## DEPARTMENT OF MATHEMATICS, UNIVERSITY OF UTAH **PDEs for Engineering Students MTH3150 – Section 004 – Spring 2018**

## Midterm 1 formula sheet

The following are some standard thermal properties of materials. Units follow in [brackets].

- u(x,t) Temperature as a function of space and time [temperature]
- e(x,t) Thermal energy density [energy/volume]
- $\phi(x,t)$  Thermal heat flux [energy/(time × area)]
- $\rho(x)$  Mass density [mass/volume]
- c(x) Specific heat [energy/(mass × temperature)]
- $K_0$  Thermal conductivity [energy/(time × temperature × length)]

You may find the following integrals helpful. In all the following, n and m are non-negative integers, and L is any positive number.

$$\int_{0}^{L} \sin\left(\frac{n\pi x}{L}\right) \sin\left(\frac{m\pi x}{L}\right) \, \mathrm{d}x = \begin{cases} 0, & n \neq m \\ L/2, & n = m \end{cases}$$
$$\int_{0}^{L} \cos\left(\frac{n\pi x}{L}\right) \cos\left(\frac{m\pi x}{L}\right) \, \mathrm{d}x = \begin{cases} 0, & n \neq m \\ L/2, & n = m \neq 0 \\ L, & n = m = 0 \end{cases}$$
$$\int_{0}^{L} \cos\left(\frac{n\pi x}{L}\right) \sin\left(\frac{m\pi x}{L}\right) \, \mathrm{d}x = 0 \quad (n > 0)$$
$$\int_{0}^{L} \sin\left(\frac{(2n+1)\pi x}{2L}\right) \sin\left(\frac{(2m+1)\pi x}{2L}\right) \, \mathrm{d}x = \begin{cases} 0, & n \neq m \\ L/2, & n = m \end{cases}$$