Kinetics of Thermal Decomposition of Cubic Ammonium Perchlorate

Sergey Vyazovkin and Charles A. Wight*

Center for Thermal Analysis, Department of Chemistry, University of Utah, 315 S., 1400 E., Salt Lake City, Utah 84112

Received July 13, 1999. Revised Manuscript Received September 7, 1999

The methods of thermogravimetric analysis (TGA) and differential scanning calorimetry (DSC) have been used to study the thermal decomposition of ammonium perchlorate (AP). TGA curves obtained under both isothermal and nonisothermal conditions show a characteristic slowdown at the extents of conversion, $\alpha = 0.30-0.35$. DSC demonstrates that in this region the process changes from an exothermic to an endothermic regime. The latter is ascribed to dissociative sublimation of AP. A new computational technique (advanced isothermal method) has been used to determine the dependence of the effective activation energy ($E_a$) on $\alpha$ for isothermal and nonisothermal TGA data. At $\alpha > 0.1$, the $E_a$ dependencies obtained from isothermal and nonisothermal data are similar. By the completion of decomposition ($\alpha \rightarrow 1$) the activation energy for the isothermal and nonisothermal decomposition respectively rises to $\sim 110$ and $\sim 130 \text{ kJ mol}^{-1}$, which are assigned to the activation energy of sublimation. The initial decomposition ($\alpha \rightarrow 0$) shows the activation energy of 90 kJ mol$^{-1}$ for the isothermal decomposition and 130 kJ mol$^{-1}$ for the nonisothermal decomposition. The difference is explained by different rate-limiting steps, which are nucleation and nuclei growth for isothermal and nonisothermal decompositions, respectively.

Introduction

As a key energetic material for rocket technologies, ammonium perchlorate (AP) continues to inspire new and new research efforts$^{1-10}$ to better understand its thermal decomposition. A significant amount of information on the process had been produced by the 1970s and is covered in several reviews.$^{7-10}$ Among many peculiar features, the most striking was the discovery of low- and high-temperature modes of decomposition. The low-temperature decomposition (LTD) occurs below approximately 300 °C and results only in ~30% decomposition. The high-temperature decomposition (HTD) is observed above 300 °C and leads to complete gasification of AP. At 240 °C, AP undergoes a transition from orthorhombic to cubic crystalline form. The practical interest is primarily focused on the thermal decomposition of cubic AP. The kinetics of this process has been the subject of many studies.$^{1,3,6,11-30}$ Some of the results of these studies are collected in Tables 1 and 2. The reported effective activation energies vary from $\sim 37$ to $260 \text{ kJ mol}^{-1}$. The interpretation of the values is also different. The confusing character of the kinetic information is not very surprising, for the process is known$^{7-10}$

to a tangled interplay of various chemical (solid-state decomposition, reaction of gaseous products with the solid, gas-phase reactions) and physical (morphological transition, diffusion, sublimation, adsorption—desorption) phenomena. The effective activation energy of the thermal decomposition of AP is obviously a composite value determined by the activation energies of elementary steps as well as by the relative contributions of these steps to the overall reaction rate. Because the ratio of these contributions is determined by the experimental conditions, the effective activation energy tends to show a dependence on experimental parameters, e.g., pressure (cf., Tables 1 and 2).

If a multistep process involves steps with different activation energies, the relative contributions of these steps into the overall reaction rate will vary with both temperature and extent of conversion. This means that the effective activation energy will also be a...
function of these two variables. For this reason a solid-
state decomposition cannot be generally described by a
single constant activation energy.\textsuperscript{31} Unfortunately, the
earlier kinetic evaluations did not make the allowance for
possible variations in the activation energy of the
thermal decomposition of AP. The activation energies
were estimated in terms of single-step kinetics, i.e., un-
der the assumption of the constancy of the activation
energy throughout a wide region of the temperatures
and the extents of conversion. Therefore, the values ob-
tained in such a way are in fact averages that are rather
insensitive to the changes in the mechanism and kinet-
ics with the temperature and the extent of conver-
sion.\textsuperscript{31,32}

The isovolumetric methods\textsuperscript{33–35} of kinetic analysis
allow one to reveal a dependence of the activation en-
ergy on the extent of conversion and/or on the tempera-
ture. The analysis of such a dependence is usually very
helpful in drawing mechanistic conclusions about the
process.\textsuperscript{31,36} In this study, we employ a new computa-
tional technique\textsuperscript{37} called the “advanced isovolumetric
method” to explore the multistep kinetics of the thermal
decomposition of cubic AP. The main purpose of this
work is to reveal the variation of the effective activation
energy on the extent of AP conversion and to suggest
its rational mechanistic interpretation.

**Experimental Section**

AP of 99.8% purity (Aldrich) was used as supplied with no
further purification. The diffractometric scanning calorimetry

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline
measurement & \ $P$, atm & \ $T$ region, °C & conversion & kinetic eq & \ $E$, kJ mol\textsuperscript{-1} & ref \\
\hline
pressure vs time, isothermal & vacuum & 240–275 & \textasciitilde30\% & accelerated: & \ log(\(a_1\)) vs \(T\) & 76.9 & 12 \\
 & & & & log(\(a_2\)) vs \(T\) & 71.5 & & \\
 & & & & ln(\(a_1/a_0\)) vs \(T\) & 96.1 & & \\
pressure vs time, isothermal & vacuum & 245–340 & \textasciitilde30\% & decelerated: & \ [-ln(1 – \(a\))]/\(\alpha\) & 85.6 & 15 \\
 & & & & ln(\(a_1/a_0\)) vs \(T\) & 73.2 & & \\
heat flow vs \(T\), nonisothermal & 6.6 × 10\textsuperscript{-5} & 290–410 & complete & \((\alpha = 0.15–0.85)\) & \textasciitilde120 & 104.5 & \\
 & 6.6 × 10\textsuperscript{-4} & & & decelerated: & ln(\(a_1/a_0\)) vs \(T\) & 79.4 & \\
mass vs \(T\), nonisothermal & 1.3 × 10\textsuperscript{-7} & 300–385 & complete & \((\alpha = 0.00–0.96)\) & \textasciitilde120 & 83.6 & \\
heat flow vs \(T\), nonisothermal & vacuum & 220–380 & not reported & \((\alpha = 0–0.93)\) & \textasciitilde120 & 77.8 & \\
mass vs \(T\), nonisothermal & 6.6 × 10\textsuperscript{-3} & 220–340 & complete & ln \(\beta\) vs \(T\) & \textasciitilde120 & 69.0 & \\
heat flow vs \(T\), nonisothermal & 6.6 × 10\textsuperscript{-3} & 270–380 & complete & ln \(\beta\) vs \(T\) & \textasciitilde120 & 88.6 & \\
heat flow vs \(T\), nonisothermal & vacuum & 290–380 & \textasciitilde30–100\% & LTD residue: & \((\alpha = 0–0.9)\) & 125.4 & 23 \\
\hline
\end{tabular}
\caption{Activation Energies for Thermal Decomposition (Dissociative Sublimation) of Ammonium Perchlorate in Vacuum}
\end{table}


(DSC) experiments were performed using a TA Instruments
DSC-2910 apparatus. Samples of AP (2–3 mg) were studied
in both open and closed (pierced) aluminum pans. The ther-
mosgravimetric analysis (TGA) experiments were carried out
using a Rheometrics Model 1000T TGA instrument. To reduce
thermal gradients and exothermic self-heating, the experi-
ments were performed on small (~1 mg) samples. The sample
temperature, which is controlled by a thermocouple, did not
exhibit any significant systematic deviations from the preset
linear temperature programs. This observation is consistent with
the earlier temperature measurements\textsuperscript{38} conducted with a
thermocouple directly embedded in a 45-mg sample of AP
that showed a maximum temperature deviation of \textasciitilde1 °C.
Samples of AP were placed in aluminum pans and heated in a
flowing atmosphere of nitrogen (100 mL min\textsuperscript{-1}). For experi-
ments carried out under nonisothermal conditions, the instru-
ment was programmed to heat the sample from room tempera-
ture at constant heating rates of 5, 7.5, 10, 12.5, and 15 °C
min\textsuperscript{-1}. After an initial period of nonlinear heating (~5 min),
the programmed linear heating rates were established. The
sample temperature versus time curves were used to evaluate
the actual heating rates for the temperature region of AP
decomposition. The values were estimated to be 5.2, 7.6, 10.5,
12.8, and 15.5 °C min\textsuperscript{-1}.

Isothermal experiments were conducted at the temperatures
265, 270, 275, 280, and 285 °C. For isothermal experiments,
the temperature program was optimized to reach the preset
isothermal temperature within 1.5 min without overshooting.
During the next 1.5 min, the sample temperature was regu-
lated to within \pm 1 °C of the set point. For the remainder of
each run, the sample temperature was maintained within
\pm0.05 °C.

**Results**

DSC and TGA. At 240 °C DSC traces (Figure 1) show an
endothermic peak corresponding to the transformation
of AP from the orthorhombic to cubic form. It is
immediately followed by an exothermic effect due to the
thermal decomposition. As seen from DSC data, the
thermal behavior of AP is markedly different in open

and closed pans. In a closed pan, the thermal decomposition of AP is completely exothermic. In an open pan, the exothermic decomposition is followed by an endothermic process in the temperature region 310–375 °C (Figure 1).

The results of the isothermal and nonisothermal TGA experiments are respectively shown in Figures 2 and 3. All the TGA curves (Figures 2 and 3) show a slowdown at ~35% of decomposition which is the salient feature of the process. The isothermal TGA curves show a noticeable induction period (Figure 2). As seen in Figure 3, the nonisothermal decomposition of AP occurs at temperatures above 240 °C, i.e., when AP is in its cubic form.

**Kinetic Computations.** The kinetics of solid-state decompositions are customarily described by the basic kinetic equation

\[ \frac{d\alpha}{dt} = A \exp\left(-\frac{E_a}{RT}\right) \theta(\alpha) \]  

where \( A \) (preexponential factor) and \( E_a \) (the activation energy) are Arrhenius parameters, \( \alpha \) is the extent of conversion, \( \theta(\alpha) \) is the reaction model, \( t \) is the time, \( T \) is the temperature, and \( R \) is the gas constant. Vyazovkin developed an advanced isoconversional method,\(^{37}\) which is based on the assumption that the reaction model is independent of the heating program, \( T(t) \). According to this method, for a set of \( n \) experiments carried out at different heating programs, the activation energy is determined at any particular value of \( \alpha \) by finding the value of \( E_a(\alpha) \) that minimizes the function

\[ \Phi(E_a) = \sum_{i=1}^{n} \sum_{j=1}^{n} \mathcal{J}[E_a, T(t_i)] \]  

Henceforth, the subscript \( \alpha \) denotes the values related to a given extent of conversion. In eq 2, the integral

\[ \mathcal{J}[E_a, T(t_i)] = \int_0^\alpha \exp\left(-\frac{E_a}{RT(t_i)} \right) dt \]  

is evaluated numerically for a set of experimentally recorded heating program, \( T(t_i) \). The minimization procedure is repeated for each value of \( \alpha \) to find the dependence of the activation energy on the extent of conversion. An advantage of the advanced isoconversional method is that it uses the actual sample temperature measurements. This makes it possible to account for uncontrollable temperature variations such as those that occur during the initial temperature jump in an isothermal experiment and/or those that result from self-heating/cooling.\(^{37}\)

The \( E_a(\alpha) \) dependences evaluated by the isothermal and nonisothermal TGA data are depicted in Figure 4. The \( E_a(\alpha) \) dependence derived from the nonisothermal experi-

ment demonstrates two distinct stages in the thermal decomposition of AP. The first stage ($\alpha < 0.3$) is related to the exothermic process. This stage is characterized by a decrease in the activation energy from $\sim 130$ to 95 kJ mol$^{-1}$. The second stage ($\alpha > 0.3$) corresponds to the endothermic process that shows an increase in the activation energy from 95 to $\sim 130$ kJ mol$^{-1}$. The $E_R$ dependence evaluated by the isothermal data can be conventionally divided into three stages: at the first stage ($\alpha < 0.1$), $E_R$ rises from $\sim 90$ to $\sim 100$ kJ mol$^{-1}$; the second stage is characterized by a decrease in $E_R$ from $\sim 100$ to $\sim 80$ kJ mol$^{-1}$; the third stage shows an increase in $E_R$ from 80 to 110 kJ mol$^{-1}$. At $\alpha > 0.1$ both isothermal and nonisothermal $E_R$-dependencies are quite similar.

### Discussion

**DSC and TGA.** Analysis of the literature DTA/DSC data$^{32,27,29,30,40-43}$ suggests (Table 3) that the thermal decomposition of AP usually appears as a sequence of two events (peaks), the first of which is exothermic. The second peak may appear as an exothermic or endothermic event, depending on the experimental conditions. When decomposition occurs under the conditions that retard the escape of reaction gases from the reaction zone (elevated pressures, closed pans, static atmosphere, etc), the second event appears as an exothermic peak. Conversely, under the conditions that facilitate the removal of gaseous products (vacuum, open pans, high flow rates of a carrier gas), the second event appears as an endothermic peak. Therefore, when the second event appears as an exothermic peak, it should rather be ascribed to the secondary reactions of gas-phase products than to the solid-state decomposition of AP.

Obviously the open pan DSC runs most closely reproduce the conditions of TGA experiments. According to the open pan DSC data, the thermal decomposition of AP passes sequentially an exothermic and endothermic stage. By comparing TGA and DSC curves (Figure 5) we can see that the point when decomposition turns into the endothermic stage is correlated with the slowdown ($\alpha = 0.30-0.35$) observed in the TGA experiments. The solid residue formed by this moment is chemically identical to the original AP.

Table 3. Thermal Events Observed in DTA/DSC Experiments on Thermal Decomposition of Ammonium Perchlorate

<table>
<thead>
<tr>
<th>thermal events</th>
<th>pan type</th>
<th>atmosphere</th>
<th>pressure, atm</th>
<th>ref</th>
</tr>
</thead>
<tbody>
<tr>
<td>exo/endo</td>
<td>static, vacuum</td>
<td>1.3 × 10$^{-3}$</td>
<td>40</td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>static, N$_2$</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>static, N$_2$</td>
<td>4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>static, NH$_3$</td>
<td>4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>Pt</td>
<td>He flow, 17 mL min$^{-1}$</td>
<td>1</td>
<td>22</td>
</tr>
<tr>
<td>exo/endo</td>
<td>Al</td>
<td>static, He, N$_2$, O$_2$</td>
<td>1</td>
<td>27</td>
</tr>
<tr>
<td>exo/endo</td>
<td>static, He, O$_2$</td>
<td>4–51</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>static, He</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>static, He</td>
<td>4–51</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>Al, pierced</td>
<td>1</td>
<td>29</td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>Pt</td>
<td>static, air</td>
<td>1</td>
<td>41</td>
</tr>
<tr>
<td>exo/endo</td>
<td>Pt</td>
<td>continuous pumping</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>Pt</td>
<td>static, vacuum</td>
<td>6.6 × 10$^{-3}$</td>
<td>42</td>
</tr>
<tr>
<td>exo/endo</td>
<td>pierced</td>
<td>N$_2$, air</td>
<td>1</td>
<td>30</td>
</tr>
<tr>
<td>single exo</td>
<td>sealed</td>
<td>static, vacuum</td>
<td>6.6 × 10$^{-3}$</td>
<td>3</td>
</tr>
<tr>
<td>single endo</td>
<td>pierced</td>
<td>static, vacuum</td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>sealed</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>exo/endo</td>
<td>Al, open</td>
<td>N$_2$ flow, 100 mL min$^{-1}$</td>
<td>1</td>
<td>43</td>
</tr>
<tr>
<td>exo/endo</td>
<td>Al, pierced</td>
<td>N$_2$ flow, 100 mL min$^{-1}$</td>
<td>1</td>
<td>present work</td>
</tr>
</tbody>
</table>

**Figure 5.** Combined plot of TGA and DSC experiments carried out at a heating rate of 5 °C min$^{-1}$.  

Kinetics of Cubic Ammonium Perchlorate

Scanning electron microscopy has been used to directly observe the development of the surface area during decomposition. The experiments demonstrated that AP heated to the first exothermic peak (27% of decomposition) is a porous material with the square holes whose shape reflects the crystal structure. Continued heating past the exotherm (41% of decomposition) showed considerable sublimation that was observed as smoothing of the square holes.

On the basis of both literature data and data of our TGA and DSC experiments, the solid-state thermal decomposition of AP involves two major stages. In the DSC experiments, the first stage appears as an exothermic peak that corresponds to the formation of thermodynamically stable products such as Cl₂, HCl, H₂O, O₂, N₂O, and NO. In TGA experiments, the completion of this stage is observed either as the cessation (LTD) or as the slowdown (HTD) of the mass loss at ~30% of decomposition. The second stage appears as an endothermic DSC peak that represents dissociative sublimation of AP to ammonia and perchloric acid. Sublimation and exothermic decomposition are most likely to occur throughout the whole process. Since the sublimation rate is proportional to the surface area, the contribution of sublimation is practically negligible (under ambient pressures) at low extents of conversion, but it increases dramatically during decomposition and ultimately outweighs the exothermic contribution of decomposition.

Kinetics. The previous section was concerned with the qualitative regularities of the thermal decomposition of AP. Here, the process is discussed in quantitative terms of the variation of the effective activation energy with the extent of conversion. As seen in Figure 4, the Eₐ dependencies derived from the isothermal and nonisothermal TGA experiments are quite similar at α > 0.1. Note that some quantitative differences in the respective Eₐ dependencies are unavoidable, because for technical reasons, isothermal and nonisothermal experiments have to be conducted in different temperature regions.

Qualitatively different kinetics are observed at α < 0.1. To explain this difference we have to take into account that the isothermal decompositions show an induction period. In solid-state decompositions, the induction period is usually associated with nucleation, i.e., the formation of reaction centers (nuclei). This process is followed by nuclei growth that is observed as an acceleration in the decomposition rate. Depending on the rates of nucleation and nuclei growth, the initial decomposition rate may be limited by either of the two processes. The overall rate of decomposition is determined by the concentration of nuclei. Under nonisothermal conditions, the faster the heating rate is, the higher the temperature corresponding to the same concentration of nuclei is. Our nonisothermal experiments have been performed at the heating rates not faster than 15.5 °C min⁻¹. In isothermal experiments, the preset temperatures were reached in ~1.5 min. This corresponds to an average heating rate of ~170 °C min⁻¹. Given such fast heating rates, we may expect the concentration of nuclei at the beginning of decomposition to be markedly smaller in the isothermal experiments than in the nonisothermal experiments. Therefore, the initial rate of decomposition is likely to be limited by nucleation in the isothermal experiments and by nuclei growth in the nonisothermal experiments. Then, the values of Eₐ at α → 0 derived from the isothermal and nonisothermal data provide respective estimates for the activation energy of nucleation (~90 kJ mol⁻¹) and nuclei growth (~130 kJ mol⁻¹) in the thermal decomposition of AP. These estimates agree well with the data of Jacobs and Ng, who report activation energies around 90 and 120 kJ mol⁻¹ for the respective processes of nucleation and growth in AP. Although the situation when the activation energy for nucleation is lower than that for growth is not very frequent, it has been observed for thermal decompositions of other solids such as carbonic carbonate hexahydrate, mercury oxalate, and copper(II) malonate. Therefore, the ascending Eₐ dependence for the isothermal decomposition at α = 0–0.1 reflects the transition of a rate-limiting step from nucleation to nuclei growth. Further variation in Eₐ (α < 0.1) is quite similar to that observed under the nonisothermal conditions.

The exothermic decomposition (α = −0.3) gives rise to porous AP. The development of the high surface area favors adsorption of the gaseous decomposition products. As a result, the exothermic decomposition is likely to become controlled by mass-transfer along the solid surface and desorption, which are usually characterized by relatively low activation energies. This seems to be a plausible explanation for the observed decrease in the effective activation energy (nonisothermal data in Figure 5) as α approaches 0.3. However, the initial decomposition is likely to be kinetically controlled. Then, the effective value of Eₐ at α = 0–0.1 gives us an estimate for the activation energy of the thermal decomposition of AP. This value is ~130 kJ mol⁻¹ for the nonisothermal decomposition, and ~90 kJ mol⁻¹ for the isothermal decomposition. Therefore the Eₐ dependence observed in the region of α = 0–0.3 reflects a change from kinetically controlled decomposition to decomposition controlled by a mass-transfer process. At α → 0.3 the decomposition is still exothermic but markedly slows down. Therefore, the effective activation energy at α = 0.3 may give us an upper estimate for the activation energy of the mass transfer process responsible for the removal of gaseous products from porous AP. The more realistic (i.e., smaller) value (~80 kJ mol⁻¹) is found from the isothermal data.

The results of our kinetic analysis suggest that even the initial (exothermic) decomposition shows multistep kinetics. Nevertheless, in the majority of earlier kinetic analyses, this process was treated as a single-step. For this reason, we cannot directly compare the averaged activation energies (Table 1) with the Eₐ dependencies found in the present work (Figure 4). Although several workers observed nonlinear Arrhenius dependences:

Figure 6. Surface plot of the activation energy estimated from the Manelis–Rubtsov model by varying the extent of conversion and temperature.

encies, only Manelis and Rubtsov\textsuperscript{19} proposed a multistep kinetic model for the net process of the solid-state decomposition of AP

\[
\frac{da}{dt} = k_1(1 - a)^3 + k_2a(1 - a)^2
\]  

(4)

We used this empirical model to derive the respective \(E_a\) dependence as follows:

\[
E_a = -R \left[ \frac{d \ln \alpha}{dT} \right]_{T_\alpha} = \frac{E_1k_1 + E_2k_2\alpha}{k_1 + k_2\alpha}
\]  

(5)

Substitution of experimentally determined\textsuperscript{19} rate constants \(k_1 = 10^8\ \text{exp}(-15098/7\text{)}\ (\text{s}^{-1})\) and \(k_2 = 10^{4.5}\ \text{exp}(-9109/7\text{)}\ (\text{s}^{-1})\) into eq 5 gives rise to the series of isothermal \(E_a\) dependencies depicted as a surface plot in Figure 6. In the experiments conducted by Manelis and Rubtsov, AP decomposed only up to 30%. Therefore, \(\alpha = 1\) in their model (eq 4) corresponds to \(\sim 30\%\) of AP decomposition (the exothermic process). In our experiments, AP decomposes completely, i.e., \(\alpha = 1\) corresponds to 100% of AP decomposition. To make the \(E_a\) dependencies obtained by eq 5 comparable to our data (Figure 4), the \(\alpha\) axis (Figure 6) has been properly rescaled after calculations. As we can see in Figure 6, the Manelis–Rubtsov model yields \(E_a\) dependencies that are very similar to the dependence we obtained from nonisothermal experiments (Figure 4).

While derived from isothermal data, the activation energies reported by Manelis and Rubtsov do not explicitly account for a lower activation energy in the induction period that we observed for the isothermal decomposition of AP (Figure 4). Perhaps, this short process went unnoticed because Manelis and Rubtsov fit eq 4 to the data related to the full range of the extents of conversion (i.e., \(\alpha = 0 \sim 1\)) without performing a separate fit for the induction period. On the other hand, we cannot rule out that for Manelis and Rubtsov’s sample the activation energy of nucleation was close to that for nucleation growth. Because the process of nucleation is extremely sensitive to the prehistory of a solid, the AP samples with different prehistories are likely to show different activation energies for nucleation. For instance, the values of the activation energy of nucleation in orthorhombic AP have been reported to be 155,\textsuperscript{21} 210,\textsuperscript{21} and 290\textsuperscript{21} kJ mol\textsuperscript{-1}. For cubic AP, Jacobs and Ng\textsuperscript{17} reported the activation energy for the induction period to vary with the crystal sizes and types of impurities as follows: 92 (large single crystals), 85 (small plate-like single crystals), 106 (crystals doped by Ba\textsuperscript{2+}), and 128 (crystals doped by SO\textsubscript{4}\textsuperscript{2-}) kJ mol\textsuperscript{-1}.

The development of high surface area plays a crucial role in changing the process from an exothermic to an endothermic regime at \(\alpha > 0.3\). The rate of sublimation is directly proportional to the surface area. Therefore, the progress of the thermal decomposition of AP at \(\alpha > 0.3\) is determined by the competition of dissociative sublimation and the exothermic decomposition. The coexistence of these two processes is supported by the fact that the endothermic effect estimated by DSC (140 kJ mol\textsuperscript{-1} after correcting for preceding mass loss) is only about 60% of experimentally found\textsuperscript{22} enthalpy of sublimation, 242 ± 8 kJ mol\textsuperscript{-1}.

The activation energy of sublimation (∼120 kJ mol\textsuperscript{-1}) was theoretically and experimentally found\textsuperscript{22} to be \(1/2\) of the enthalpy of sublimation. Because this value is greater than that for the mass-transfer processes (∼80 kJ mol\textsuperscript{-1}), the relative contribution of sublimation to the overall process rate increases with the temperature. For the nonisothermal data, the variation of the activation energy with temperature can be easily followed by replacing the \(\alpha\) values with the respective \(T_\alpha\) values related to an average heating rate used for kinetic computations (Figure 4). It is clear from Figure 4 that at \(\alpha > 0.3\) the effective activation energy increases with the temperature. The value of \(E_a\) corresponding to the maximum temperature represents the greatest contribution of sublimation to the overall rate of decomposition. Consequently, the effective value of \(E_a\) at \(\alpha \to 1\) gives us an estimate for the activation energy of sublimation. This value is about 130 kJ mol\textsuperscript{-1} for the nonisothermal data.

The \(E_a\) dependence derived from the isothermal data (Figure 4) also demonstrates an increase in the effective activation energy in that region. The value of \(E_a\) at \(\alpha \to 1\) is 110 kJ mol\textsuperscript{-1}, which is reasonably consistent with the activation energy of sublimation obtained from the nonisothermal data. Overall, the kinetics of the thermal decomposition of AP seems to be quite similar under isothermal and nonisothermal conditions at \(\alpha > 0.3\). Both nonisothermal (130 kJ mol\textsuperscript{-1}) and isothermal (110 kJ mol\textsuperscript{-1}) estimates are in accord with the activation energy of sublimation determined by Jacobs and Russel-Jones\textsuperscript{23} (125 kJ mol\textsuperscript{-1}).

Table 2 collects the values of the activation energy for the thermal decomposition of AP in a vacuum, i.e.,
under conditions when the process is controlled by dissociative sublimation. Analysis of the data from Table 2 suggests that the value obtained by Jacobs and Russel-Jones stands out as being noticeably greater. However, we should take into account that Jacobs and Russel-Jones used in their experiments the residue of LTD (i.e., 30% decomposed porous AP), whereas all other experiments were performed on undecomposed AP. In our experiments, we observe sublimation (endothermic DSC peak) only after 30% of decomposition. Then, our measurements should yield the activation energy of sublimation of the LTD residue and should rather be consistent with the value determined by Jacobs and Russel-Jones. They also found that sublimation of the LTD residue proceeds with the same activation energy under ambient pressures and in a vacuum.

The difference in the values of the activation energy for sublimation of undecomposed AP and of LTD residue may be the evidence that the mechanism of sublimation changes with the development of the high surface area in AP. For undecomposed AP, Aleksandrov and Khairetdinov suggest a stepwise mechanism of sublimation. According to this mechanism, sublimation of the LTD residue proceeds with the same activation energy under ambient pressures and in a vacuum.

The difference in the values of the activation energy for sublimation of undecomposed AP and of LTD residue may be the evidence that the mechanism of sublimation changes with the development of the high surface area in AP. For undecomposed AP, Aleksandrov and Khairetdinov suggest a stepwise mechanism of sublimation. According to this mechanism, sublimation of the LTD residue proceeds with the same activation energy under ambient pressures and in a vacuum. The proposed model suggests the activation energy to be $1/3$ of the enthalpy of sublimation, i.e., $\sim 80$ kJ mol$^{-1}$, which is consistent with the values reported for sublimation of undecomposed AP (Table 2).

**Conclusion**

On the basis of our kinetic analysis as well as on the literature data, we can propose a relatively simple kinetic scheme (Figure 7) for the thermal decomposition of cubic AP. The process starts from nucleation that appears as an induction period on isothermal kinetic curves. The activation energy of nucleation is an ambiguous value that depends on the prehistory of an AP sample. As soon as the amount of nuclei reaches the critical mass, thermal decomposition becomes controlled by nuclei growth with the activation energy of about 130 kJ mol$^{-1}$. At this stage ($\alpha < 0.3$), the overall process, which includes thermal decomposition and quite likely sublimation, is exothermic. The contribution of sublimation is insignificant under ambient pressures. Nevertheless, it increases with decrease of pressure and may become prevailing in a vacuum. The activation energy of sublimation in a vacuum appears to be about 80–90 kJ mol$^{-1}$. The high surface area of porous AP formed during the exothermic decomposition causes the process to turn into a slow regime controlled by mass transfer with an activation energy less than 80 kJ mol$^{-1}$. Processes that occur at the late stages ($\alpha > 0.3$) are governed by competition between the mass transfer controlled decomposition and sublimation. In open systems, the latter makes the overall process endothermic. The difference in the activation energy for sublimation of porous and of undecomposed AP is most likely due to the change in the mechanism of sublimation.

**Acknowledgment.** This research is supported in part by the University of Utah Center for Simulations of Accidental Fires and Explosions, funded by the Department of Energy, Lawrence Livermore Laboratory, under subcontract B341493, and by the Office of Naval Research under contract No. N00014-95-1-1339).