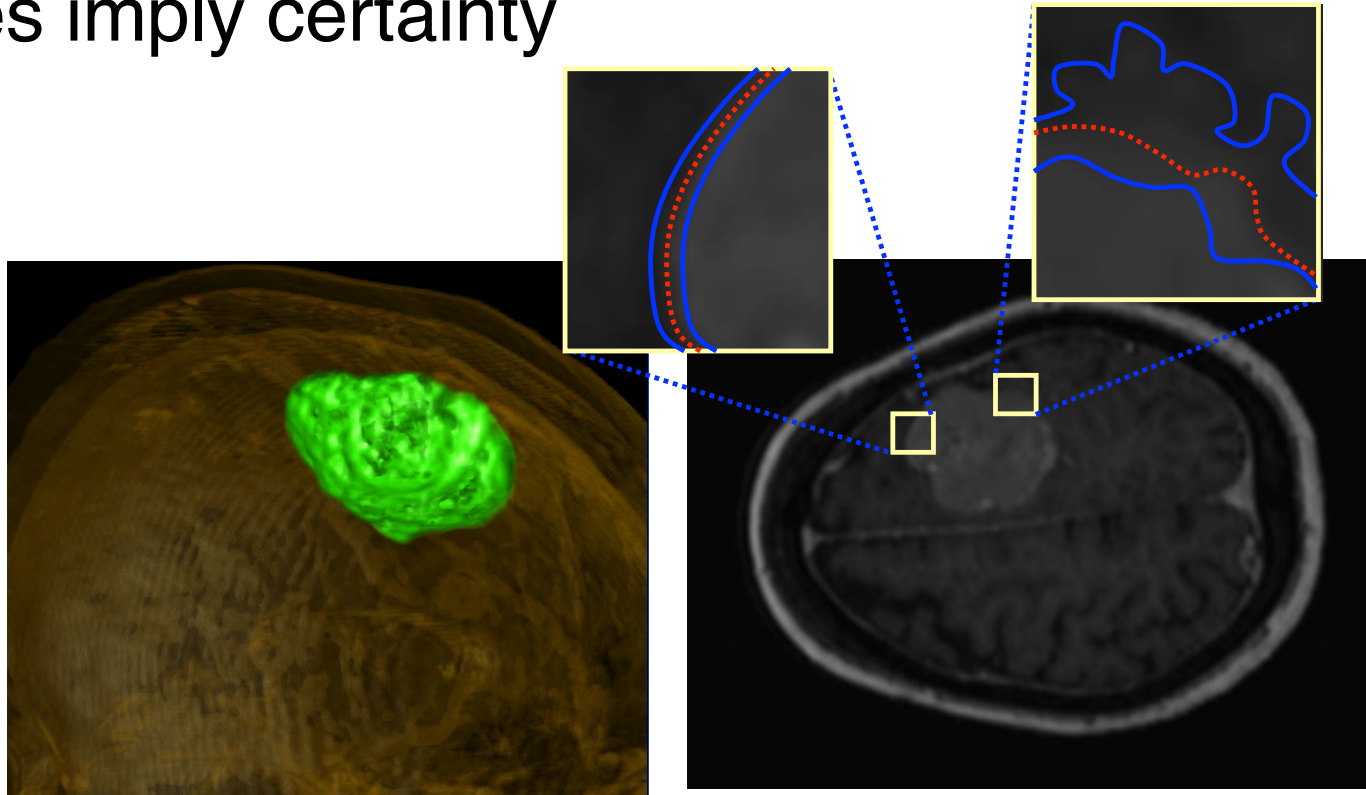
CSRankings.com





Decision Making Under Uncertainty

Surfaces imply certainty



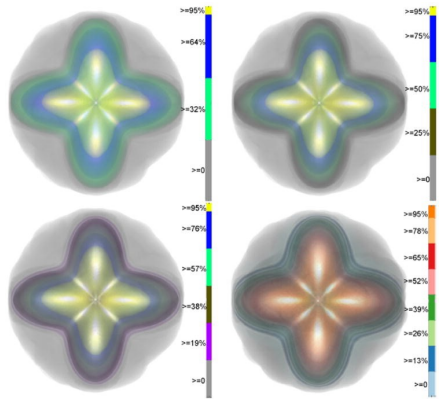
Uncertainty Quotes

- Richard Feynman: *What is not surrounded by uncertainty cannot be the truth.*
- Richard Feynman: *If you thought that science was certain, well, that is just an error on your part.*
- George Box: *All models are wrong. Some models are useful.*
- John W. Tukey: *Far better an approximate answer to the right question, which is often vague, than an exact answer to the wrong question, which can always be made precise.*
- Francis Bacon - If we begin with certainties, we shall end in doubts; but if we begin with doubts, and are patient in them, we shall end in certainties
- Winston Churchill: *True genius resides in the capacity for evaluation of uncertain, hazardous, and conflicting information.*

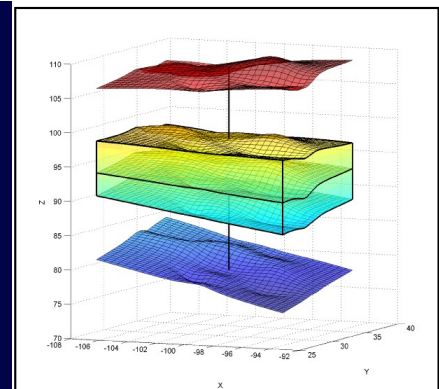
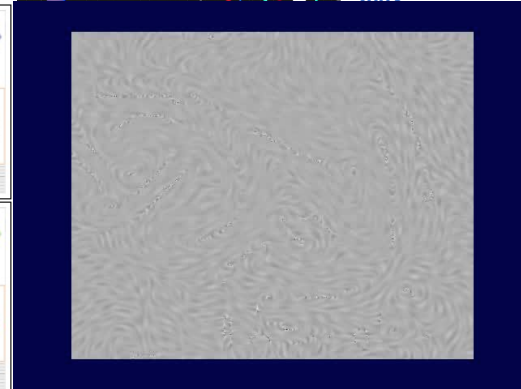
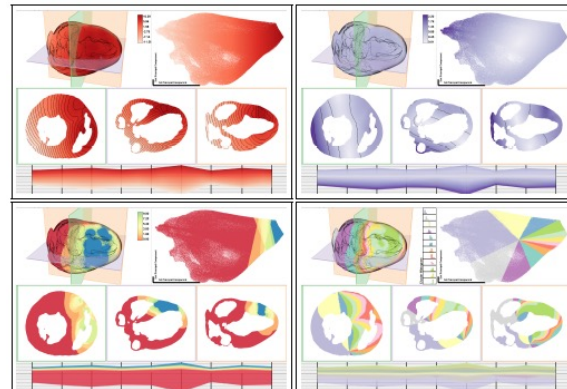
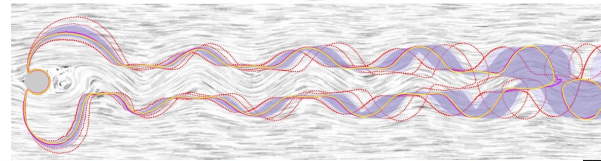
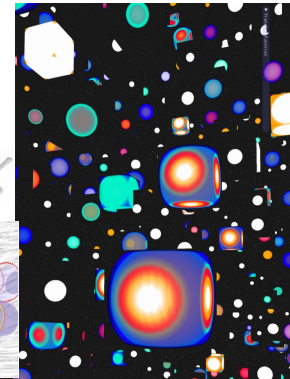
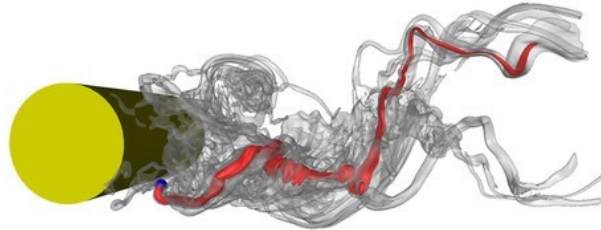


Scientific Computing and Imaging Institute, University of Utah

Uncertainty Visualization



When is the last time you've seen an error bar in a visualization of complex data ?



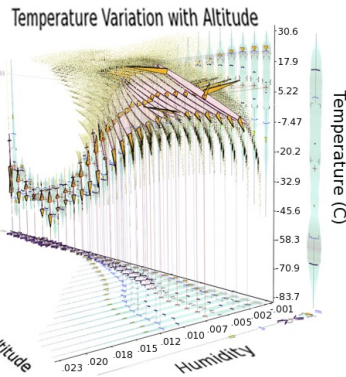
G.P. Bonneau, H.C. Hege, C.R. Johnson, M.M. Oliveira, K. Potter, P. Rheingans, T. Schultz. "Overview and State-of-the-Art of Uncertainty Visualization," In *Scientific Visualization: Uncertainty, Multifield, Biomedical, and Scalable Visualization*, Edited by M. Chen and H. Hagen and C.D. Hansen and C.R. Johnson and A. Kauffman, Springer-Verlag, pp. 3-27. 2014.

M.G. Genton, C.R. Johnson, K. Potter, G. Stenchikov, Y. Sun. "Surface boxplots," In *Stat Journal*, Vol. 3, No. 1, pp. 1-11. 2014.

K. Potter, P. Rosen, C.R. Johnson. "From Quantification to Visualization: A Taxonomy of Uncertainty Visualization Approaches," In *Uncertainty Quantification in Scientific Computing*, IFIP Series, Vol. 377, Springer, pp. 226-249. 2012.

K. Potter, A. Wilson, P.-T. Bremer, D. Williams, C. Doutriaux, V. Pascucci, C.R. Johnson. "Ensemble-Vis: A Framework for the Statistical Visualization of Ensemble Data," In *Proceedings of the 2009 IEEE International Conference on Data Mining Workshops*, pp. 233-240. 2009.

C.R. Johnson, A.R. Sanderson. "A Next Step: Visualizing Errors and Uncertainty," In *IEEE Computer Graphics and Applications*, Vol. 23, No. 5, pp. 6-10. September/October, 2009.



Sources of Uncertainty

- Uncertainty observed in sampled data.
- Uncertainty measures generated by models or simulations.
- Uncertainty introduced by the data processing or visualization processes.

Sources of Uncertainty

- Experimental (observational, equipment limits, multiple trials)
- Numerical (approximation, interpolation, extrapolation)
- Mathematical Model (approximation to true physics/biology)
- Geometric Model (accuracy compared to true geometry)



Categories

ALEATORIC UNCERTAINTY

- *Statistical uncertainty*
- *Unknowns that differ on each run*
- *i.e. throwing dice*

Irreducible: cannot be eliminated through improvements in models or measurements



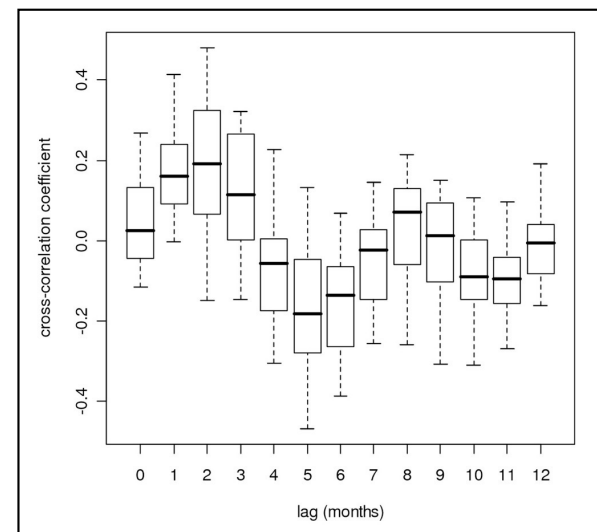
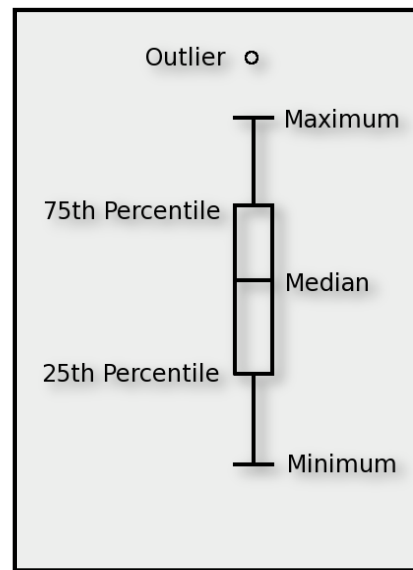
Statistical Uncertainties - Common in Visualization

- Probability Distribution Functions (PDFs) - approximate outcome through a probability function
- Probability Density - continuous random variables, frequency of outcome values
- Statistics on PDFs - mean, median, standard deviation

Traditional Display of Uncertainty

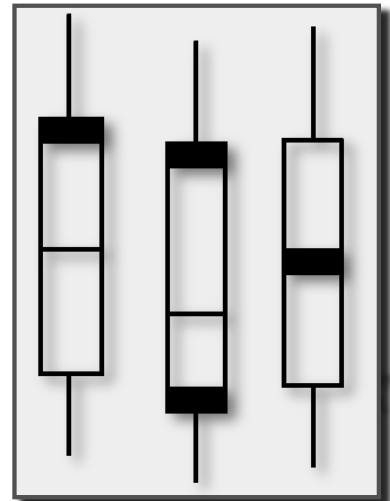
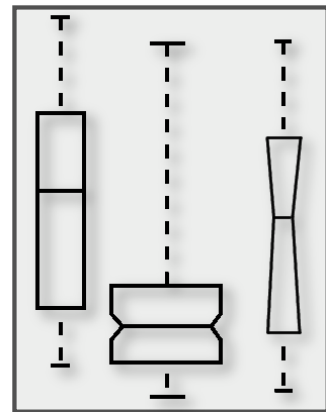
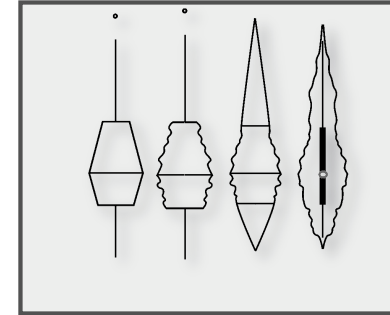
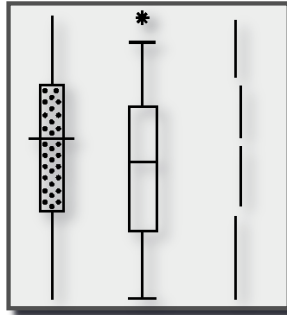
Boxplots (Tukey, 1977)

- Quartile range including median
- Outliers
- Assume Gaussian



Boxplot Modifications

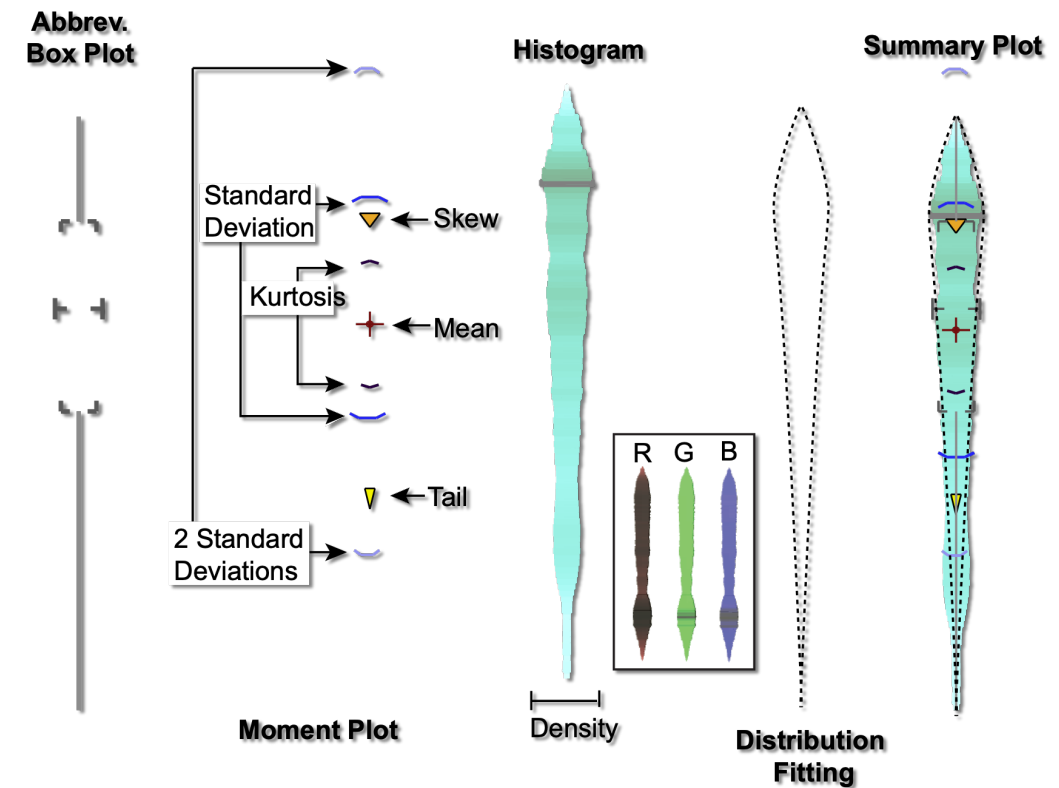
- Visual Modifications
 - Refinement for aesthetic purposes
- Density indications
 - Use the box sides to encode
- Data Characteristics
 - Sample size, confidence levels
- Additional Statistics
 - Skew, modality

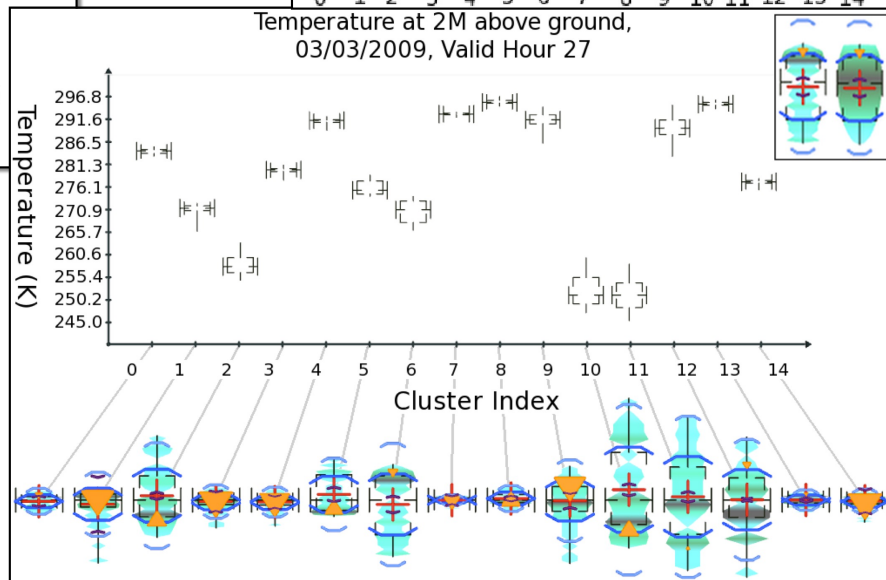
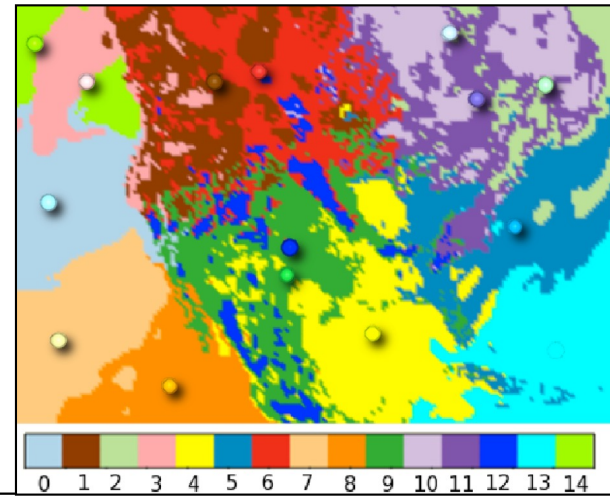
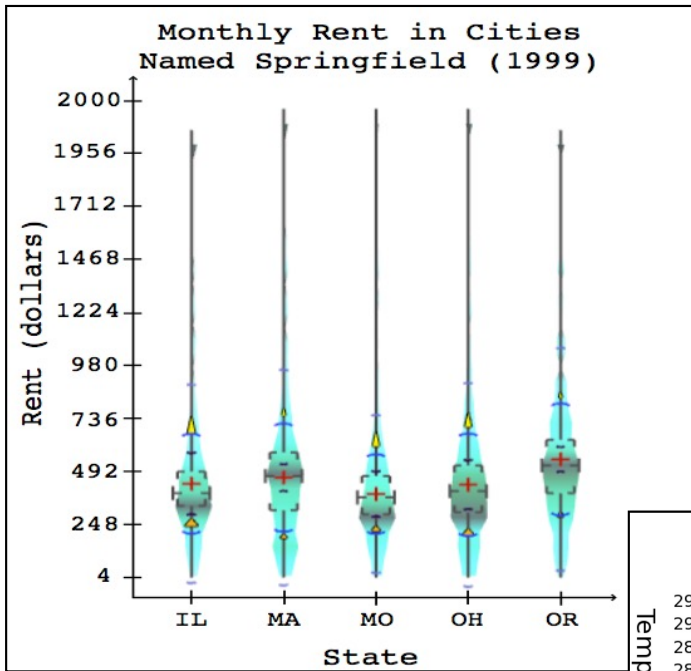


The Summary Plot

- Augment boxplot with numerous display techniques
- Emphasize characteristics other than mean/variance
- Indicate quantity and location of uncertainty

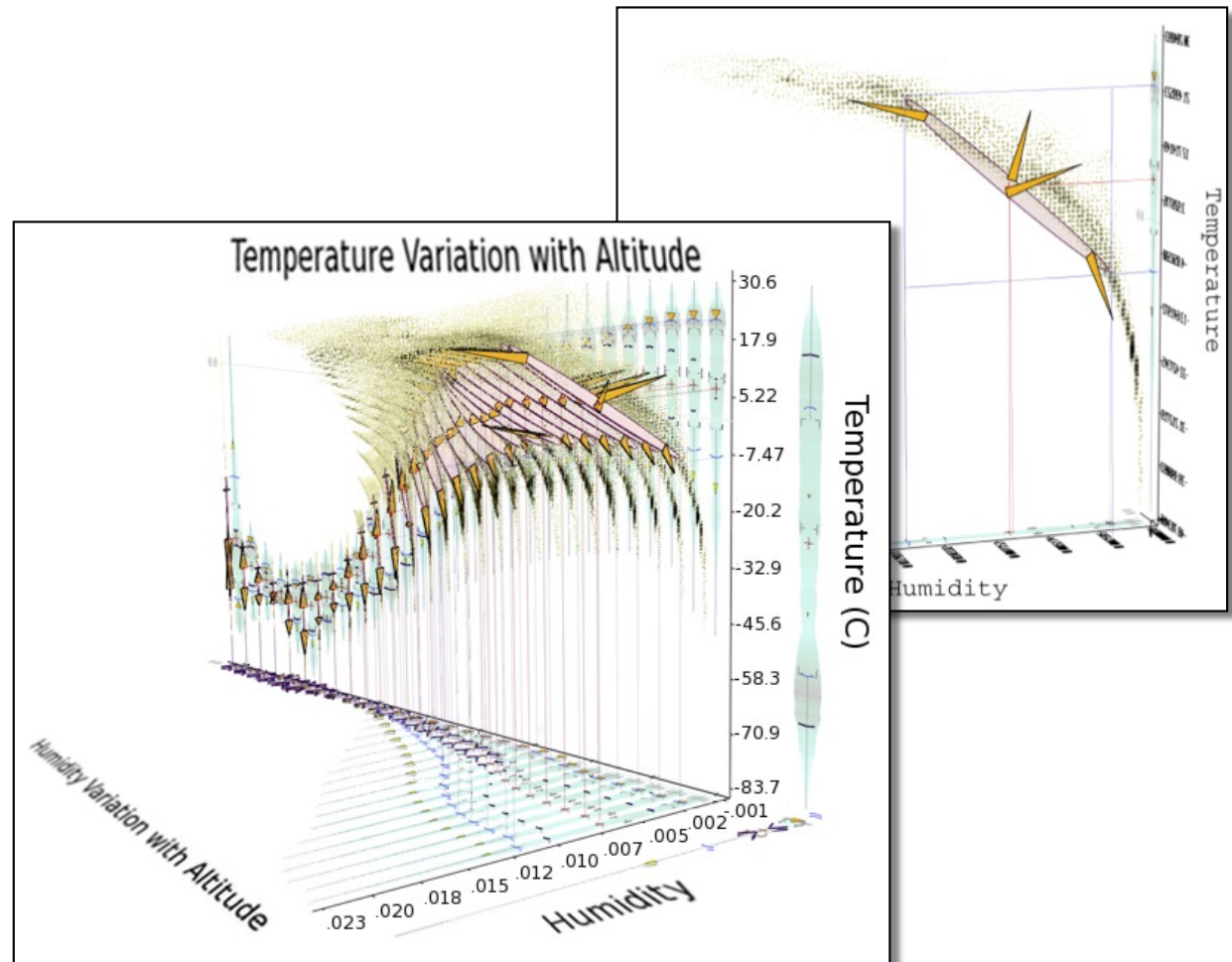
K. Potter, J. Kniss, R. Riesenfeld, C.R. Johnson.
"Visualizing Summary Statistics and Uncertainty".
In Proc Eurovis 2010, 29(3), 2010.





Summary Plot in Higher Dimensions

- Statistics similar to summary plot
- Highlight correlations



K. Potter, J. Kniss, R. Riesenfeld, C.R. Johnson.
"Visualizing Summary Statistics and Uncertainty".
In Proc Eurovis 2010, 29(3), 2010.

Visual Encodings of Temporal Uncertainty

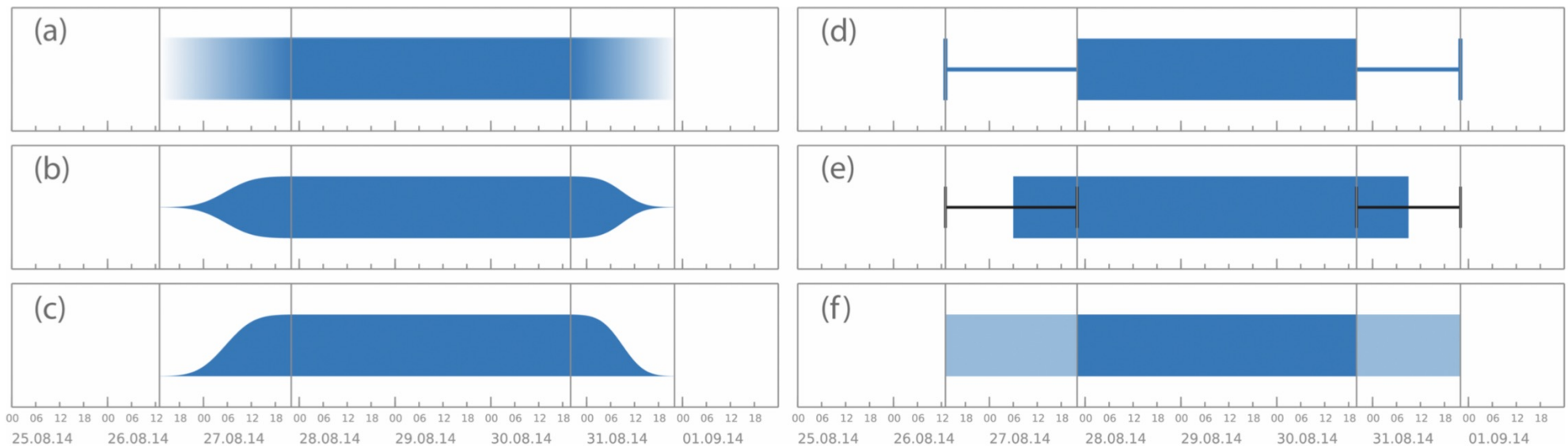
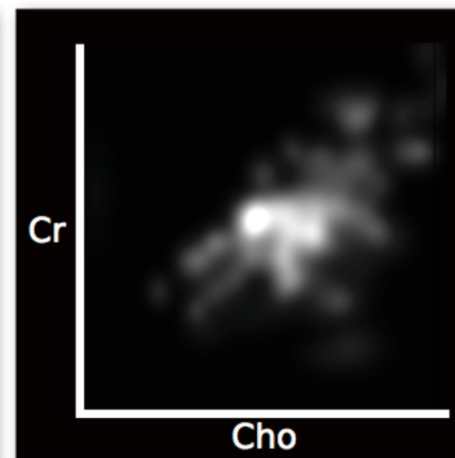
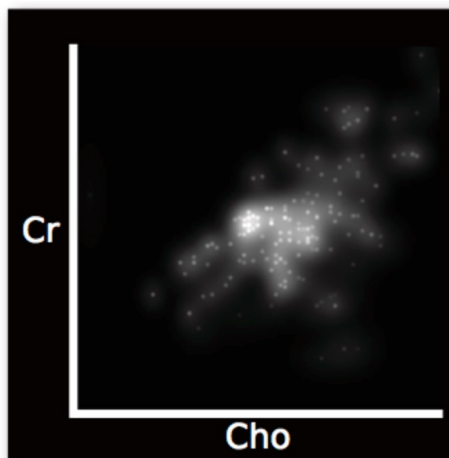
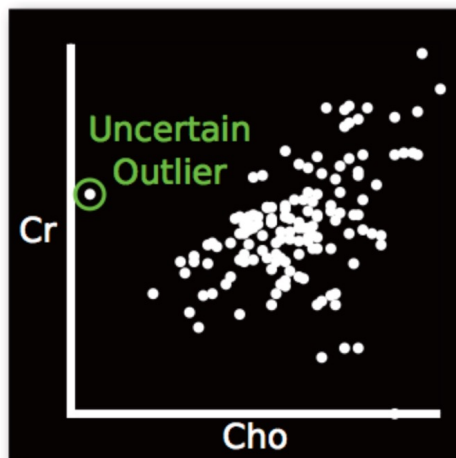
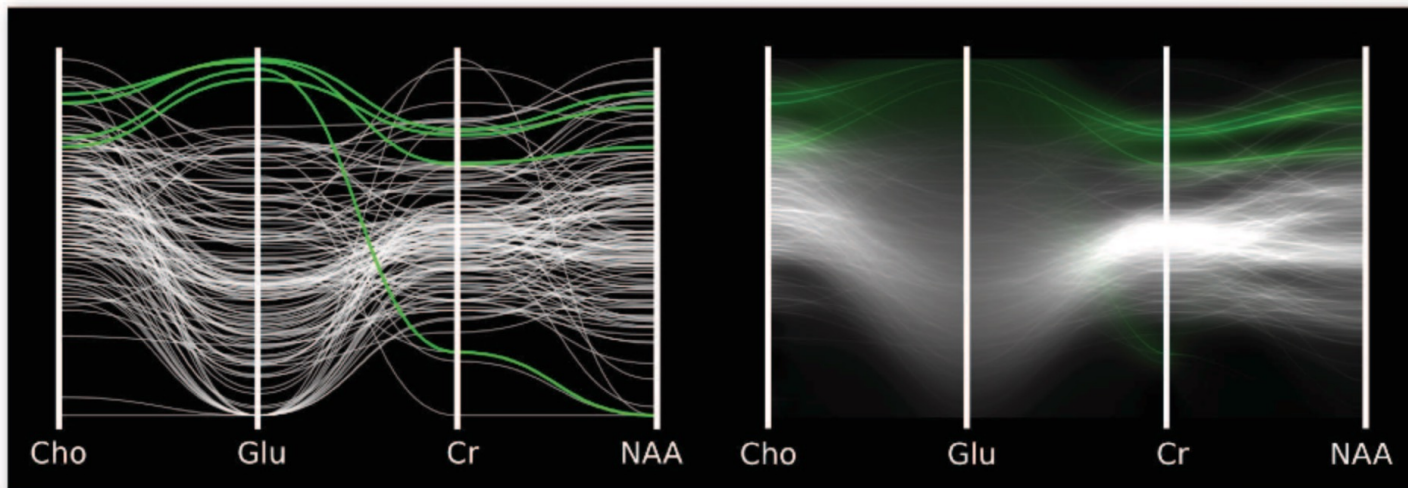


Fig. 1: Six different visual encodings of start/end uncertainty of temporal intervals used in the user study: (a) gradient plot, (b) violin plot, (c) accumulated probability plot, (d) error bars, (e) centered error bars, and (f) ambiguation. We designed encodings (a)–(c) to encode statistical uncertainty and encodings (d)–(f) to encode bounded uncertainty. All encodings were used to estimate earliest start, latest start, earliest end, and latest end, as well as minimum, maximum, and average interval duration. Moreover, encodings (a)–(c) were used to estimate the probability that the interval has already started/ended at a marked position in time.



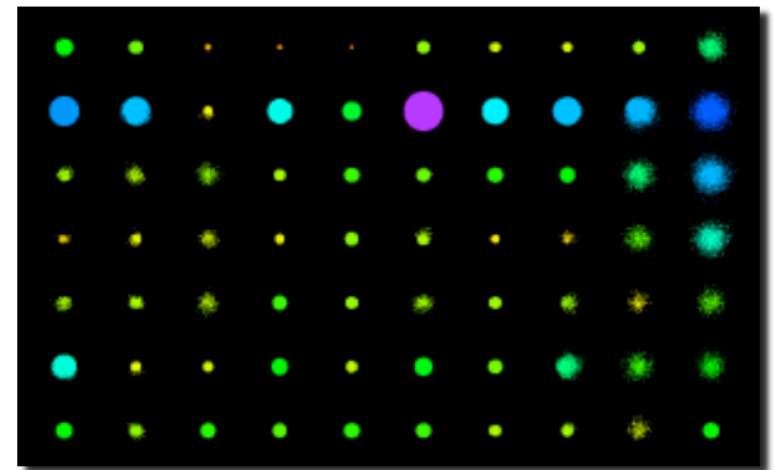
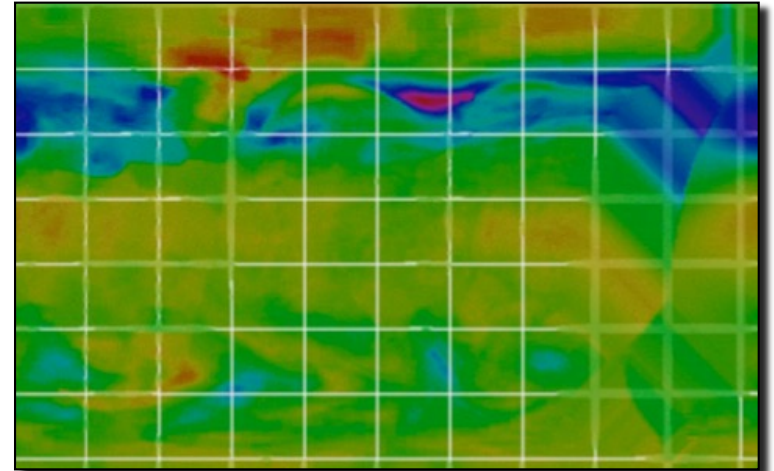
Gschwandtnei, T., Bögl, M., Federico, P., & Miksch, S. (2015). Visual encodings of temporal uncertainty: A comparative user study. *IEEE transactions on visualization and computer graphics*, 22(1), 539-548.



Feng, D., Kwock, L., Lee, Y., & Taylor, R. M., 2nd (2010). Matching visual saliency to confidence in plots of uncertain data. *IEEE transactions on visualization and computer graphics*, 16(6), 980–989. doi:10.1109/TVCG.2010.176

2D Annotation

- Modulate annotation lines or glyphs with uncertainty
- Minimal interference
- Uncertainty not emphasized



A. Cedilnik, P. Rheingans.
Procedural Annotation of Uncertain Information.
In Proc IEEE Vis, 2000.

Visual Entropy

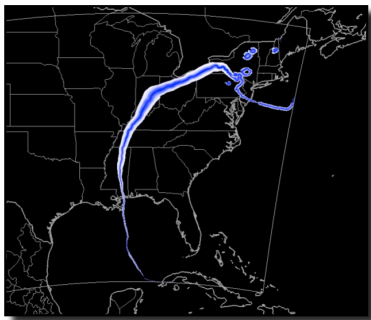
Holliman, N. S., Coltekin, A., Fernstad, S. J., Simpson, M. D., Wilson, K. J., & Woods, A. J. (2019). Visual entropy and the visualization of uncertainty. arXiv preprint arXiv:1907.12879.



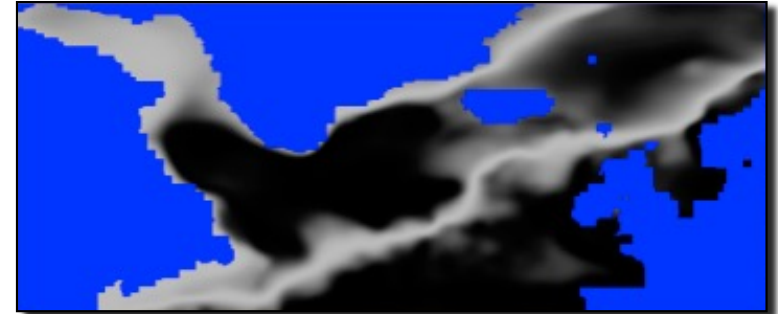
Fig. 10. The urban temperature data visualization showing both hourly mean temperature values using the MetOffice color scale and the variance of those values using our new visual entropy scale, this image is an example of the high uncertainty target-present stimulus used in the experiment described below.

Contouring

- Contours follow the line of a specific data value (ex. terrain map)
- Standard Deviation
- Fuzzy contours
- Graduated contours

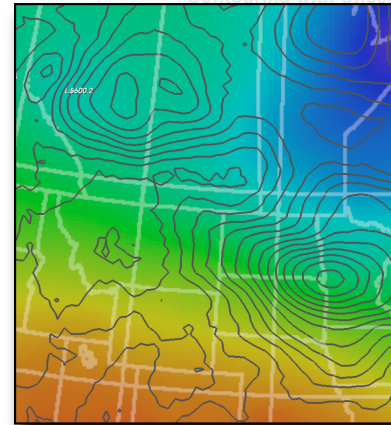


. Sanyal, S. Zhang, J. Dyer, A. Mercer, P. Amburn.
Noodles: A Tool for Visualization of Numerical Weather Model Ensemble Uncertainty
In Proc IEEE Vis, 2010.



R.S. Allendes Osorio, K.W. Brodlie.
Contouring with Uncertainty.
In Theory and Practice of Computer Graphics Conf, 2008

R.S. Allendes Osorio, K.W. Brodlie.
Contouring with Uncertainty.
In Theory and Practice of Computer Graphics Conf, 2008.

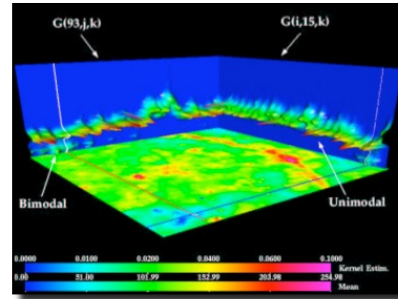


Mean = colormap,
Standard Deviation
= contours

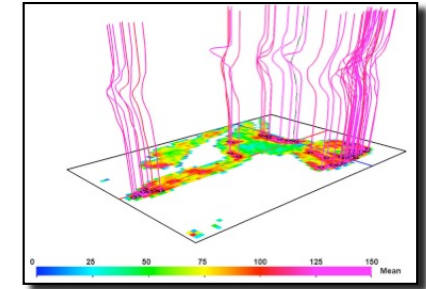
K. Potter, et al.
Ensemble-Vis: A Framework for the Statistical Visualization of Ensemble Data.
In IEEE ICDM Workshop on Knowledge Discovery from Climate Data: Prediction, 2009.

Ensembles / 2D Distributions

- Multi-run/model simulations
- Distribution of data at every point
- Mean/std dev may not be appropriate



D. Kao, A. Luo, J. Dungan, A. Pang.
Visualizing Spatially Varying
Distribution Data.
In Proc Information Visualisation, 2002.

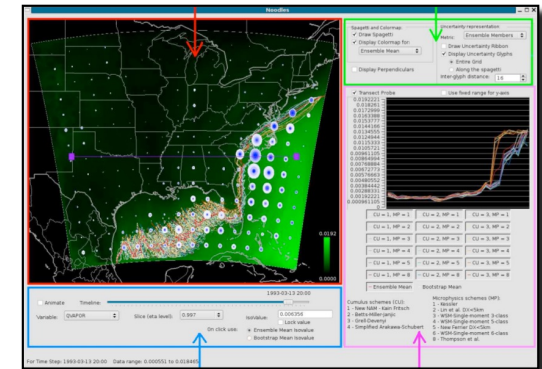
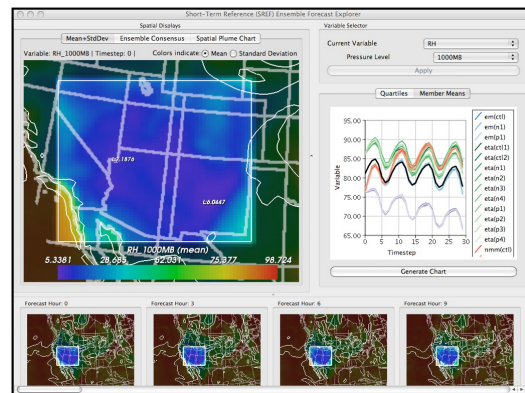


D. Kao, M. Kramer, A. Luo, J. Dungan,
A. Pang.
Visualizing Distributions from Multi-
Return Lidar Data to Understand Forest
Structure.

K. Potter, et al.

Ensemble-Vis: A Framework for the
Statistical Visualization of Ensemble
Data.

In IEEE ICDM Workshop on Knowledge
Discovery from Climate Data:
Prediction, 2009.



. Sanyal, S. Zhang, J. Dyer, A. Mercer, P. Amburn.
Noodles: A Tool for Visualization of Numerical
Weather Model Ensemble Uncertainty
In Proc IEEE Vis, 2010.



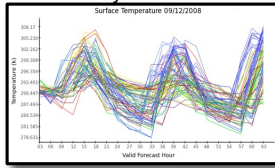
What is ensemble data?

Collection of data sets generated by computational simulations.

Used to simulate complex systems, mitigate uncertainty, unknowns in initial conditions, and parameter sensitivity.

These data sets are:

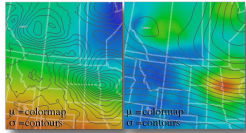
- Multidimensional
- Multivariate
- Multivalued



Ensemble-Vis Workflow

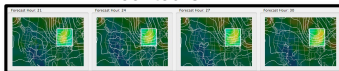
- User-driven
- Component-based

Ensemble Overviews



Spatial Overviews:

Mean and standard deviation encoded through colormaps and contours.

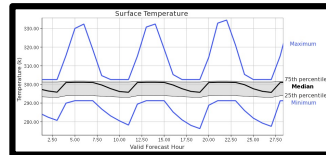


Temporal Overviews:

Filmstrip and animation. Show evolution through time. Small multiples show every time step. User can select desired temporal location.

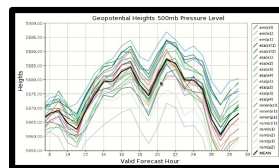
Ensemble-Vis: A Framework for the Statistical Visualization of Ensemble Data

Trend Charts



Quartile Charts:

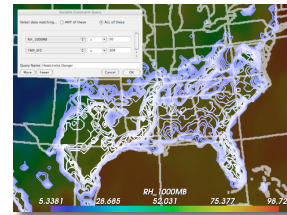
Show minimum and maximum, innerquartile range.



Plume Charts:

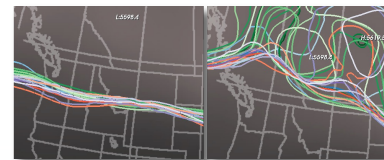
Show every member and mean. Color coded based on model. Deselect members to hide. Drill-down to direct data display.

Query Contours



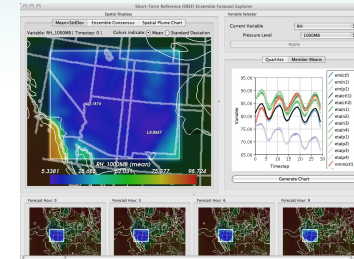
- * User-driven query
- * Select subset based on conditions
- * Returns % of satisfying members
- * Displayed as nested contours

Spaghetti Charts



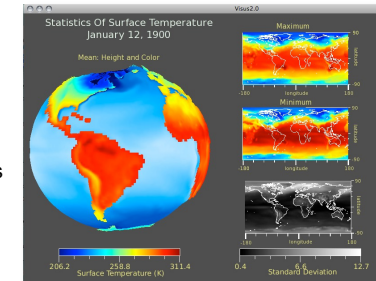
- * Show variation across space
- * User chosen contour value
- * Isocontour for each desired member
- * Highlights outliers and divergence

Implementation



SREF Weather Explorer

- VTK filters, Qt Widgets
- Relational database:
 - MySQL/ Netezza

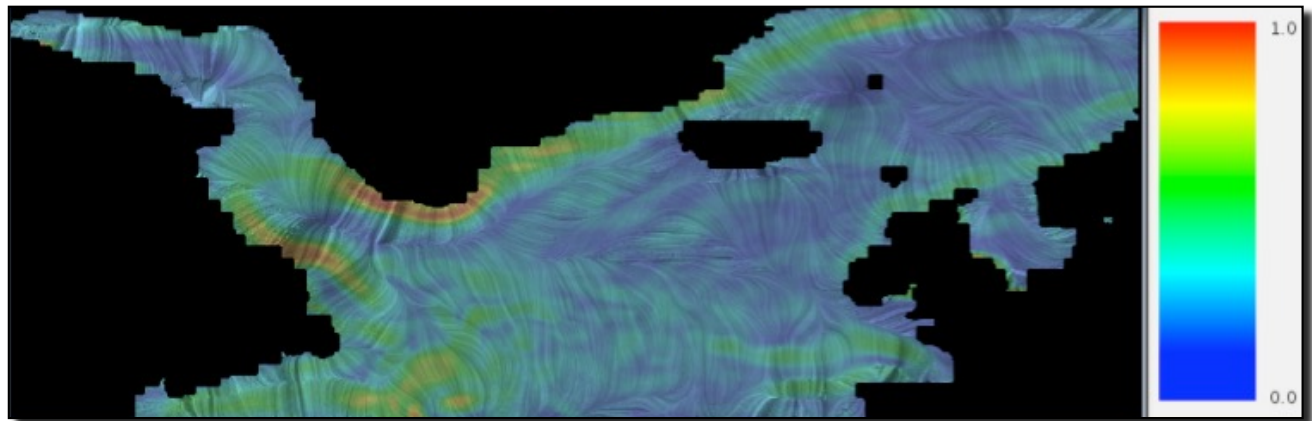


ViSUS

- Climate Data Analysis Tools (CDAT) integration
- C++, python, FLTK
- Out-of-core, streaming

2D Vector Fields - LIC

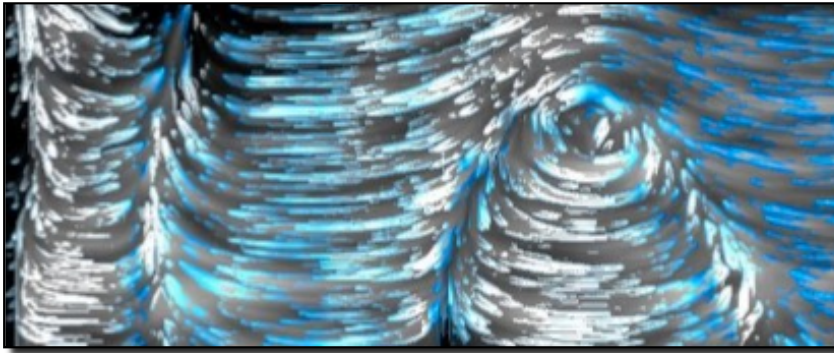
- Line Interval Convolution
- 2D steady flow
- PDF describes the magnitude & direction of each vector in the field
- LIC representation of the gradient field, color encodes magnitude of uncertainty



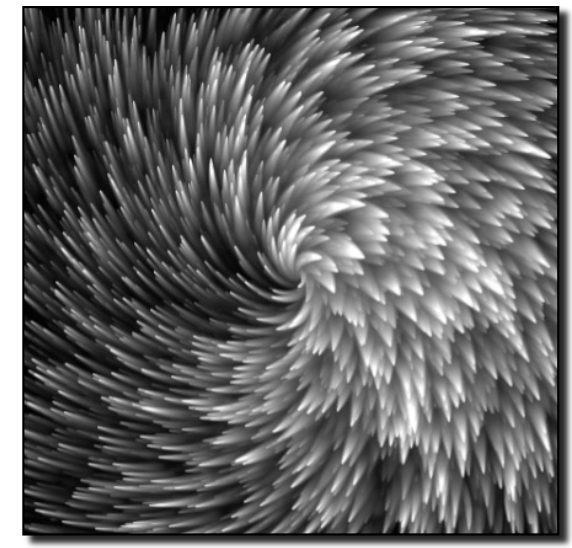
R. S. Allendes Osorio, K. W. Brodlie.
Uncertain Flow Visualization using LIC.
In Theory and Practice of Computer Graphics, 2009.

2D Vector Fields

- Texture-based
- Particle positions along streamlines
- Measuring errors and their influence on position

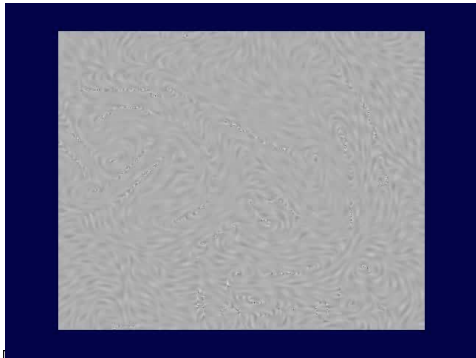
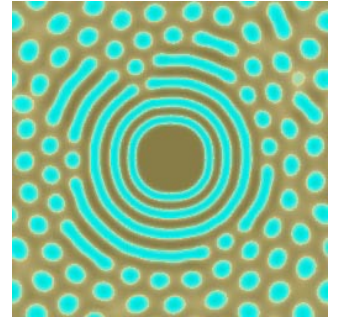
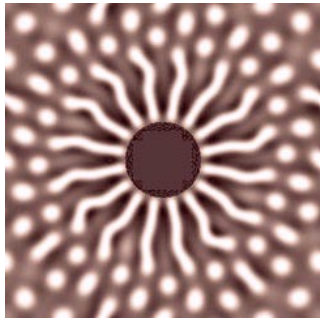


R. Botchen, D. Weiskopf, T. Ertl.
Interactive visualisation of uncertainty in flow fields using texture-based techniques.
In International Symposium on Flow Visualisation, 2006.



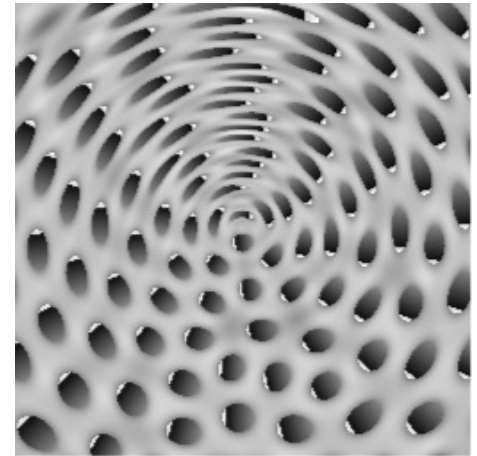
R. Botchen, D. Weiskopf, T. Ertl.
Texture-based visualization of uncertainty in flow fields. In IEEE Vis, 2005.

Reaction Diffusion Vector Field Visualization



A.R. Sanderson, C.R. Johnson, R.M. Kirby. "Display of Vector Fields Using a Reaction Diffusion Model," In Proceeding of IEEE Visualization 2004, pp. 115--122. 2004

A.R. Sanderson, R.M. Kirby, C.R. Johnson, L. Yang. "Advanced Reaction-Diffusion Models for Texture Synthesis," In Journal of Graphics Tools, Vol. 11, No. 3, pp. 47--71. 2006.



Streamlines

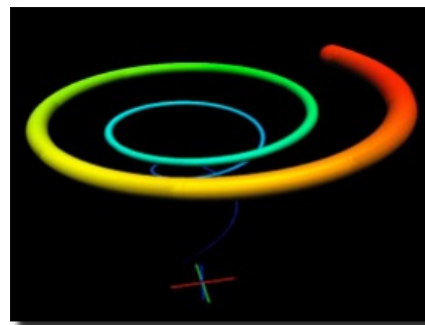
- Uncertainty from numerical algs for particle tracing in fluid flow
- Highlight sensitivity of algorithm choice - particularly near critical pts

S. Lodha, A. Pang, R. Sheehan, C. Wittenbrink.
UFLOW: visualizing uncertainty in fluid flow.
In Proc IEEE Vis, 1996.

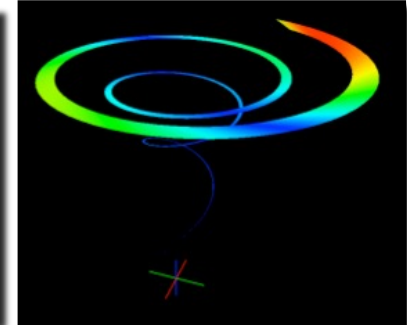
S. Lodha, C. Wilson, R. Sheehan.
"LISTEN: sounding uncertainty visualization".
In Proceedings Visualization '96, pp. 189--195,
1996



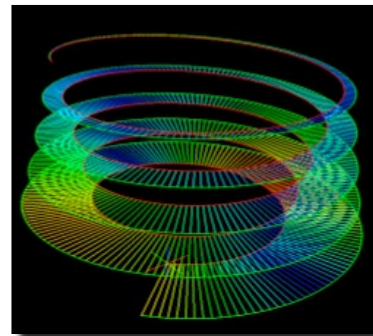
Differences between 2 streamlines



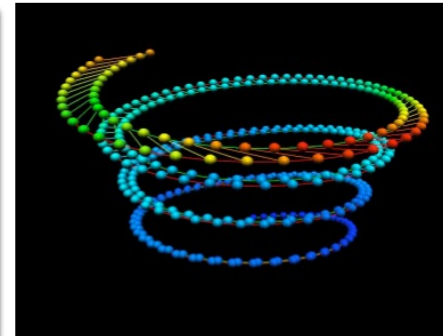
Tube



Ribbon



Lines



Balls + lines

Modulate pitch based on uncertainty

Streamline Variability Plots for Characterizing the Uncertainty in Vector Field Ensembles

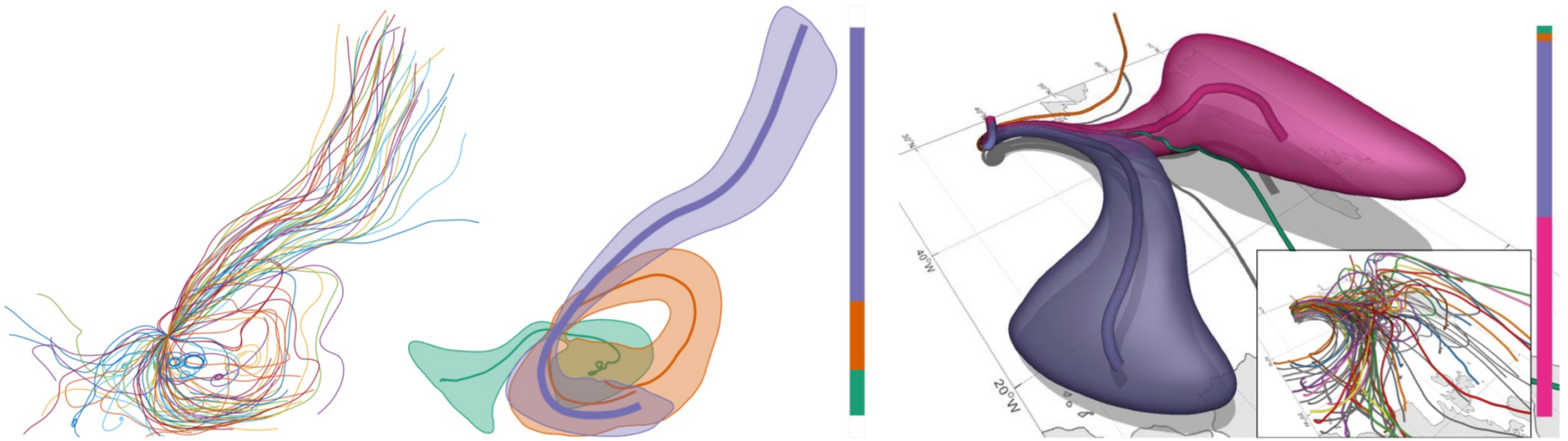


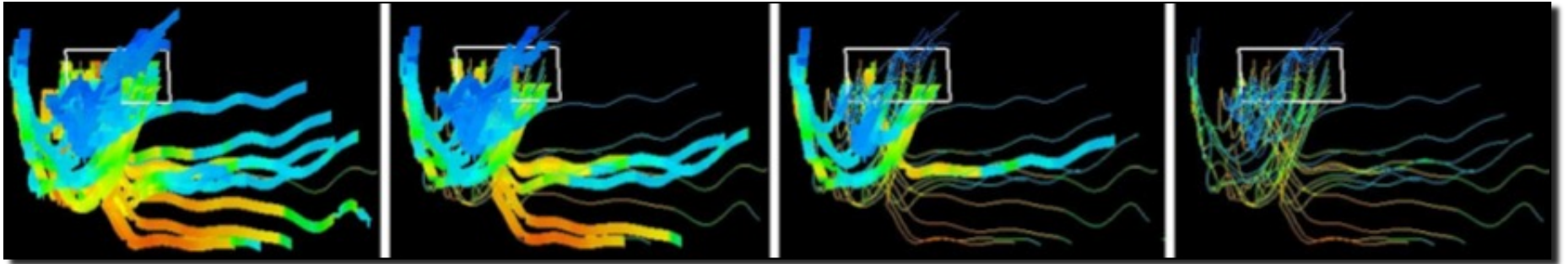
Fig. 1. From a set of streamlines in an ensemble of vector fields (left), our method generates an abstract visualization of the major trends in this set (middle). For each trend, a region of high confidence and a representative streamline-median is extracted. The relative strength of a trend is indicated by the thickness of its median line and by the bar plot on the right. Our method works in 2D and 3D (right), as well as for particle trajectories in time-dependent fields.



Ferstl, F., Bürger, K., & Westermann, R. (2015). Streamline variability plots for characterizing the uncertainty in vector field ensembles. *IEEE Transactions on Visualization and Computer Graphics*, 22(1), 767-776.

3D Meteorological Trajectory

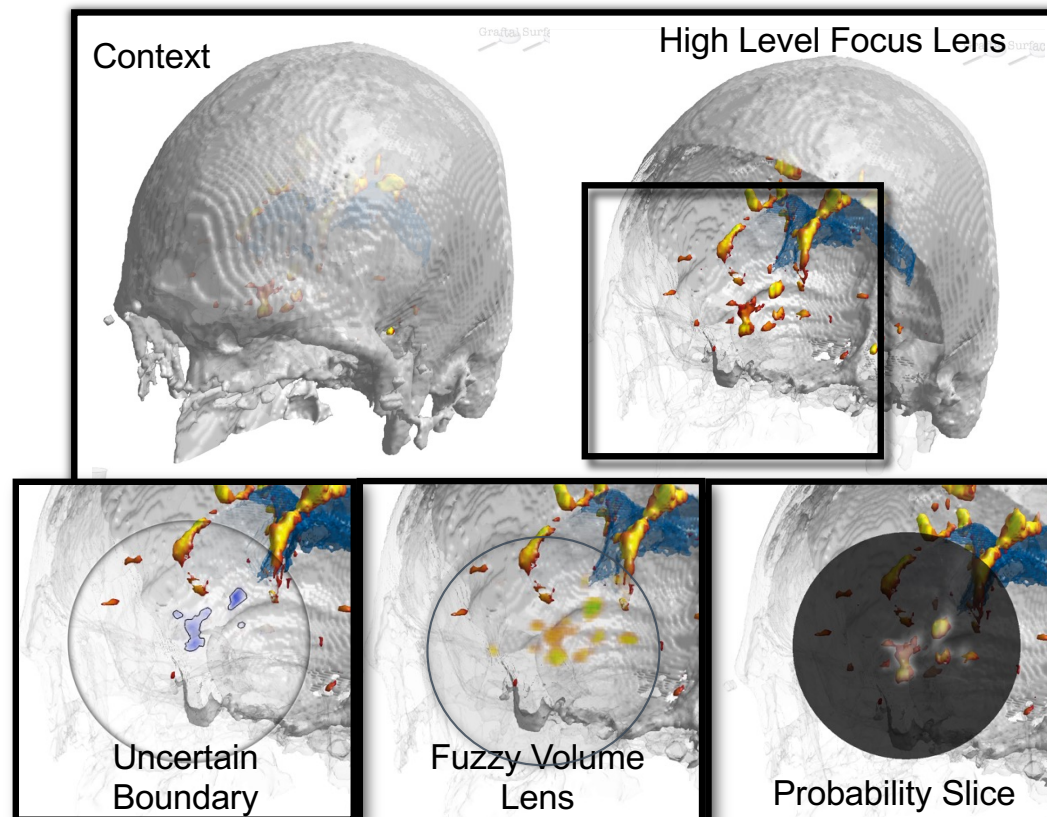
- Estimate uncertainty due to interpolation
- User seeded trajectories
- Prune trajectories with high uncertainty



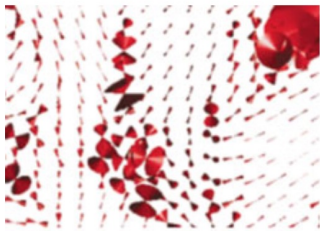
R. Boller, S. Braun, J. Miles, D. Laidlaw.
Application of Uncertainty Visualization Methods to
Meteorological Trajectories.
In Earth Science Informatics, 3(1-2), 2010.

QuizLens: A Multi-lens approach for uncertainty exploration

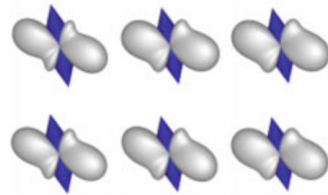
- Global information important for qualitative evaluation & context
- Local information necessary for quantitative understanding
- Interchangeable lenses to explore various data characteristics



DTI Tensor Uncertainty Visualization



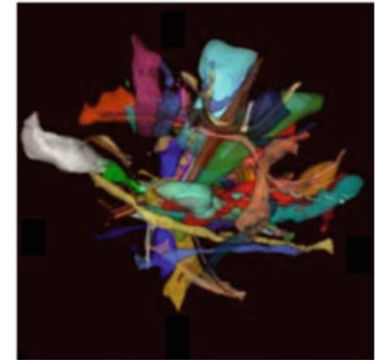
(a) Uncertainty cones [50]



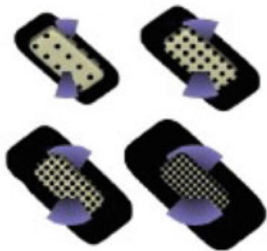
(b) HiFiVE Glyphs [90]



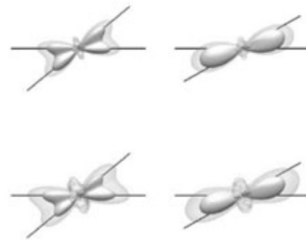
(a) Spaghetti plot [51]



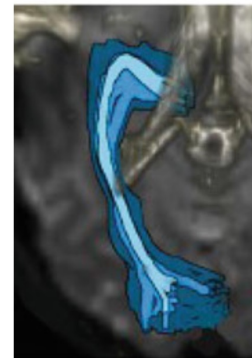
(b) Wrapped streamlines [19]



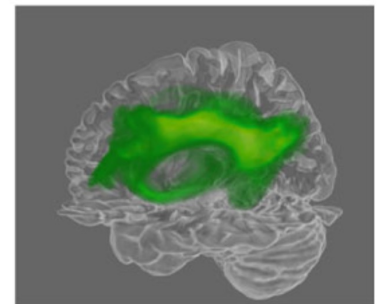
(c) Decomposed ensemble representation [110]



(d) ODF glyphs [96]



(c) Illustrative visualization [15]

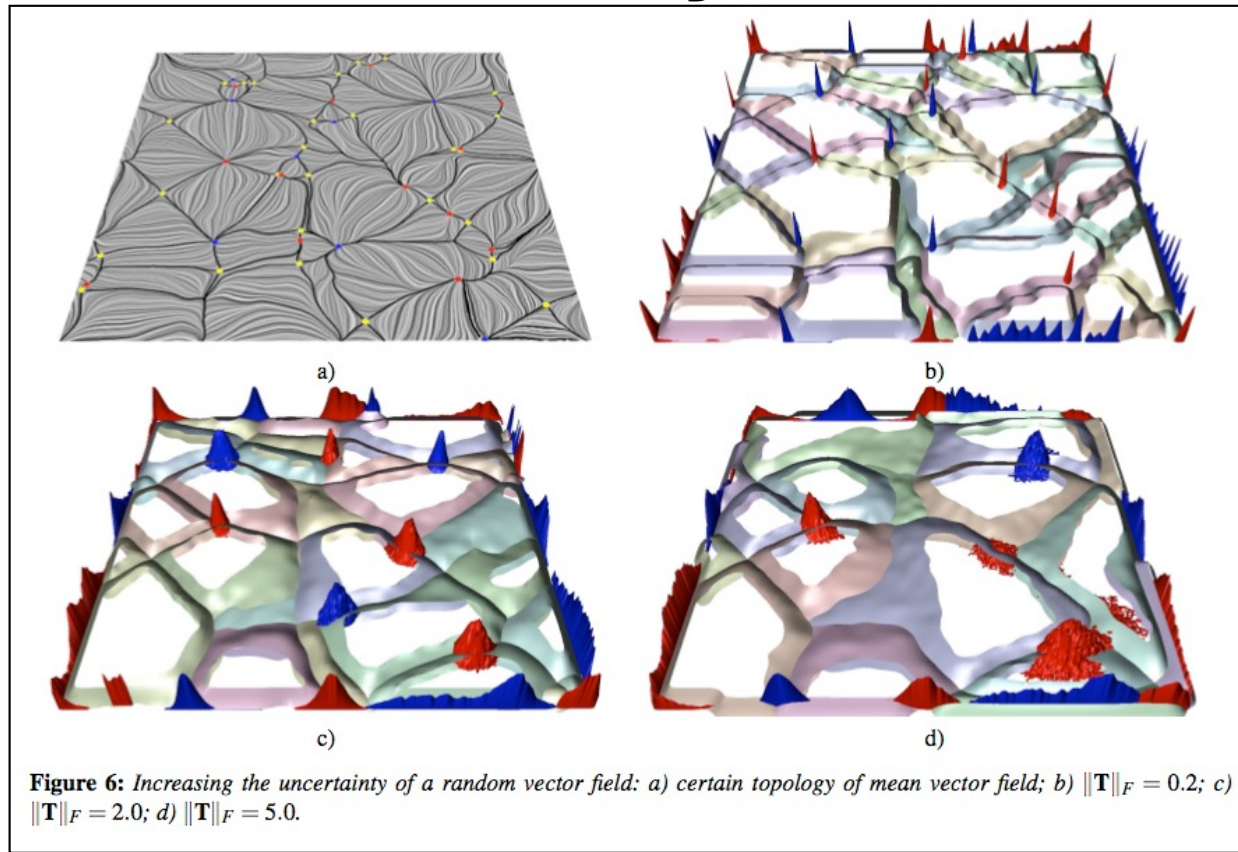


(d) Connectivity mapping [55]



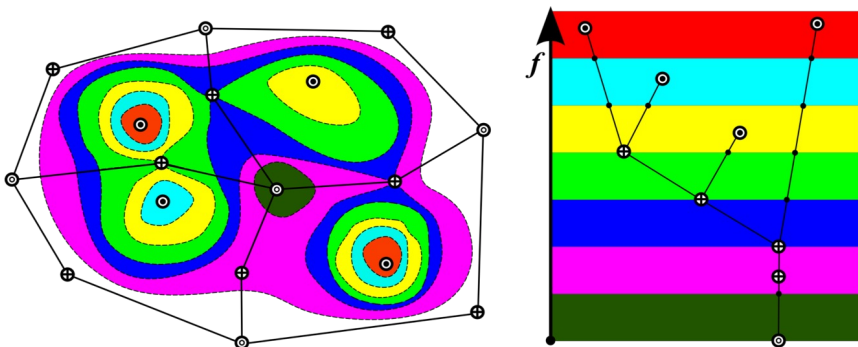
Siddiqui, F., Höllt, T., & Vilanova, A. (2021). Uncertainty in the DTI Visualization Pipeline. *Anisotropy Across Fields and Scales*, 125.

Topological Uncertainty

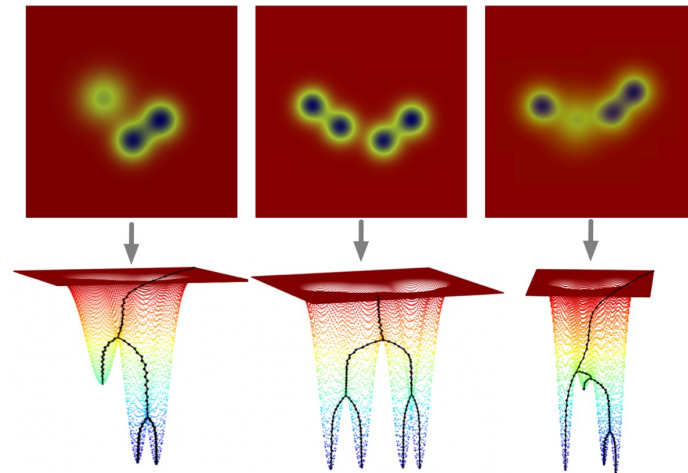


M. Otto, T. Germer, H.C. Hege, H. Theisel. Uncertain 2D Vector Field Topology. In CGF, 29(2), 2010.

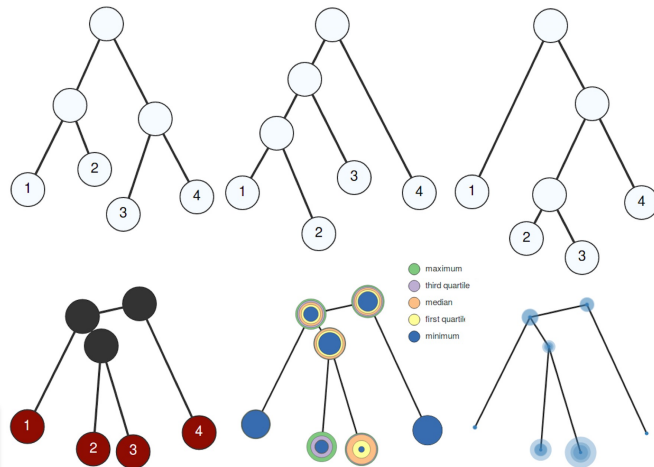
Visualizing uncertainty in topological structures



Merge Tree: a topological summary of scalar fields



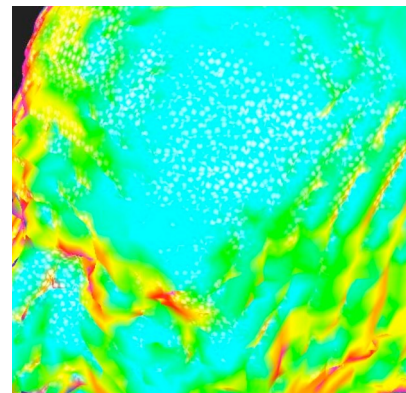
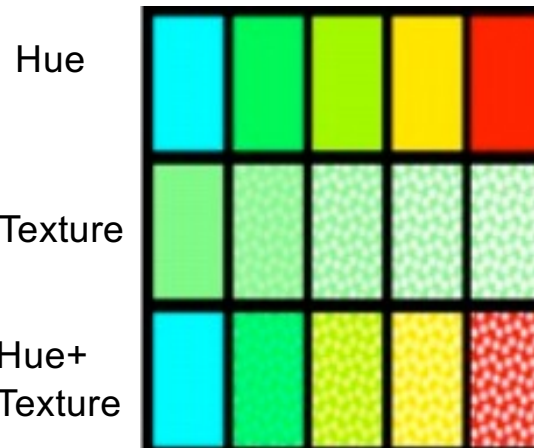
Merge trees that arise from an ensemble of scalar fields



1. Compute an average merge tree from an ensemble
2. Uncertainty visualization of the average tree captures structural variations among the ensembles

Volumetric Data - Isosurfacing

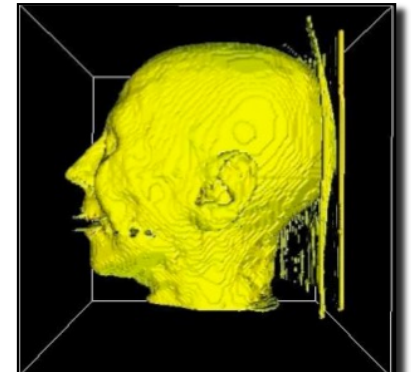
- Isosurfaces show where a volumetric data value lies in space
- Map uncertainties to:
 - hue, saturation, brightness
 - texture mapping
- Isovalue eases display



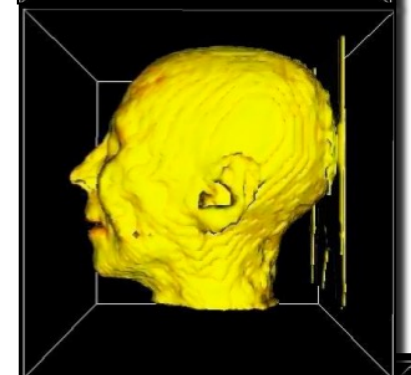
P. Rhodes, R. Laramée, R.D. Bergeron, T. Sparr.
Uncertainty Visualization Methods in Isosurface
Rendering.
In EUROGRAPHICS 2003 Short Papers, 2003.



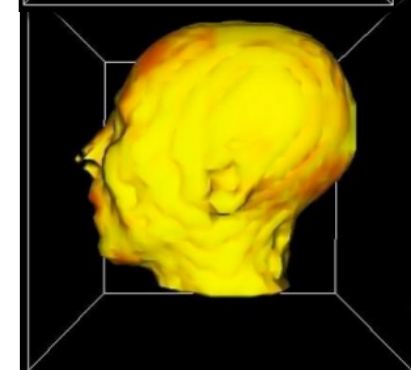
128³



64³



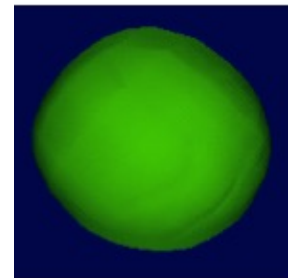
16³



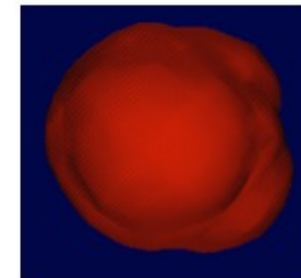
Visualization Uncertainties - Isosurfaces

- Uncertainty from differences in isosurface creation
- Compare
 - marching cubes & marching cubes with ambiguous cell correction
 - interpolation schemes

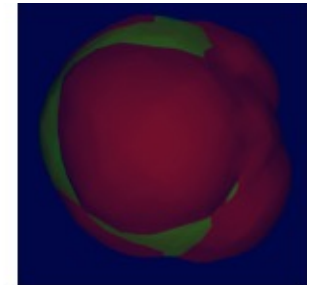
A. Jospeh, S. Lodha, J. Renteria, A. Pang.
UISURF: Visualizing Uncertainty in Isosurfaces.
In Proc Computer Graphics and Imaging, 1999.



(a)

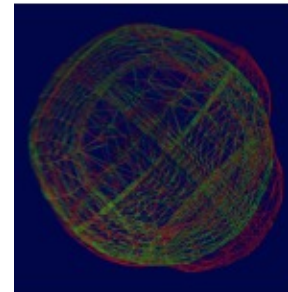


(b)

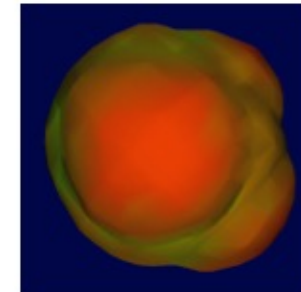


(c)

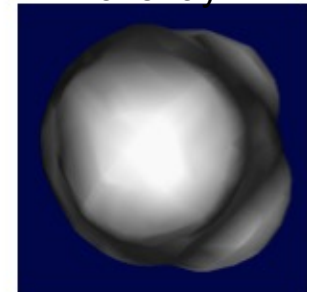
overlay



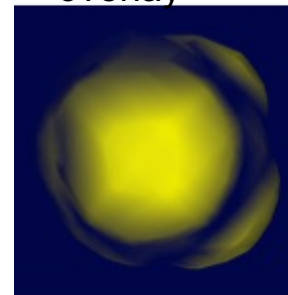
wireframe
overlay



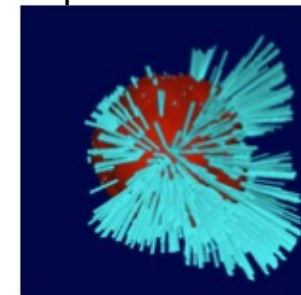
green/red
psuedo-coloring



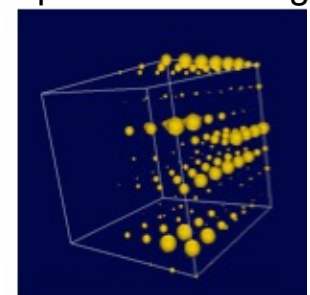
gray (f)
psuedo-coloring



transparency
(g)



box glyphs
(h)



ball glyphs
(i)

Possibilistic Marching Cubes

Possibility theory is mathematically the simplest uncertainty theory for dealing with incomplete information. It is a natural means for quantifying epistemic uncertainty coming from lack of knowledge.

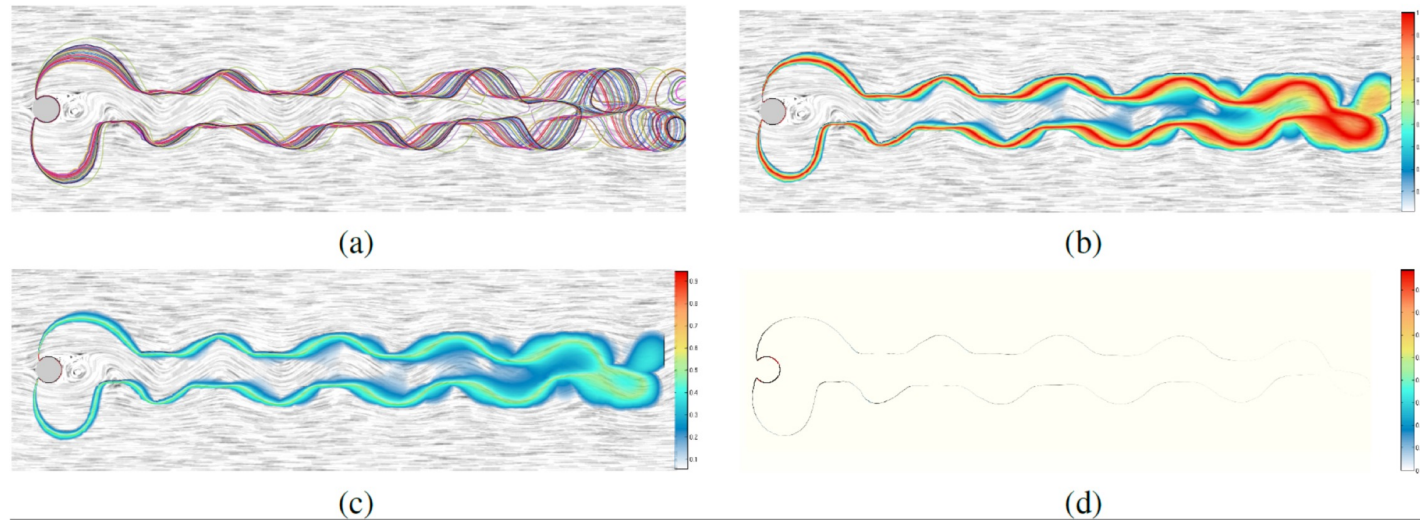


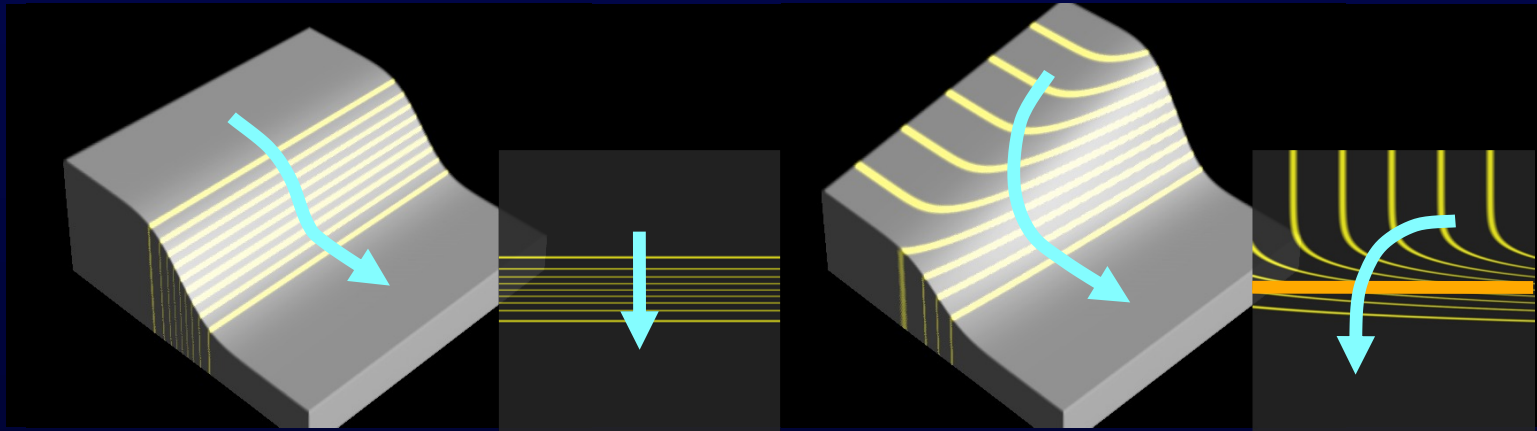
FIG. 7: Uncertain isocontours of the pressure field: (a) Ensemble of isocontours of the pressure field extracted from fluid simulation. (b) Possibilities (from PossMC) visualization. (c) Pignistic probabilities (from PossMC) visualization. (d) Necessities (from PossMC) visualization (the contour is faded looking due to the chosen colorbar: small necessity values are represented by white and light blue colors). The visualization has been overlaid on top of a LIC [49] visualization of one of the ensemble members.



He, Y., Mirzargar, M., Hudson, S., Kirby, R. M., & Whitaker, R. "An uncertainty visualization technique using possibility theory: Possibilistic marching cubes." *International Journal for Uncertainty Quantification* 5.5 (2015).

Isosurface uncertainty

Two kinds of boundaries

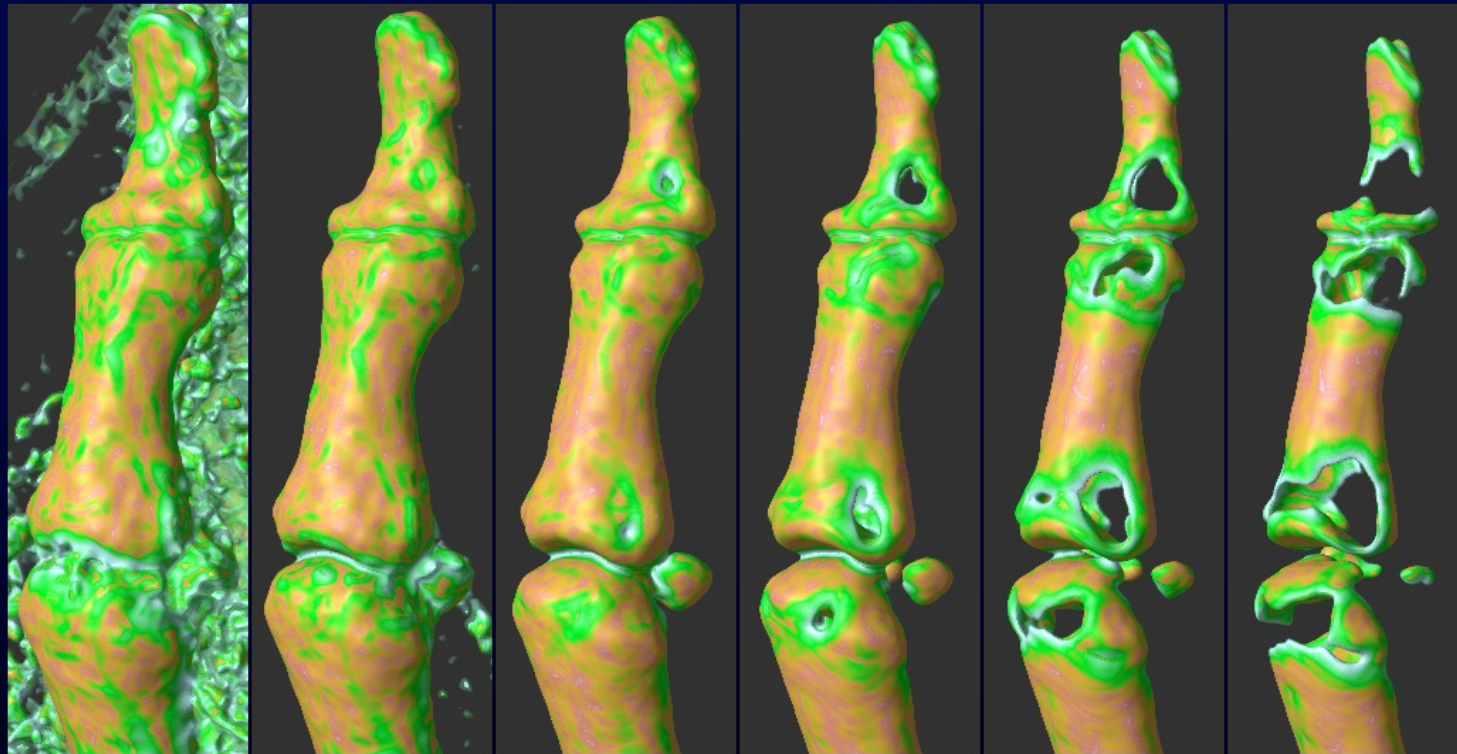


Flow-line curvature (ter Haar Romeny et al., 1991) for uncertainty visualization:

- **Material boundaries are intrinsic**
- **If small Δ isovalue \Rightarrow big Δ isosurface orientation, isosurface probably not a good material boundary**
- **Qualitative indicator of surface model uncertainty**

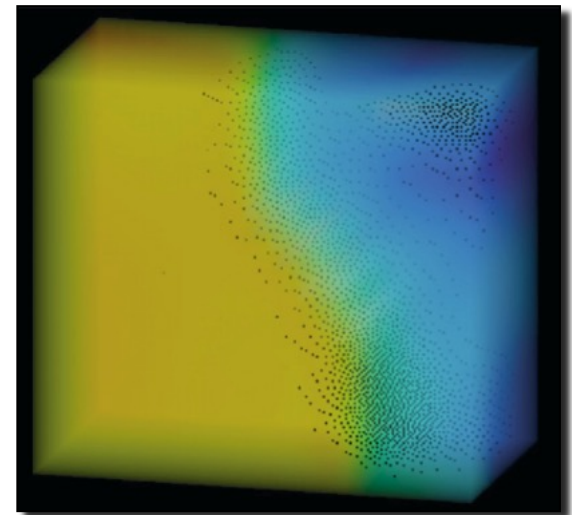
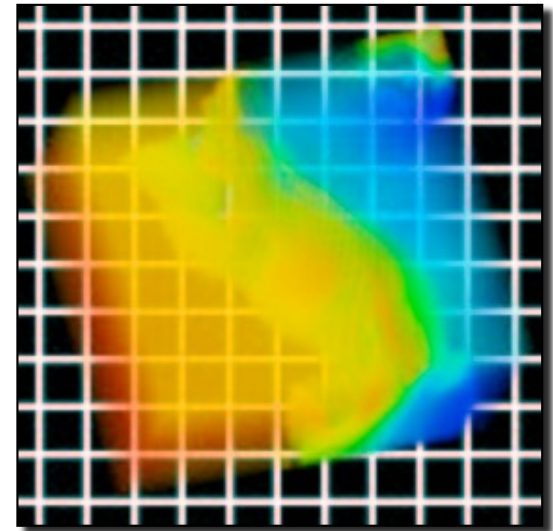
Flow-line curvature results

Thumb from Visible Human Female, fresh CT:



Volumetric Data-Volume Rendering

- Show data with high or low uncertainty
- Map data to color & uncertainty to opacity
- Add discontinuities to regions of high uncertainty (speckles, noise)

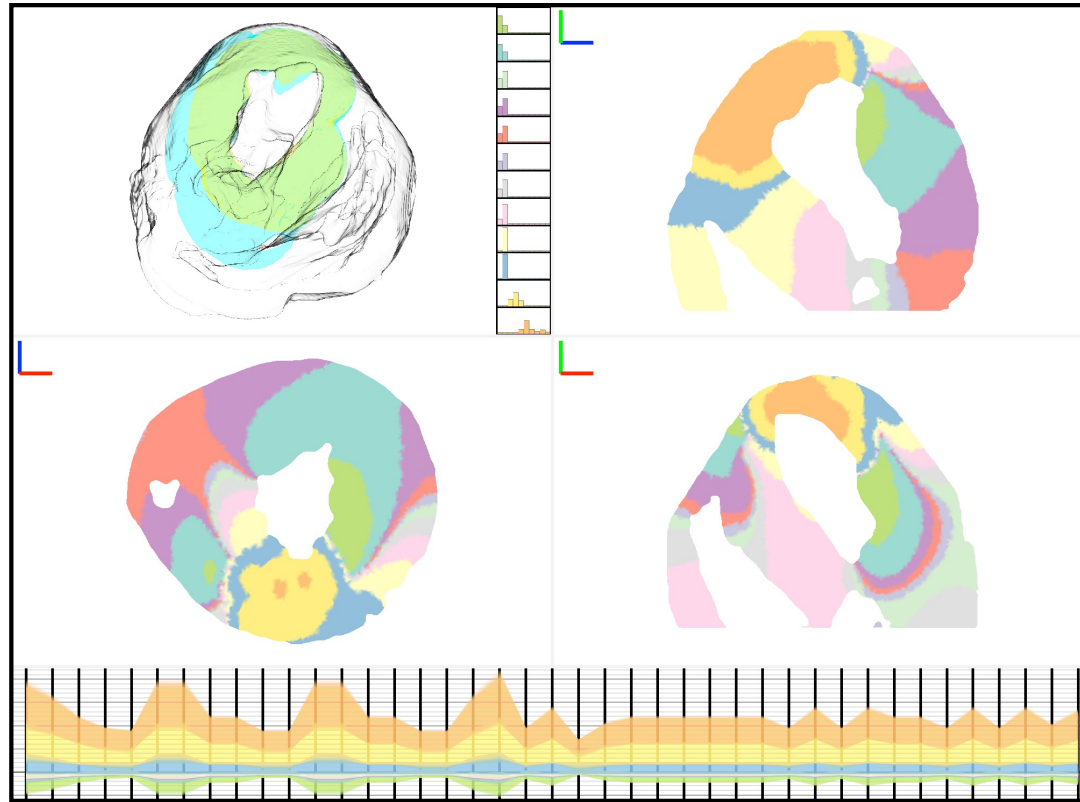


S. Djurcilov, K. Kim, P. Lermusiaux, A. Pang.
Visualizing Scalar Volumetric Data with Uncertainty.
In *Computers and Graphics*, vol. 26, 2002.

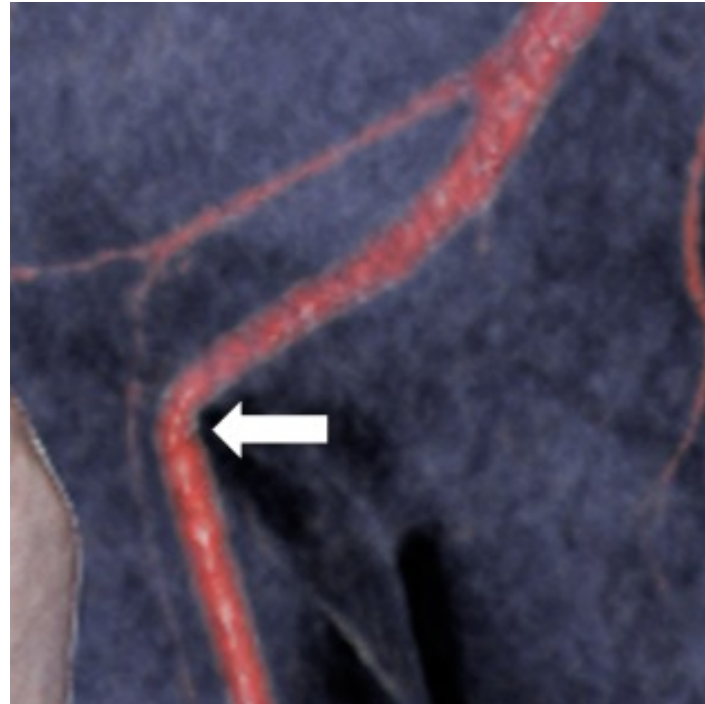
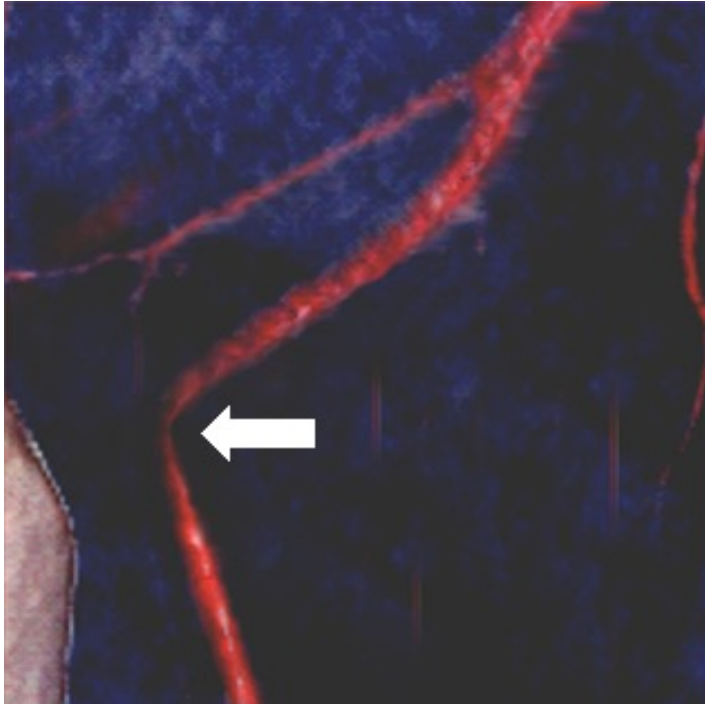
S. Djurcilov, K. Kim, P. Lermusiaux, A. Pang.
Visualizing Scalar Volumetric Data with Uncertainty.
In *Computers and Graphics*, vol. 26, 2002.

muView Visualization System

Visualizing uncertainty in cardiac ischemia simulations

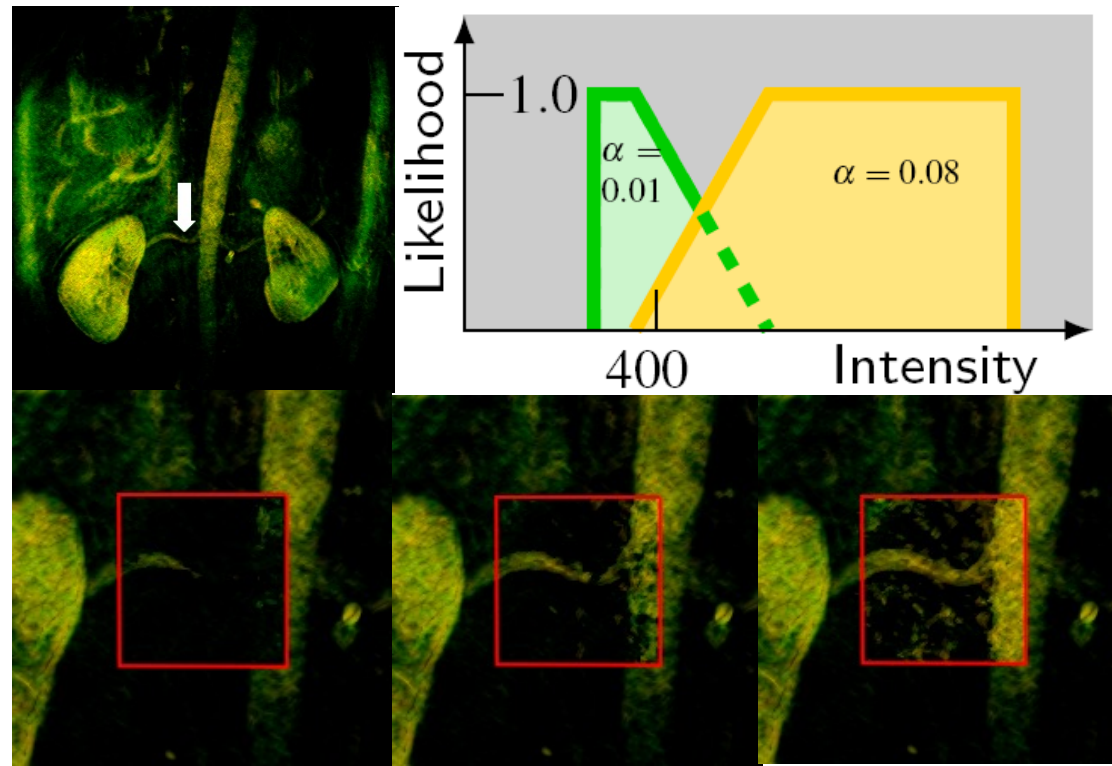


Uncertainty Visualization



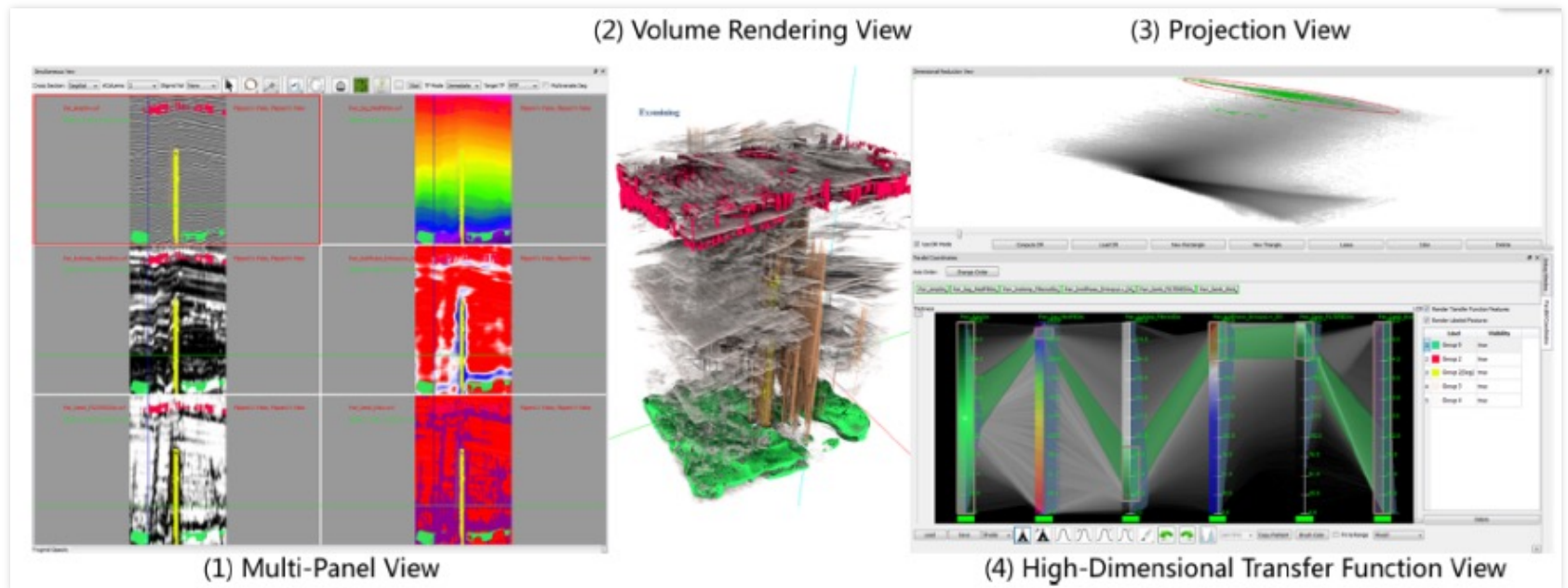
Images Courtesy of Claes Lundström, Patric Ljung, Anders Persson,
Anders Ynnerman

Uncertainty Visualization



Volume Rendering using High Dimensional Transfer Functions

- Create Transfer Functions (TFs) from user selected samples in spatial domain and error/uncertainty.
- Multiple linked views.



Functional Box Plot

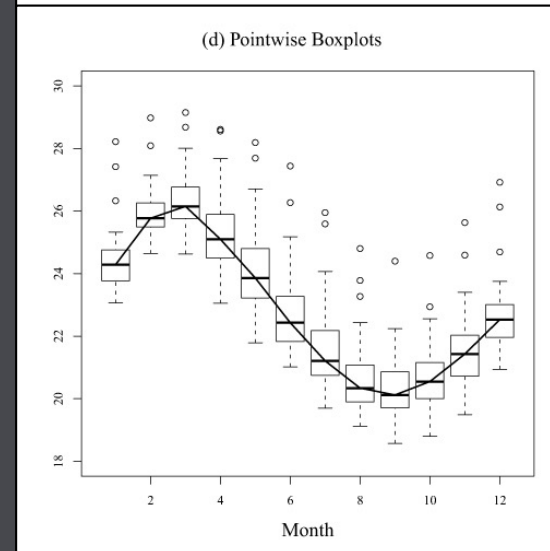
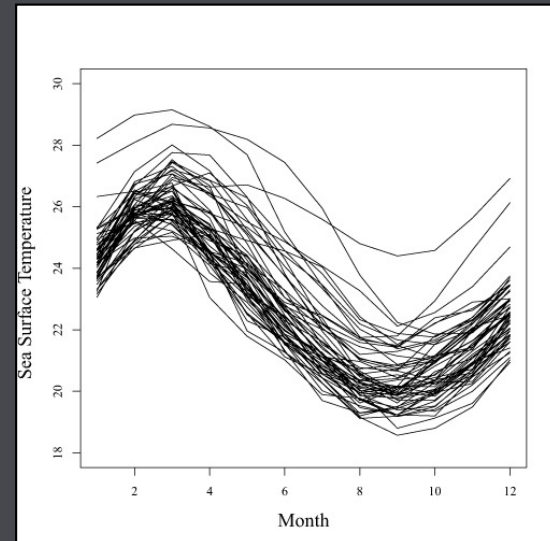
Boxplot statistics on 2D functions

Defined on the function, rather than point-wise

Functional Boxplots.

Ying Sun, Marc G. Genton.

J. of Comp. and Graphical Statistics 20:2, 2011, 316-334.



Functional Box Plot

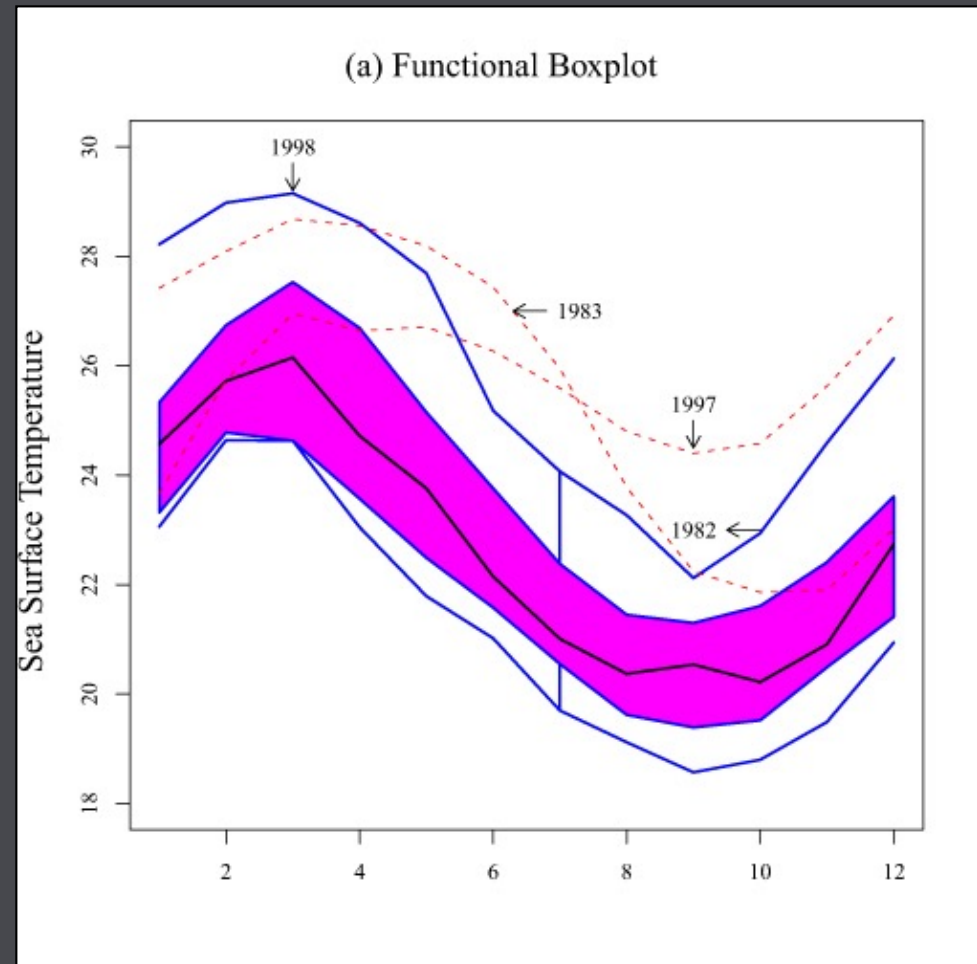
Band Depth

The amount of time a function lies within the set of functions

Functional Boxplots.

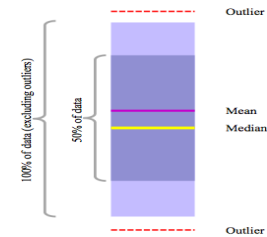
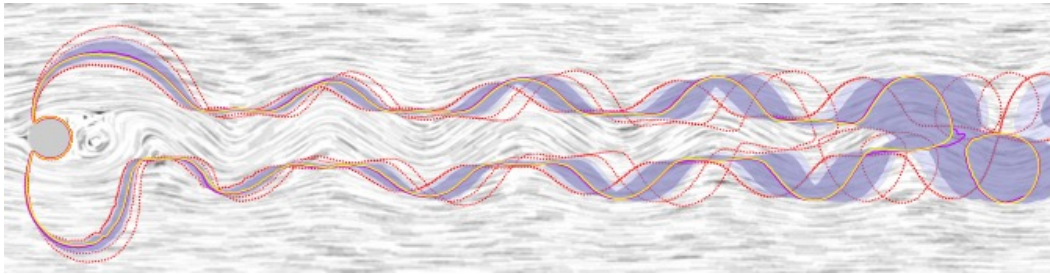
Ying Sun, Marc G. Genton.

J. of Comp. and Graphical Statistics 20:2, 2011, 316-334.



Contour Box Plots

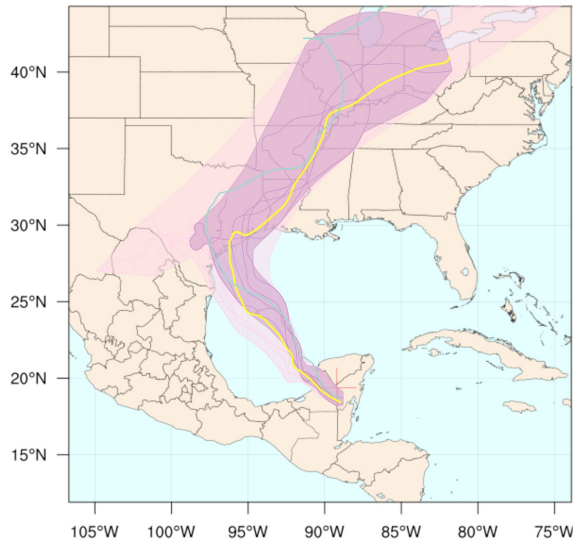
$$S \in \text{sB}(S_1, \dots, S_j) \iff \bigcap_{k=1}^j S_k \subset S \subset \bigcup_{k=1}^j S_k.$$



Whitaker, Mirzargar, Kirby, *IEEE Transactions on Visualization and Computer Graphics*, Vol. 19, No. 12, pp. 2713--2722, 2013.

M.G. Genton, C.R. Johnson, K. Potter, G. Stenchikov, Y. Sun.
"Surface boxplots," In *Stat Journal*, Vol. 3, No. 1, pp. 1-11. 2014.

Ensemble Curved Boxplot



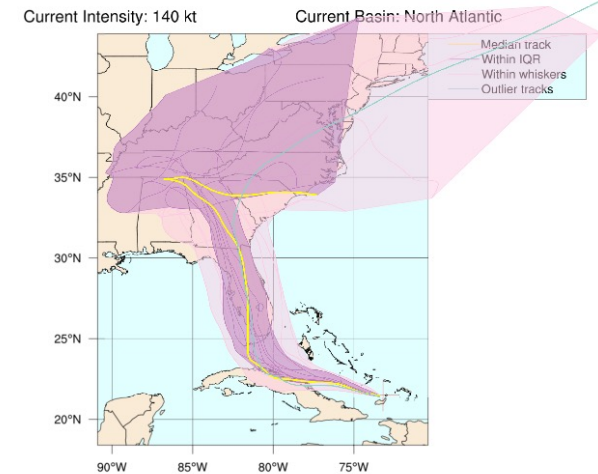
This plot is an experimental boxplot visualization

By using this plot, the user agrees to the UCAR Terms of Use which can be accessed at: <http://www2.ucar.edu/terms-of-use>

Plot generated at 0613 UTC 23 August 2017

MAJOR HURRICANE IRMA (AL11)

GFS ensemble curve boxplot initialized at 0600 UTC, 08 September 2017



This plot is an experimental boxplot visualization

By using this plot, the user agrees to the UCAR Terms of Use which can be accessed at: <http://www2.ucar.edu/terms-of-use>

Plot generated at 1522 UTC 08 September 2017



M. Mirzargar, R. Whitaker, R. M. Kirby. "Curve Boxplot: Generalization of Boxplot for Ensembles of Curves,"
IEEE Transactions on Visualization and Computer Graphics, Vol. 20, No. 12, IEEE, pp. 2654-63. December, 2014.

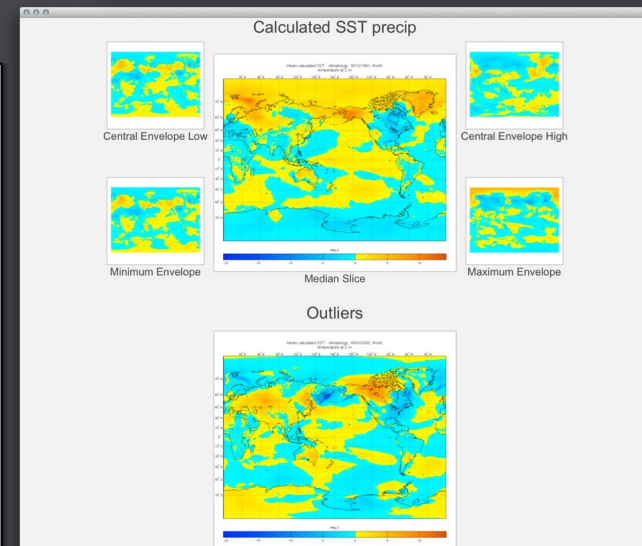
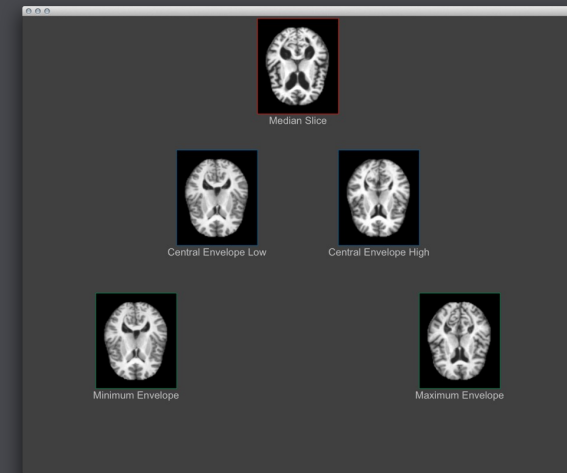
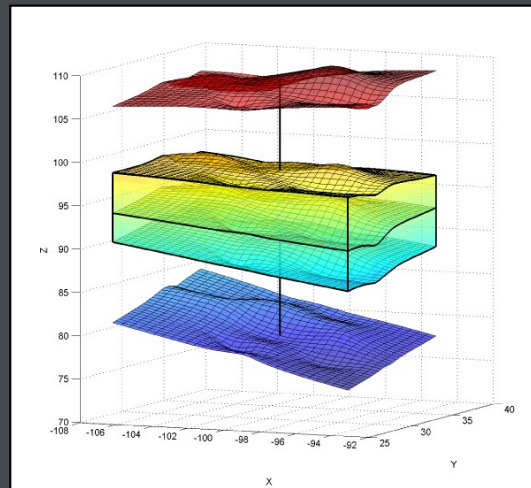


Surface Box Plots

- Extension of band depth to 3D
- *Images rather than curves*
- *Volume-based band-depth*

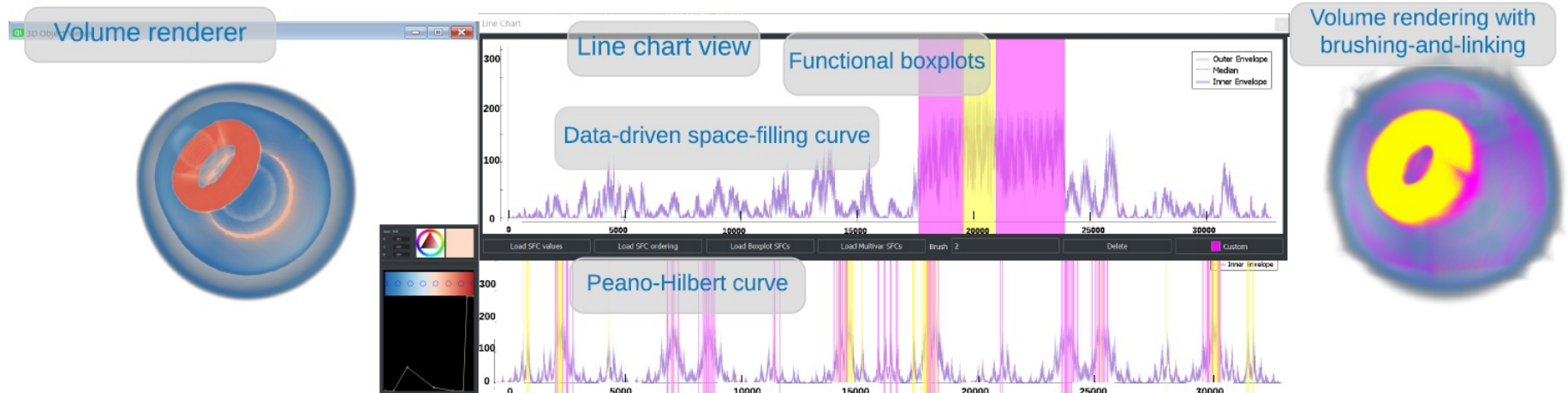
Surface Boxplots.

Marc G. Genton, Christopher Johnson,
Kristin Potter, Georgiy Stenchikov, and
Ying Sun.
Stat. 3:1, 2014, 1–11.



Data-driven space-filling curves

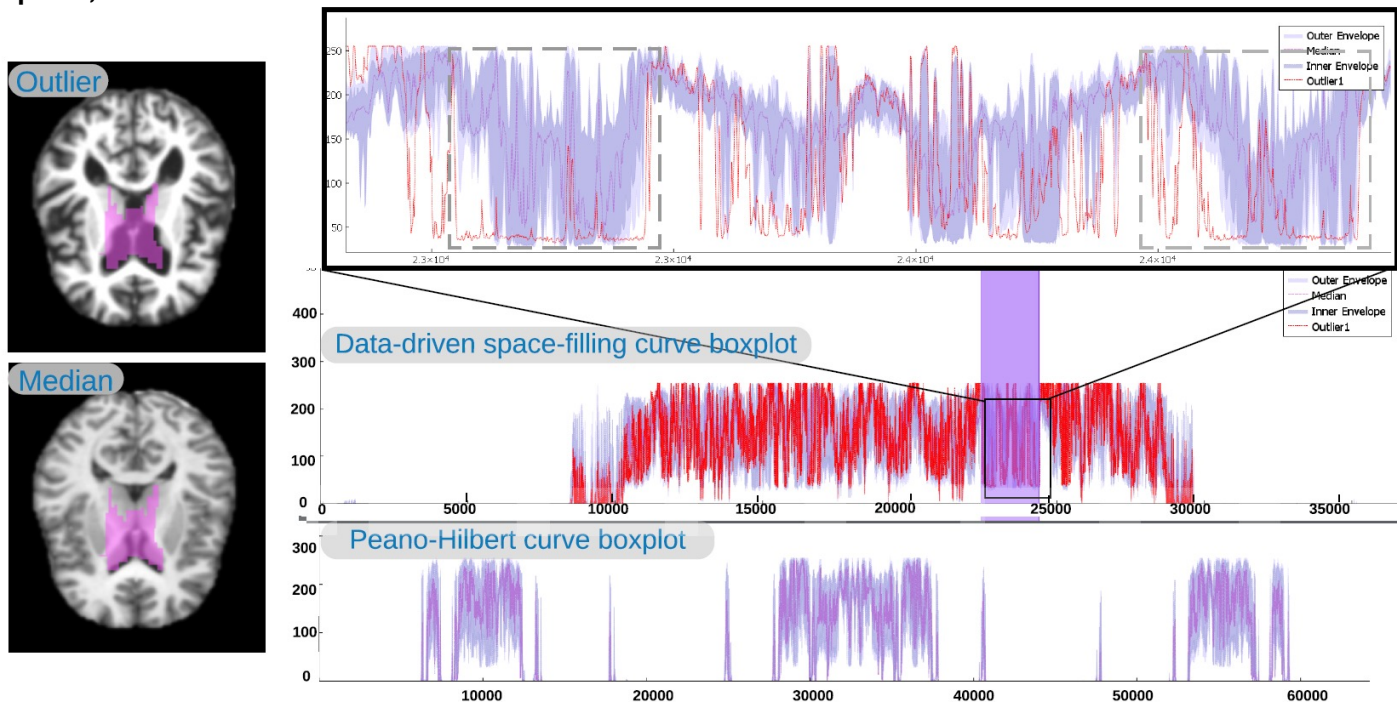
- Data-driven space-filling curves
 - better coherency preservation (data value + position) than existing methods
 - 2D and 3D data
 - regular grids and multiscale
- A flexible Hamiltonian path method



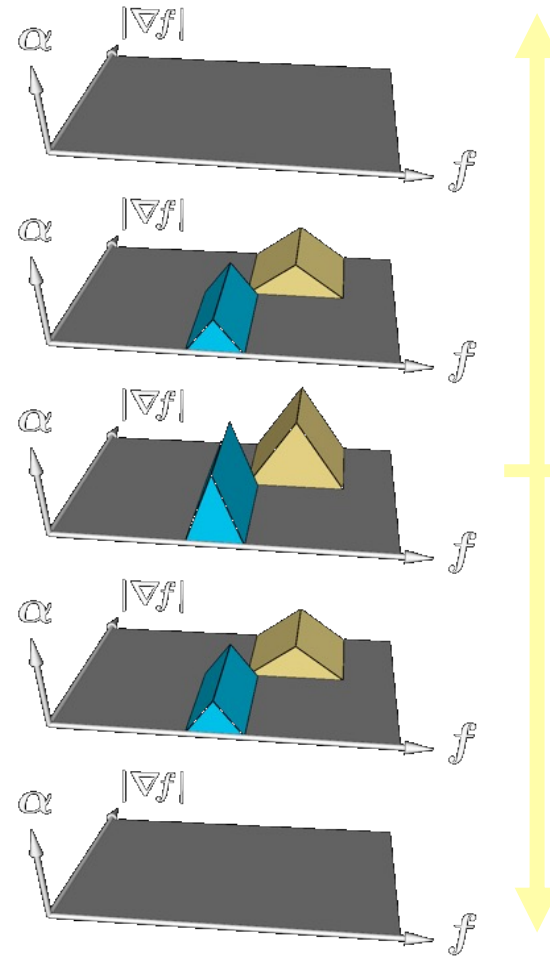
L. Zhou, C. R. Johnson, D. Weiskopf. "Data-Driven Space-Filling Curves," In IEEE Transactions on Visualization and Computer Graphics, Vol. 27, No. 2, IEEE, pp. 1591-1600. 2021.

Example - Brain Atlas

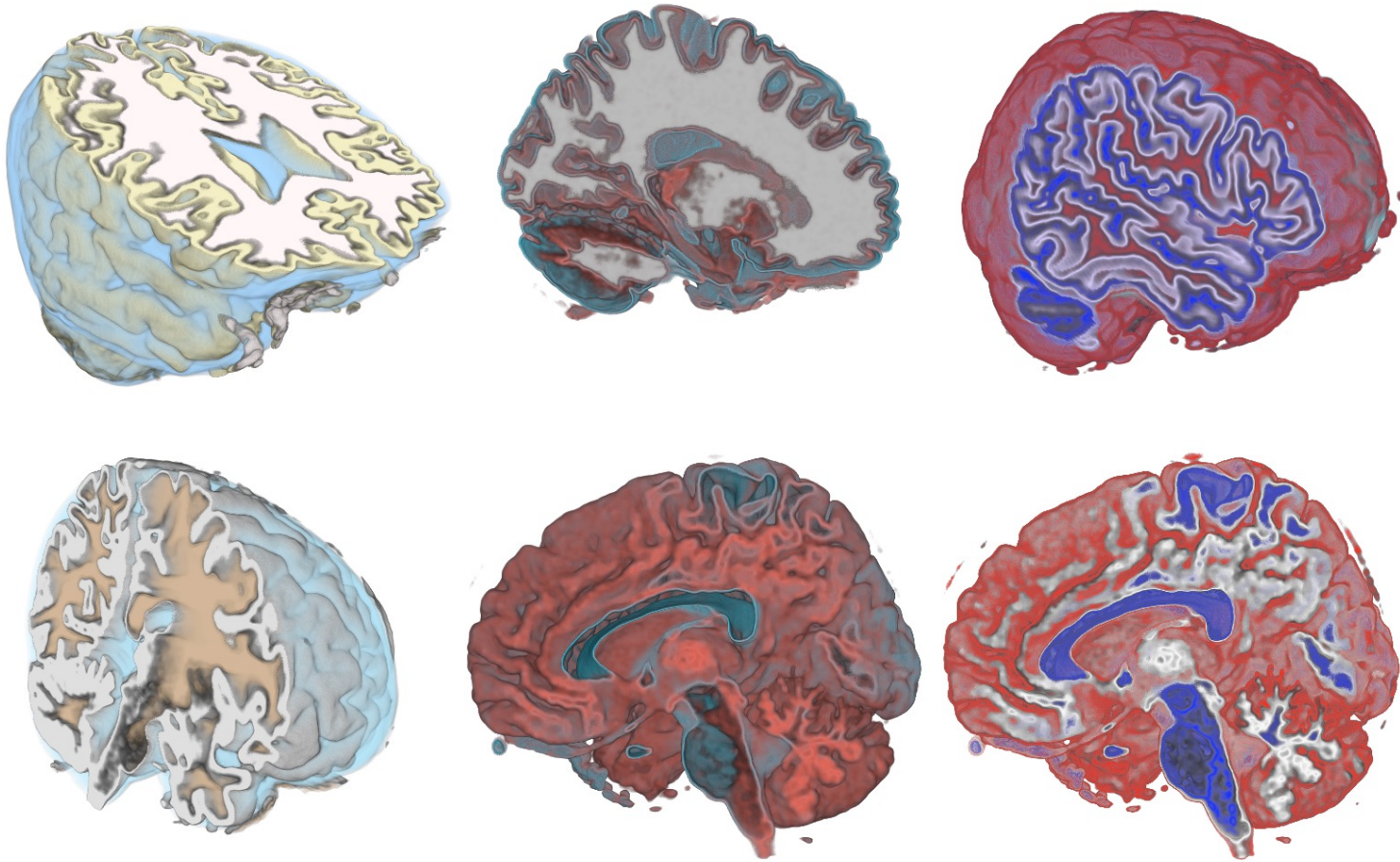
- Brain atlas of 2D MRI scans (176*208 pixels); curve generation time: 3m49s
- Surface Boxplot; linearized based on the median



3D Transfer Function

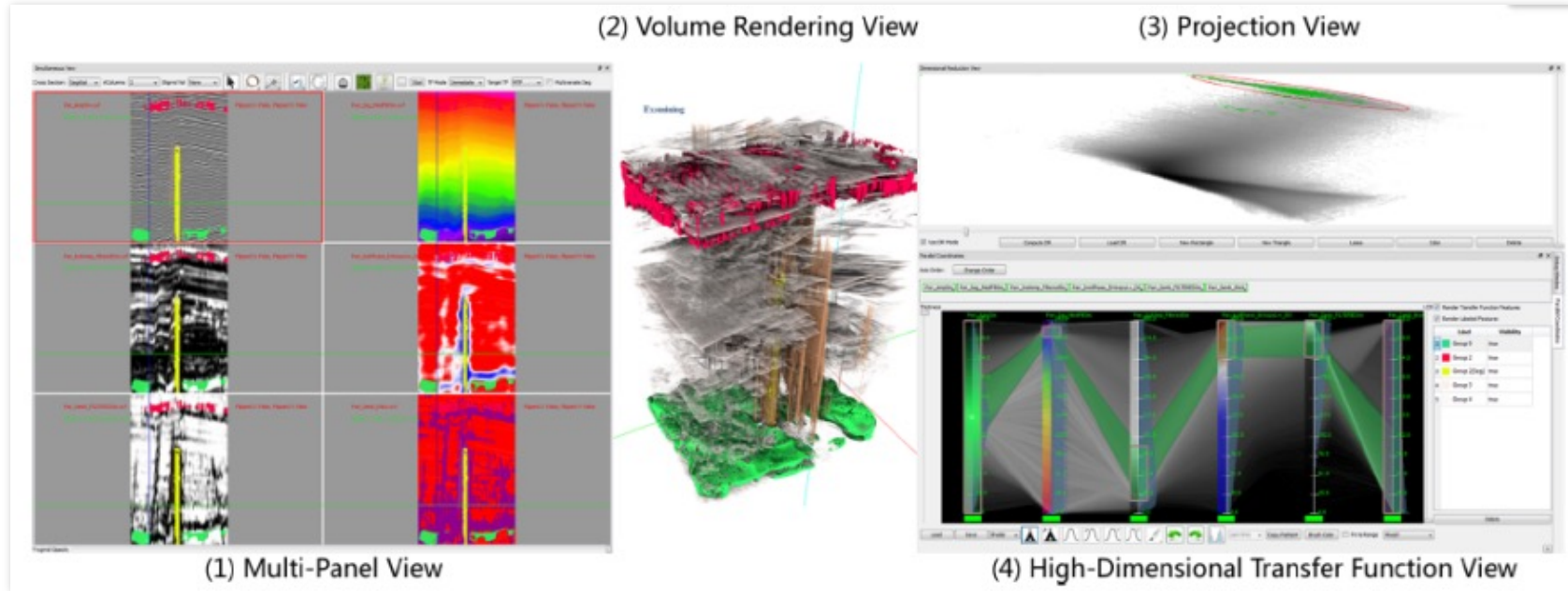


Visualizing Uncertainty Using Volume Rendering

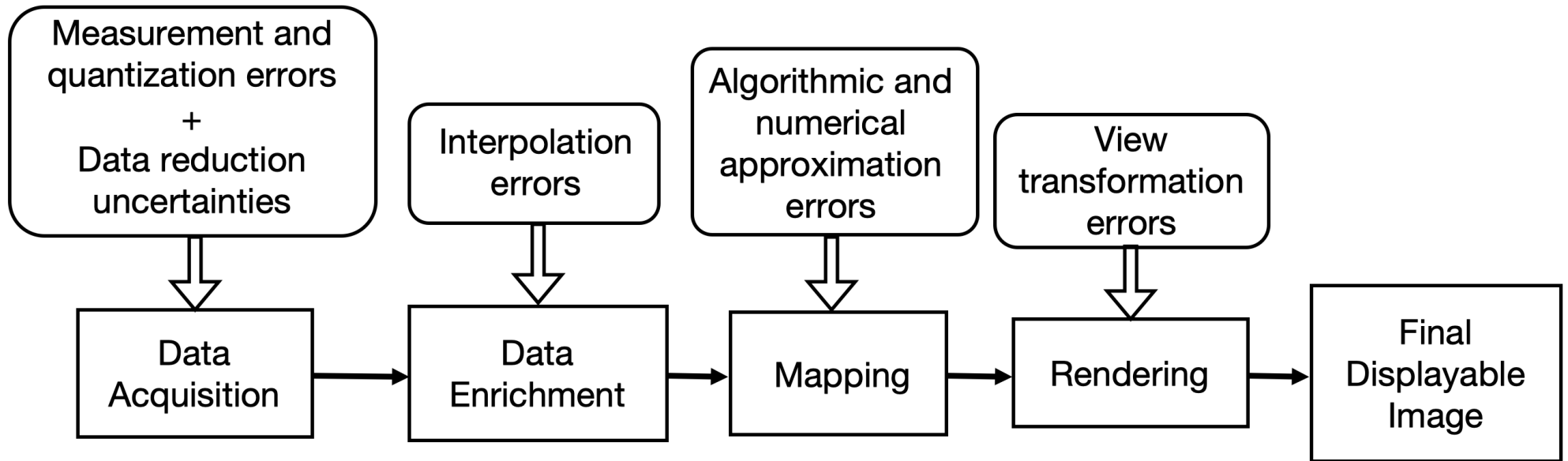


High Dimensional Transfer Functions

- Create Transfer Functions (TFs) from user selected samples in spatial domain and error/uncertainty.
- Multiple linked views.



Uncertainty-Aware Volume Visualization



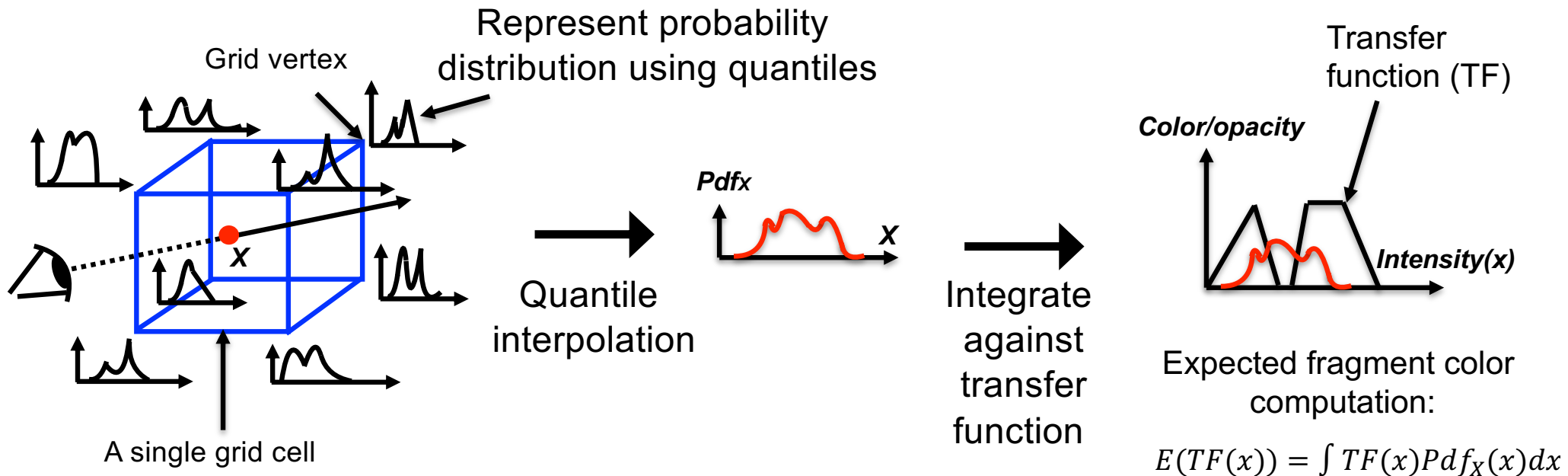
Visualization pipeline
[Brodie et al., 2012]

Contributions

- Nonparametric statistical framework for the quantification, analysis, and propagation of data uncertainty in direct volume rendering (DVR).
- Nonparametric models of uncertainty improve the quality of reconstruction and classification within an uncertainty-aware direct volume rendering framework.
- Closed-form nonparametric framework for efficient statistical rendering. Linear time complexity compared to Monte Carlo methods.
- Qualitative and quantitative comparisons with the mean, parametric, and Gaussian mixture models
- Application of statistical volume rendering to multidimensional transfer functions



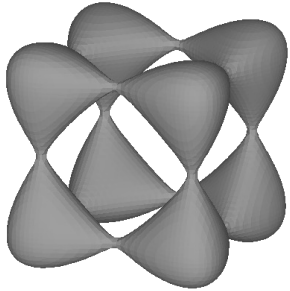
Volume Rendering With Nonparametric Statistics



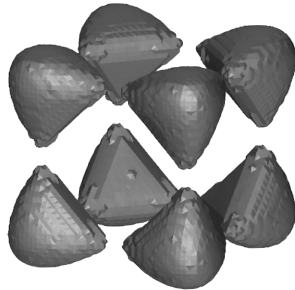
T. Athawale, B. Ma, E. Sakhaee, C.R. Johnson, and A. Entezari.
 Nonparametric Statistical Framework for Direct Volume Rendering
 of Uncertain Data. IEEE Visualization 2020, Oct. 2020.

Models of Uncertainty

Ground truth:
Tangle function
mixed with noise

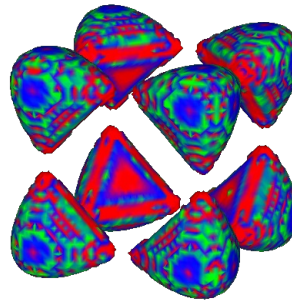


Mean

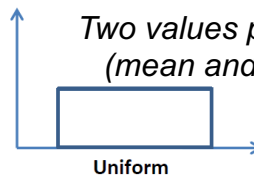


One value per-voxel

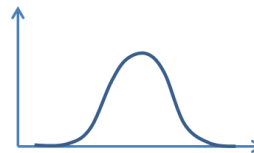
Parametric



Two values per-voxel
(mean and width)

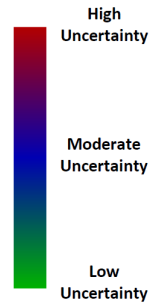
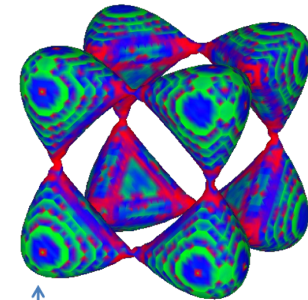


Uniform

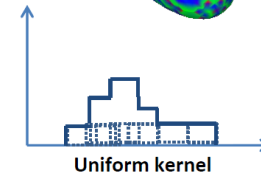


Gaussian

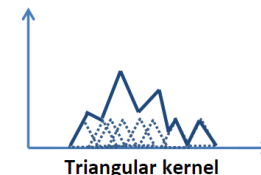
Nonparametric



n representative samples
per-voxel (e.g., min, Q1,
median, Q2, max)



Uniform kernel

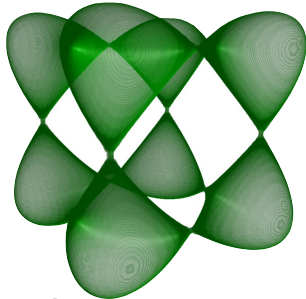


Triangular kernel

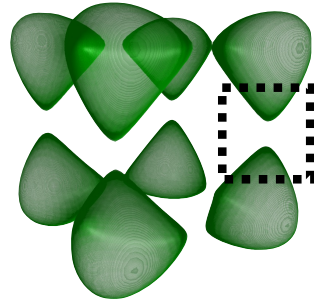
Probabilistic marching cubes,
[Pöthkow et al., 2013];

Uncertainty-aware marching
cubes [Athawale et al., 2015]

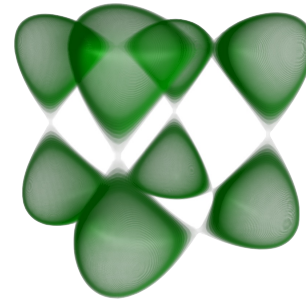
Tangle Function (Qualitative Comparisons)



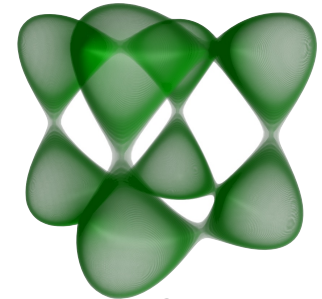
Ground truth



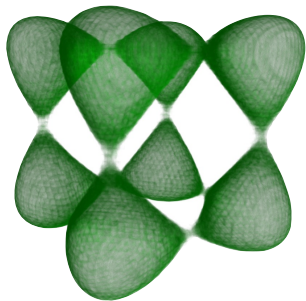
Mean



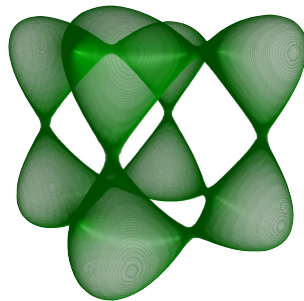
Uniform



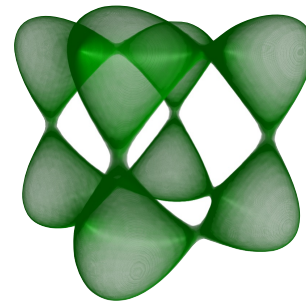
Gaussian



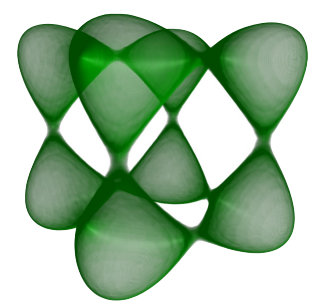
Gaussian mixtures
(four Gaussians)
(Monte Carlo)



Quantile interpolation
(two quantiles)

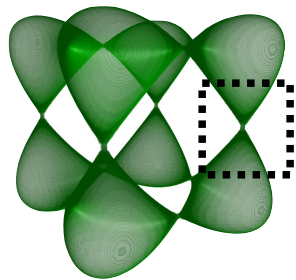


Quantile interpolation
(four quantiles)



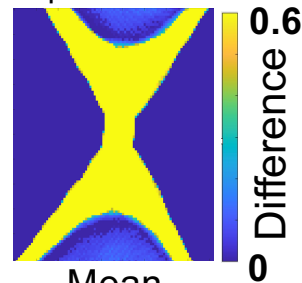
Quantile interpolation
(eight quantiles)

Tangle Function (Quantitative Comparisons)



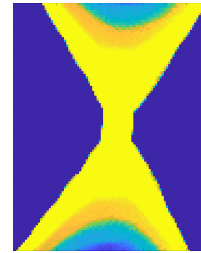
Ground truth

RMSE = 0.0245
fps = 10



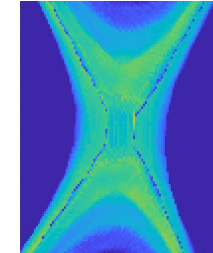
Mean

RMSE = 0.02
fps = 5



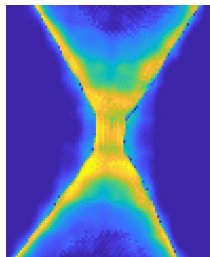
Uniform

RMSE = 0.0062
fps = 4.9



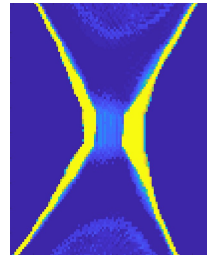
Gaussian

RMSE = 0.0051



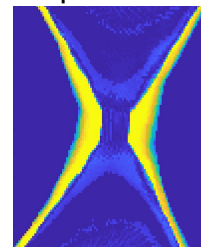
Gaussian mixtures
(Monte Carlo)

RMSE = 0.0067
fps = 6.1



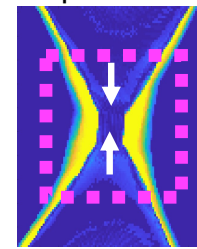
Quantile interpolation
(two quantiles)

RMSE = 0.0053
fps = 5.8



Quantile interpolation
(four quantiles)

RMSE = 0.0055
fps = 5.3



Quantile interpolation
(eight quantiles)

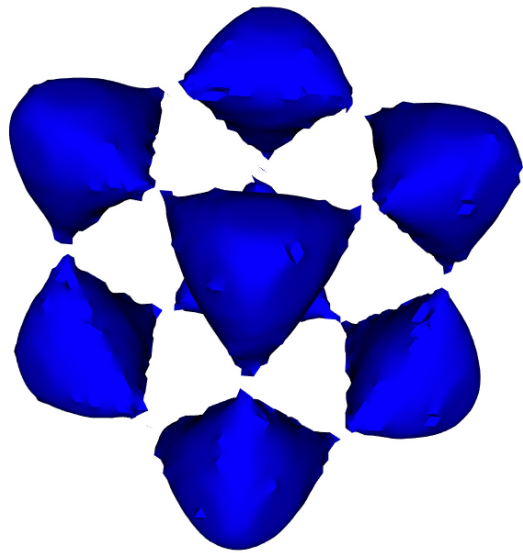
Visualizing Uncertain Multivariate Data Using Feature Confidence Level-Sets

- We explore whether extending the method by Zehner et al. to compute “Feature Confidence Level-Sets” is useful.
 - We would effectively be replacing “additional” feature level-sets with feature confidence level-sets.
- Assume each grid point has a distribution of values represented using a mean and standard deviation.
- For each grid point we compute an upper and lower confidence value using mean, standard deviation and confidence interval %.
- We perform a range intersection to determine if a trait exists at a grid point.

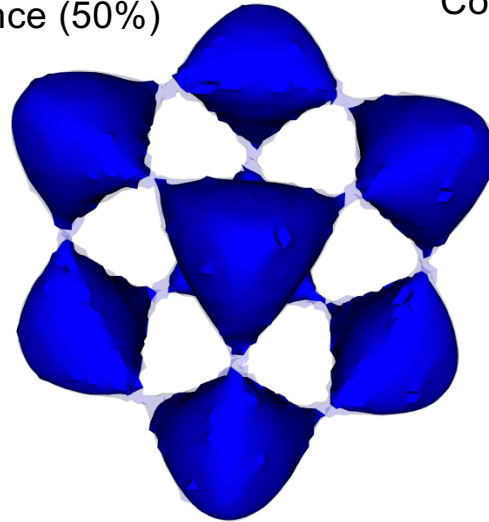
S. Sane, T. Athawale, and C.R. Johnson. Visualization of Uncertain Multivariate Data via Feature Confidence Level-Sets. EuroVis 2021.



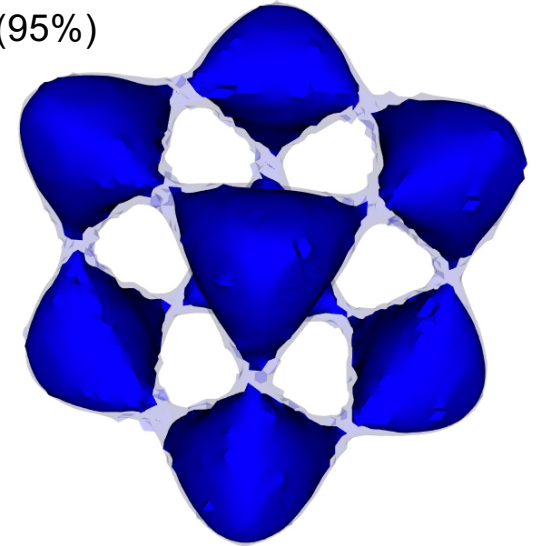
Zero level-set



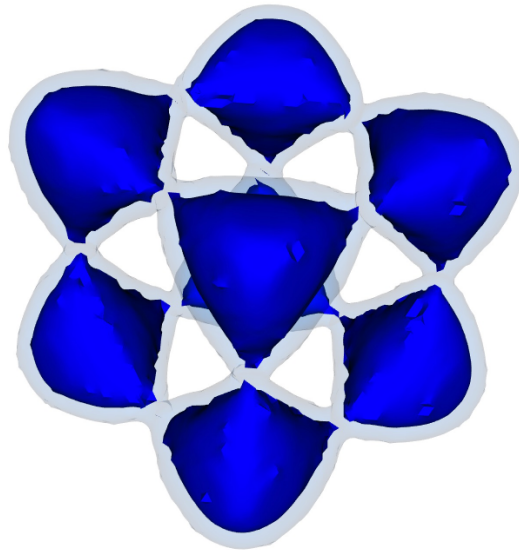
+ Feature
Confidence (50%)



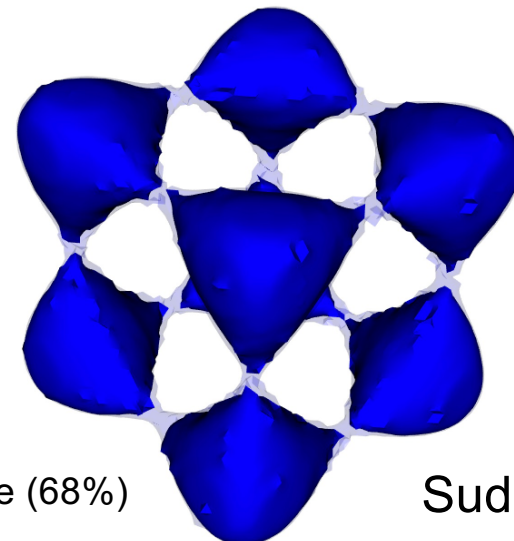
+ Feature
Confidence (95%)



+ Distance Field (2)



+ Feature
Confidence (68%)

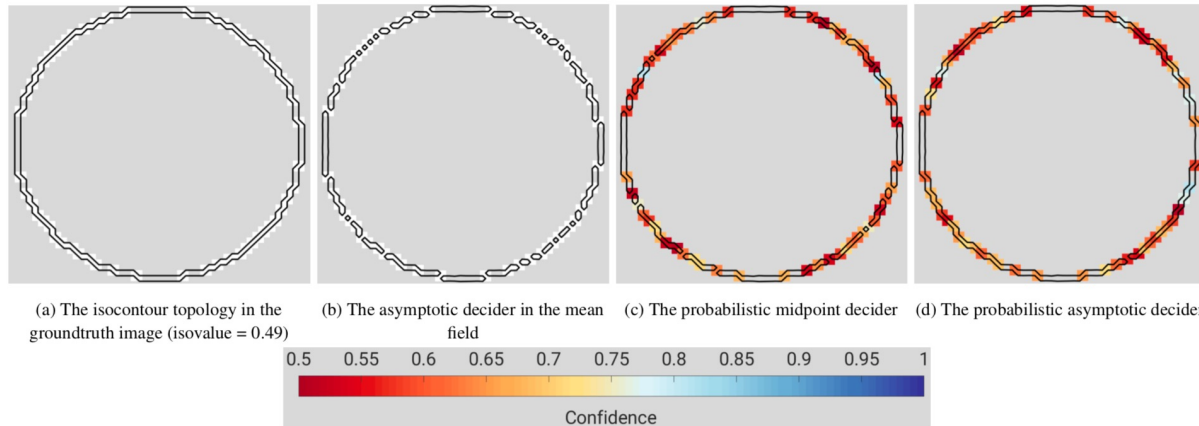


Sudhanshu Sane

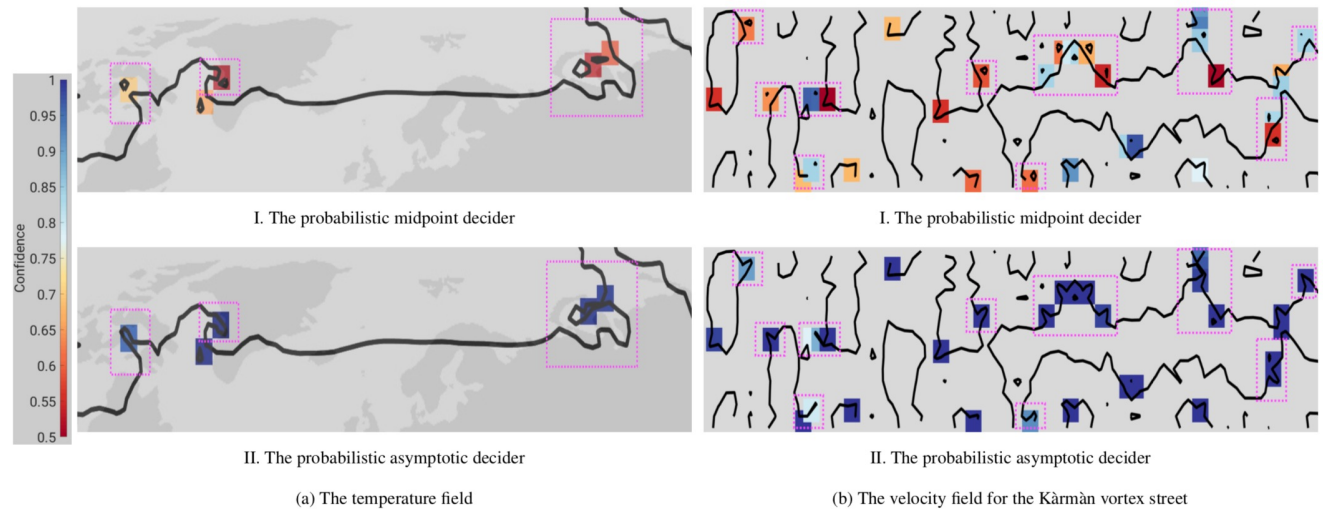


Probabilistic Asymptotic Decider for Topological Ambiguity Resolution in Level-Set Extraction for Uncertain 2D Data

Tushar Athawale and Chris R. Johnson



T. Athawale, C. R. Johnson. "Probabilistic Asymptotic Decider for Topological Ambiguity Resolution in Level-Set Extraction for Uncertain 2D Data," In IEEE Transactions on Visualization and Computer Graphics, Vol. 25, No. 1, IEEE, pp. 1163-1172. Jan, 2019.



Uncertainty Visualization of the Marching Squares and Marching Cubes Topology Cases - VIS 2021

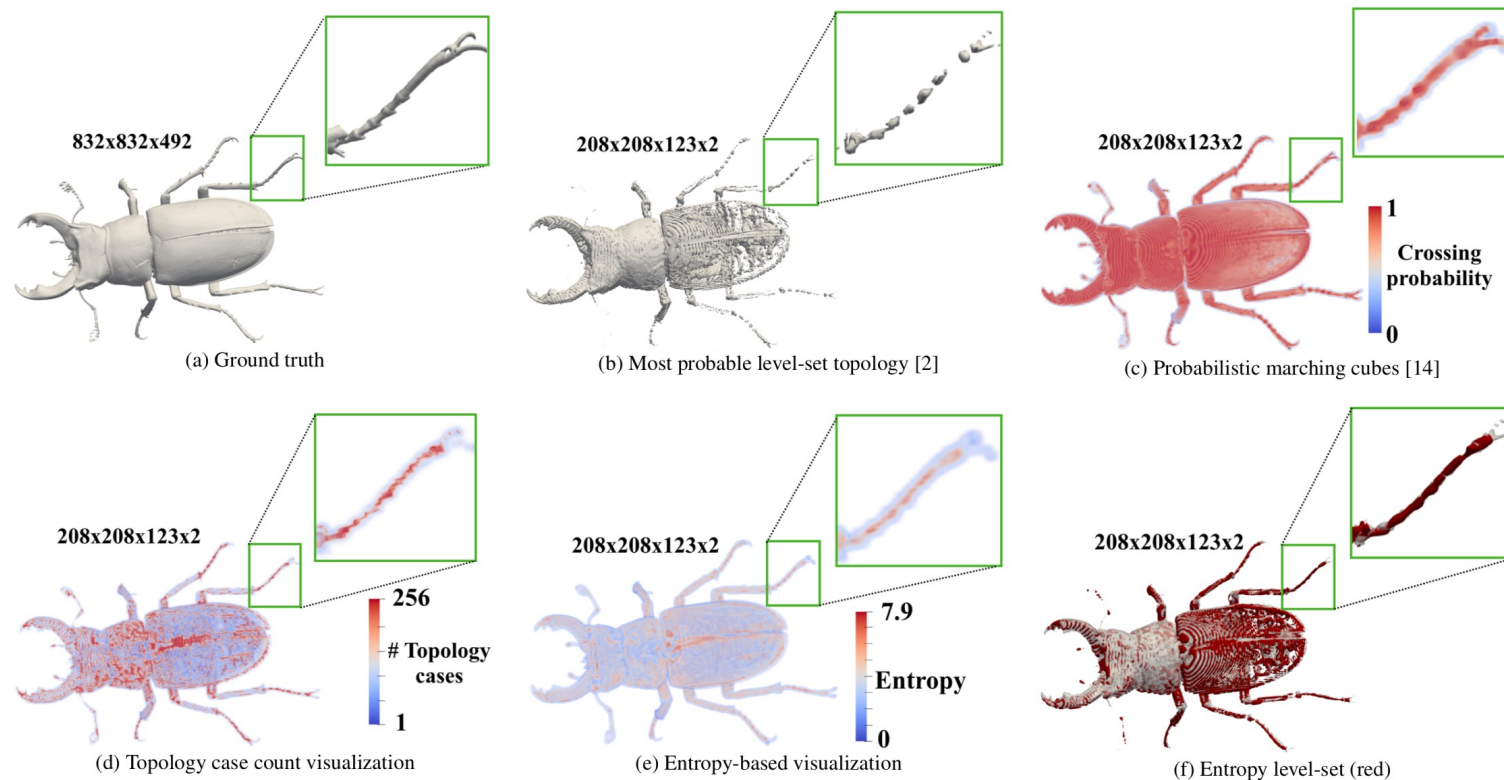
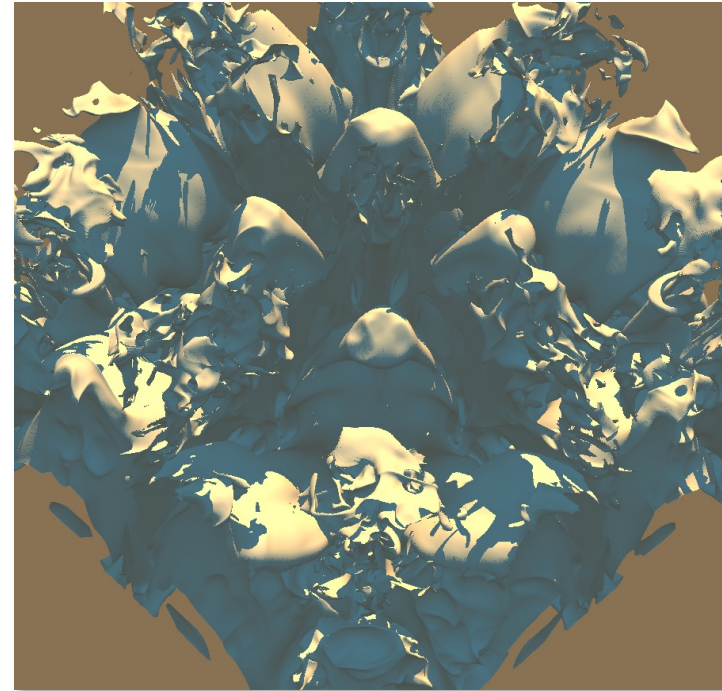
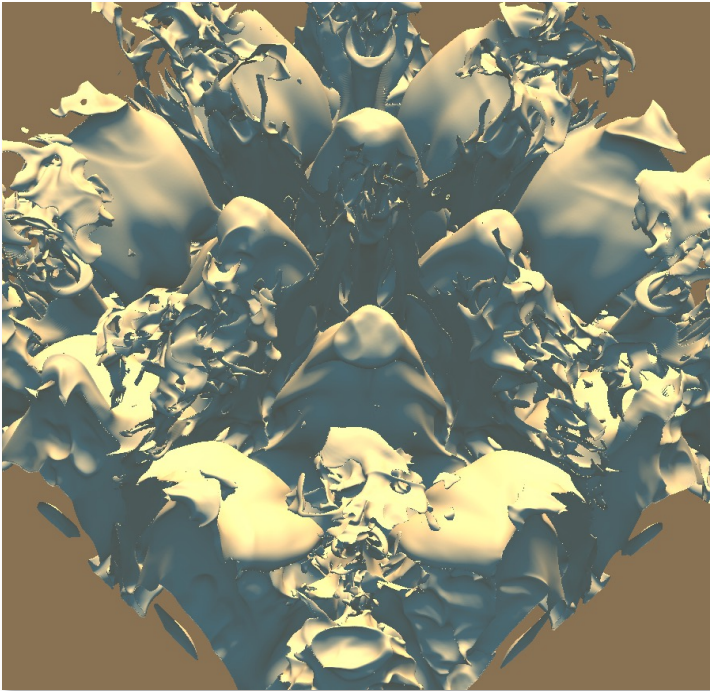


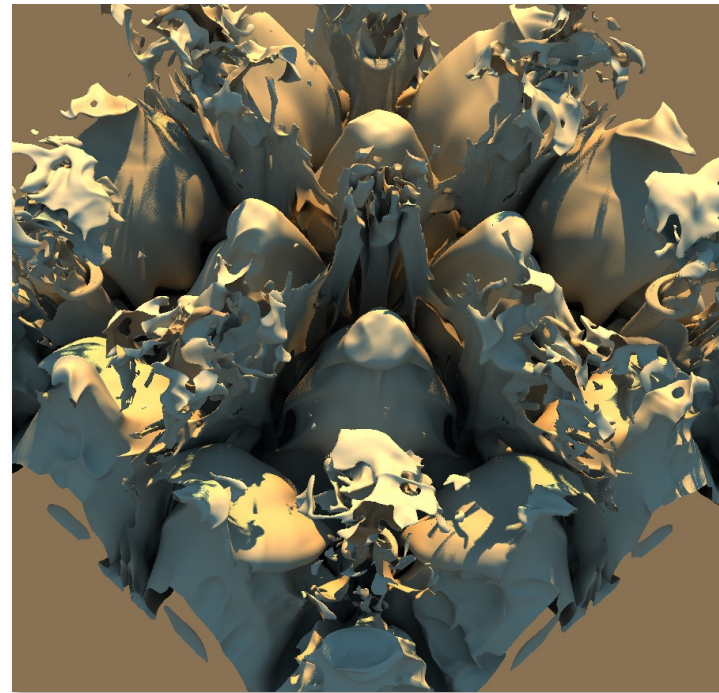
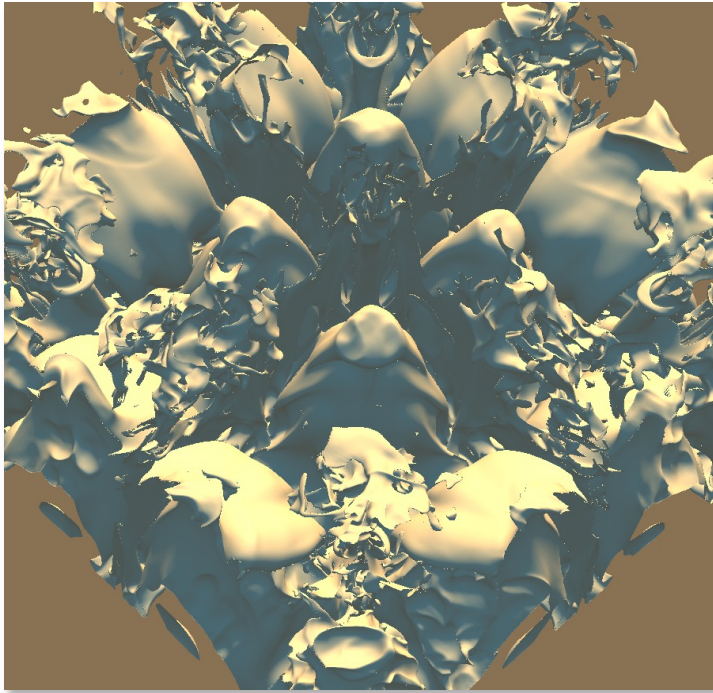
Figure 5: Uncertainty visualizations for the stag beetle [21] hixel dataset at $k = 900$. The noise in the data results in breaking of the beetle leg in image (b). In probabilistic marching cubes, it is difficult to distinguish between the regions of high and topological uncertainty, which is easier using our visualizations in images (d-f). The relatively high sensitivity of the beetle leg topology to noise is detected in images (d-f) by the red regions. In image (f), the most probable level-set (gray) is overlaid with the entropy volume level-set (red) for entropy isovalue 5.

Perceptual Uncertainty

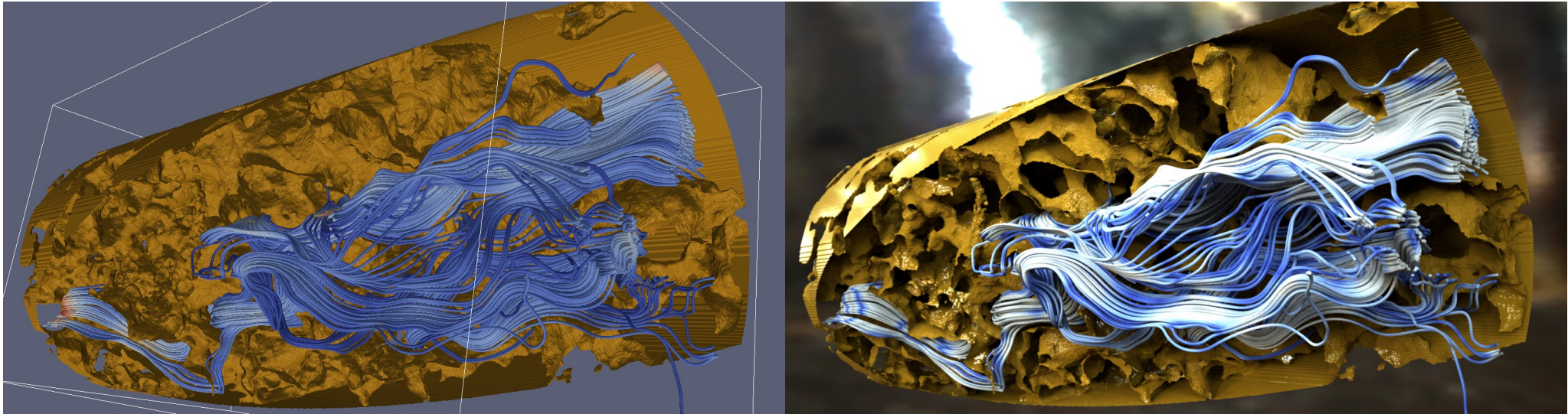


Scientific Computing and Imaging Institute, University of Utah

Perceptual Uncertainty

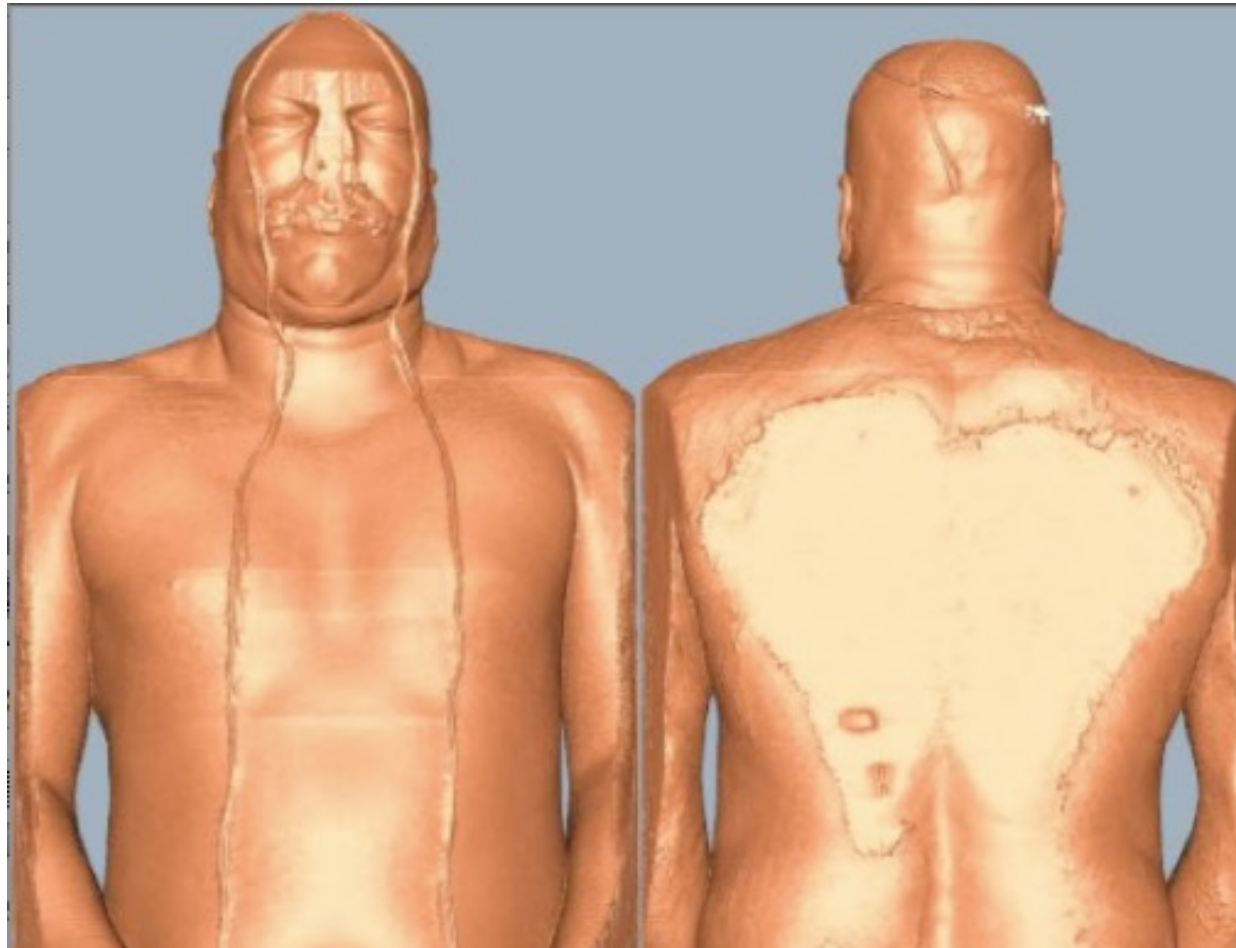


Scientific Computing and Imaging Institute, University of Utah



Path of water through a karst limestone structure of a ground sample analysis visualizing stone porosity and the spatial arrangement of the flow traces.

NIH Visible Male



Visible Human - High Resolution

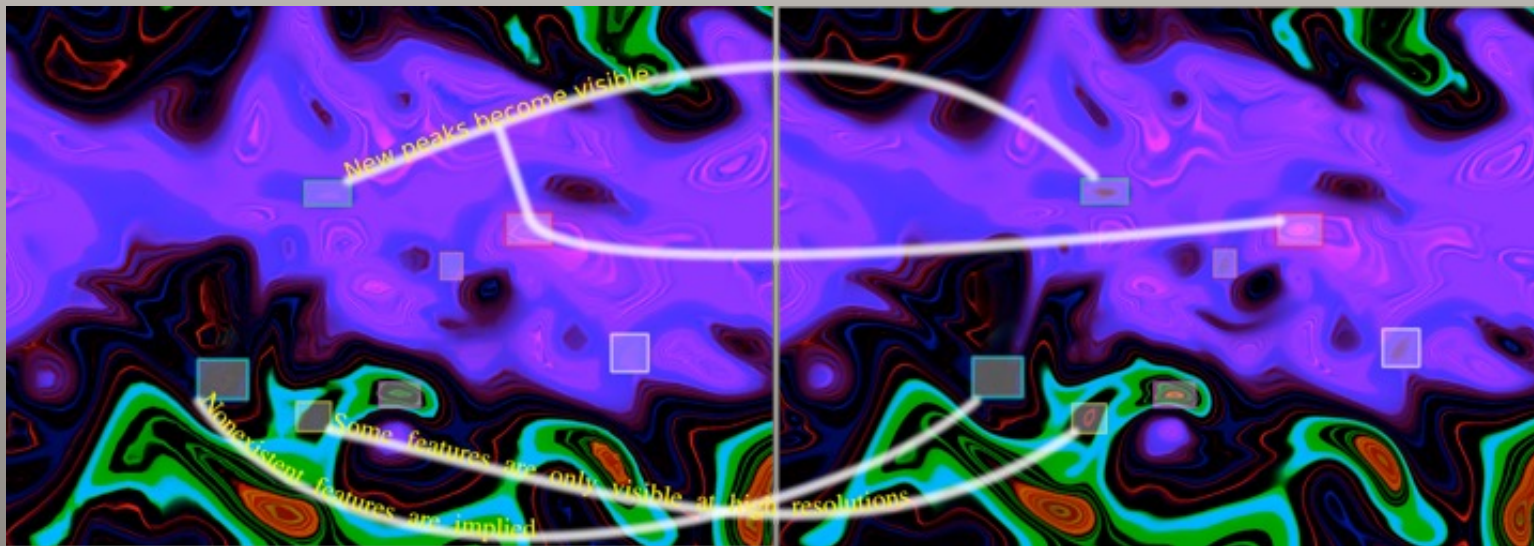




The Need for High Resolution Visualization

“...the data show for the first time how detailed transport and chemistry effects can influence the mixing of reactive scalars. It may be advantageous to incorporate these effects within molecular mixing models. It is worth noting that at present it is impossible to obtain this type of information any other way than by using the type of highly resolved simulation performed here.”

[Jacqueline Chen, Sandia National Laboratories](#)



Lower Resolution

High Resolution

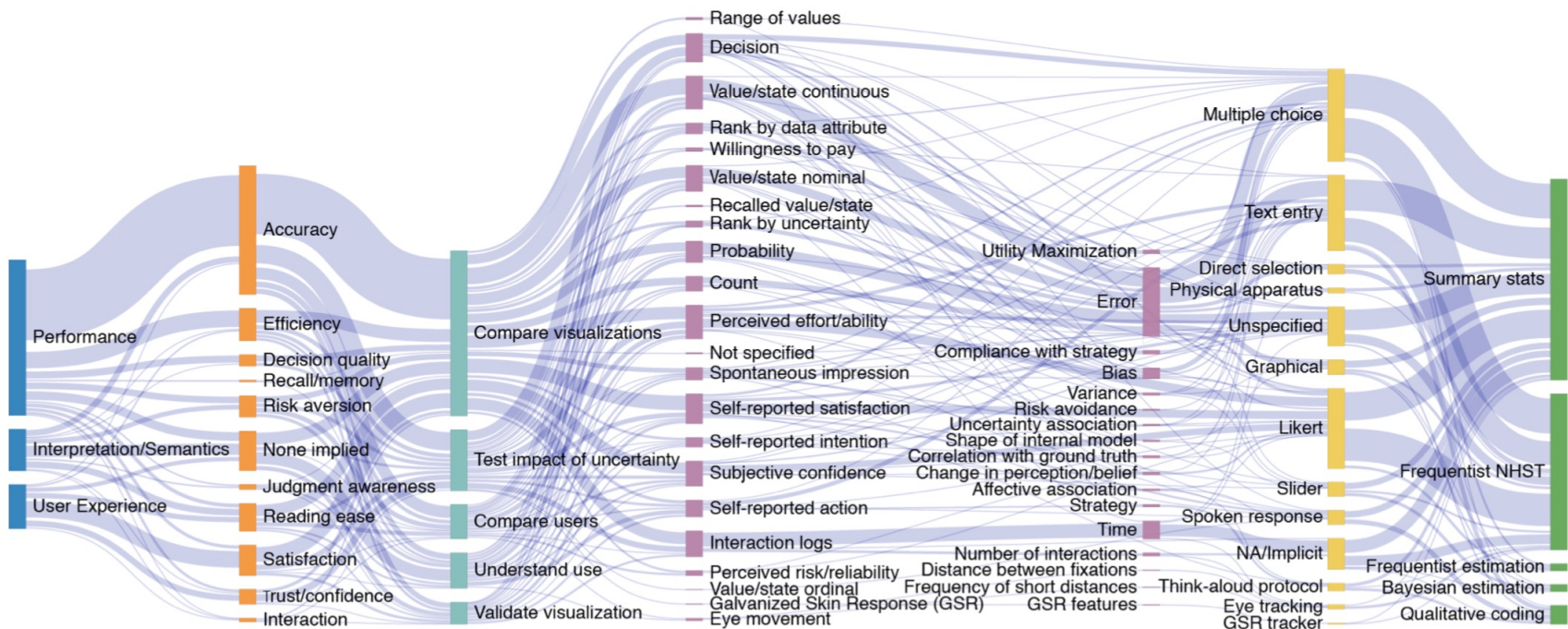


Fig. 2. 372 evaluation paths that we observed across a sample of 86 publications with uncertainty visualization evaluations. The number of inlinks and outlinks differ for some nodes due to the same evaluation path representing multiple codes at a single level (e.g., Analysis).

[In Pursuit of Error: A Survey of Uncertainty Visualization Evaluation](#)

[Jessica Hullman](#), [Xiaoli Qiao](#), [Michael Correll](#), Alex Kale, Matthew Kay
IEEE Trans. Visualization & Comp. Graphics (Proc. InfoVis), 2019



Summary

- Decision making, exploration, and understanding with uncertainty
- Currently, the study of uncertainty is usually performed in along disciplinary lines.
- We need more unified, interdisciplinary treatments of uncertainty:
- Representation, Quantification, Propagation, and Visualization of Uncertainty
- Need to also concentrate on *Certainty*



More Information

www.sci.utah.edu

crj@sci.utah.edu

