

# Shape from Silhouettes III

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CS 6320, Spring 2015

(credit: slides modified from Marc Pollefeys  
UNC Chapel Hill, some of the figures and slides are adapted  
from M. Pollefeys, J.S. Franco, J. Matusik's presentations,  
and referenced papers)



# Outline

- Silhouettes
  - basic concepts
  - extract silhouettes
  - fundamentals about using silhouettes
  - reconstruct shapes from silhouettes
  - use uncertain silhouettes
  - calibrate from silhouettes
- Perspectives and cool ideas



# Silhouette Consistency Constraints: Forbes et al.

- <http://www.dip.ee.uct.ac.za/~kforbes/Publications/Publications.html>
- Keith Forbes, Anthon Voigt and Ndimi Bodika. [Using Silhouette Consistency Constraints to Build 3D Models](#). In *Proceedings of the Fourteenth Annual Symposium of the Pattern Recognition Association of South Africa (PRASA 2003)*, November 2003.
- Keith Forbes, Anthon Voigt and Ndimi Bodika. [Visual Hulls from Single Uncalibrated Snapshots Using Two Planar Mirrors](#). In *Proceedings of the Fifteenth Annual Symposium of the Pattern Recognition Association of South Africa (PRASA 2004)*, November 2004.



# Merging sets of silhouettes (Forbes et al.)

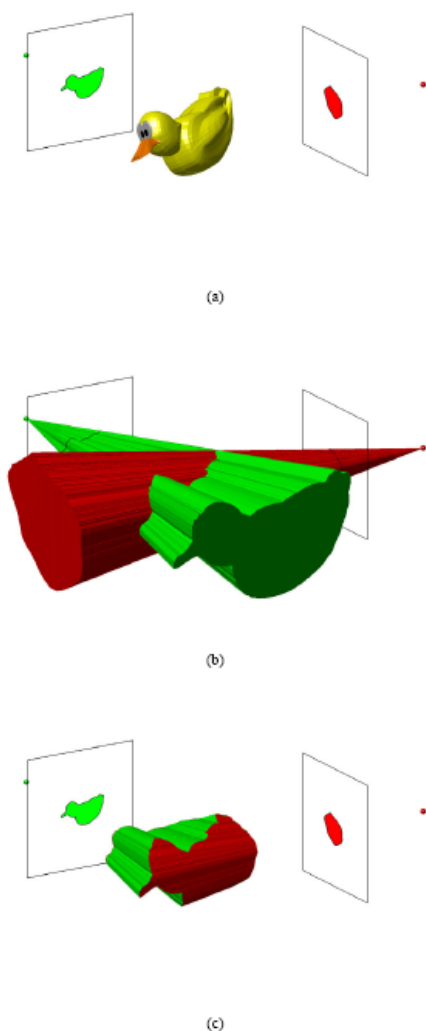


Figure 1: Two silhouette views of a duck showing (a) the cameras, each represented by a camera centre and image plane, (b) the visual cones corresponding to each of the two silhouettes, and (c) the visual hull corresponding to the two silhouettes.

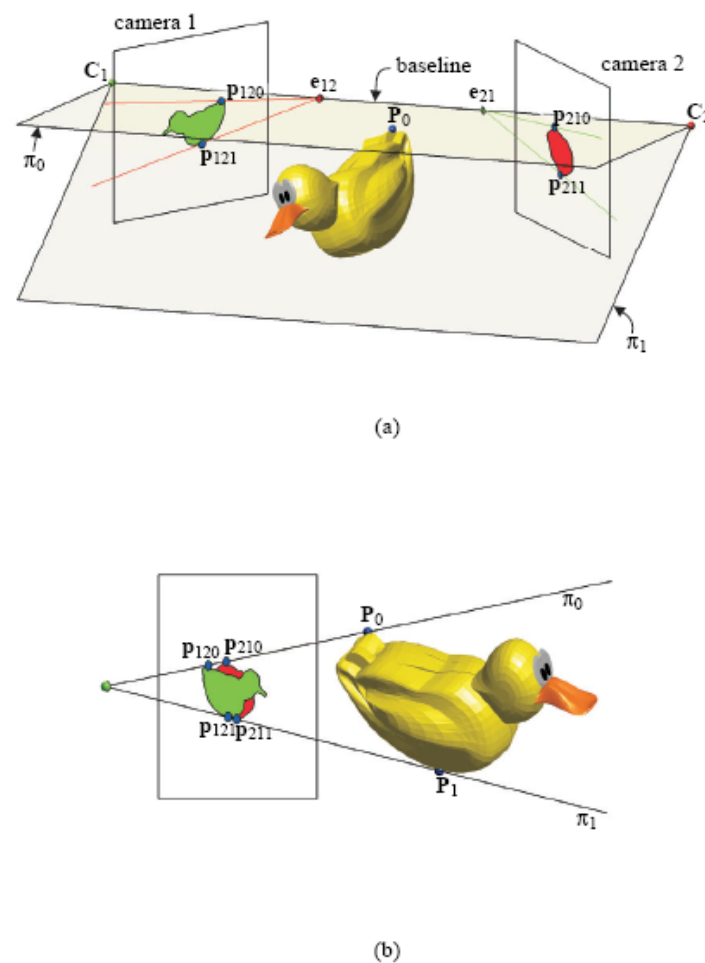


Figure 2: Two views of the epipolar geometry of a scene: (a) shows a front view, and (b) shows a side view looking onto the scene in a direction parallel to the baseline.



## Review Epipolar Geometry Matrix Form

$$\mathbf{p} \cdot [\mathbf{t} \times (\mathcal{R}\mathbf{p}')] = 0$$

$$\vec{a} \times \vec{b} = [a_x] \vec{b}$$

$$\mathbf{p}^T [t_x] \mathcal{R} \mathbf{p}' = 0$$

$$\mathcal{E} = [t_x] \mathcal{R}$$

$$\mathbf{p}^T \mathcal{E} \mathbf{p}' = 0$$



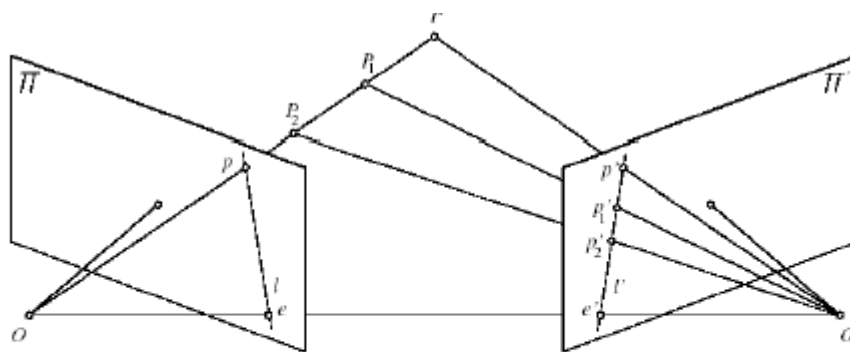
# Review Epipolar Geometry

## The Essential Matrix

Matrix that relates image of point in one camera to a second camera, given translation and rotation.

$$\mathcal{E} = [t_x] \mathfrak{R}$$

$$p^T \mathcal{E} p' = 0$$



$$\vec{a} \times \vec{b} = [a_x] \vec{b}$$

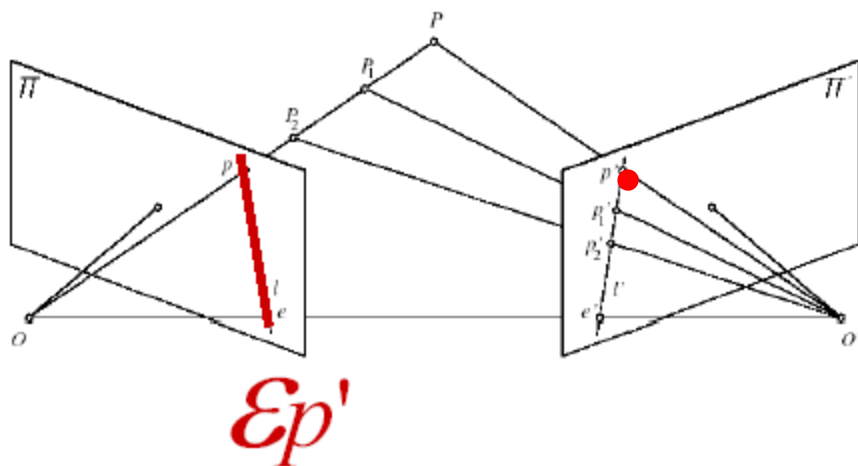


# Review Epipolar Geometry

## The Essential Matrix

$\mathcal{E}p'$  is the epipolar line corresponding to  $p'$  in the left camera.

$$au + bv + c = 0$$



$$p = (u, v, 1)^T$$

$$l = (a, b, c)^T$$

$$l \cdot p = 0$$

$$\mathcal{E}p' \cdot p = 0$$

$$p^T \mathcal{E}p' = 0$$

Similarly  $\mathcal{E}p$  is the epipolar line corresponding to  $p$  in the right camera



# Review Epipolar Geometry (Ch 10)

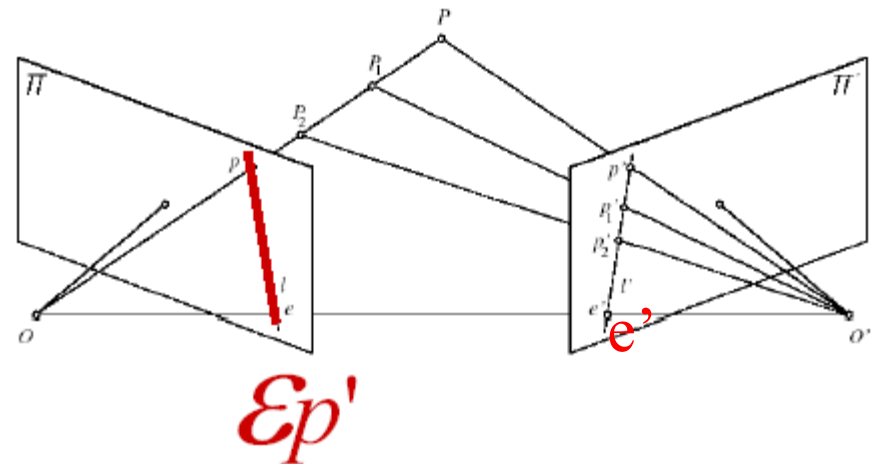
## Calculation of Epipoles

$$\mathcal{E}e' = [t_{\times}]Re' = 0$$

$$\text{Similarly, } \mathcal{E}^T e = R^T [t_{\times}]^T e = -R^T [t_{\times}]e = 0$$

Essential Matrix is singular with rank 2

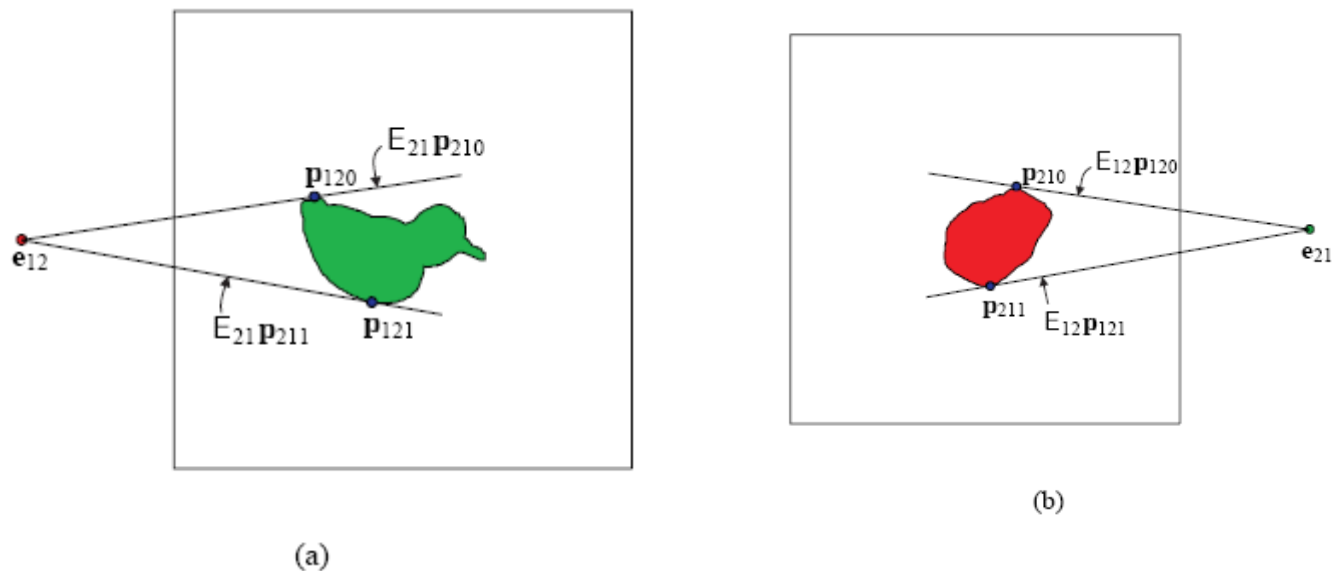
Epipoles are left and right nullspaces of  $\mathcal{E}$   
 (SVD:  $U\Sigma V^T$ , select last column of  $V$ )







# Merging sets of silhouettes (Forbes et al.)

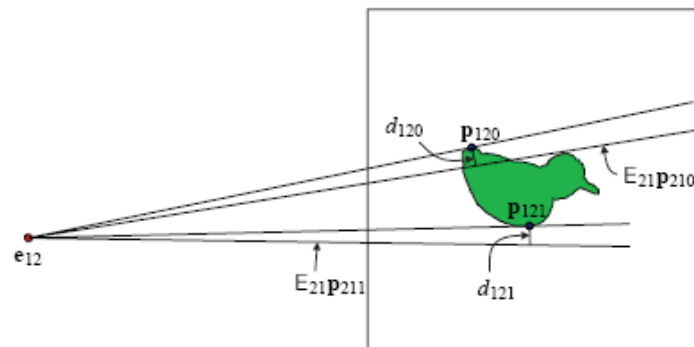


**Figure 3:** The epipolar tangency constraint: the epipolar tangent line touches the silhouette at the projection of the frontier point, as shown in (a) and (b); the projection of this line onto the image plane of the opposite camera is constrained to coincide with the opposite epipolar tangency line.

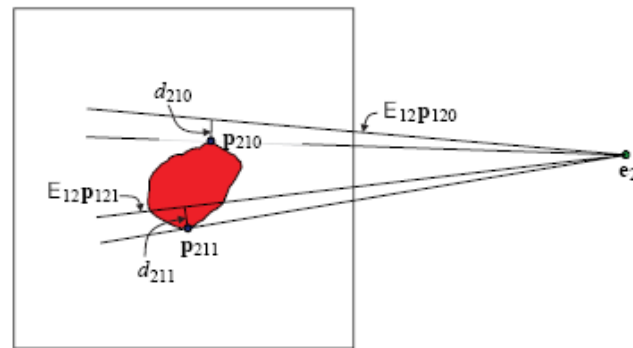
- $\mathbf{P}_0, \mathbf{P}_1$ : Frontier points
- $\mathbf{p}_{120}, \mathbf{p}_{210}$  projections of  $\mathbf{P}_0$  ( $\mathbf{p}_{121}, \mathbf{p}_{211} \rightarrow \mathbf{P}_1$ )
- Epipolar geometry: line  $\mathbf{e}_{12}\mathbf{p}_{120}$  same as line defined by  $E_{21}\mathbf{p}_{210}$



# Reprojection Errors: Measure of Inconsistencies



(a)



(b)

- Reprojection error: Shortest distance from epipolar tangency to epipolar line of corresponding point
- Distances can be computed via  $E_{ij} \rightarrow$  cost function associated to pose

$$d_{ijk} = \frac{\mathbf{p}_{ijk}^T \mathbf{E}_{ij} \mathbf{p}_{jik}}{\sqrt{(\mathbf{E}_{ij} \mathbf{p}_{jik})_1^2 + (\mathbf{E}_{ij} \mathbf{p}_{jik})_2^2}}$$

- **Pose estimation:** Adjust pose parameters to minimize cost fct:

$$\text{cost} = \sum_{i=1}^m \sum_{j=1}^n \sum_{k=0}^1 d_{ijk}^2$$

Figure 4: Epipolar tangent lines with the projection of the epipolar tangent line of the opposite view and incorrect pose information: since the pose information is incorrect, the epipolar tangent lines do not project onto one another. The silhouettes are inconsistent with one another for the given viewpoints. The reprojection error is a measure of the degree of inconsistency.



# Results

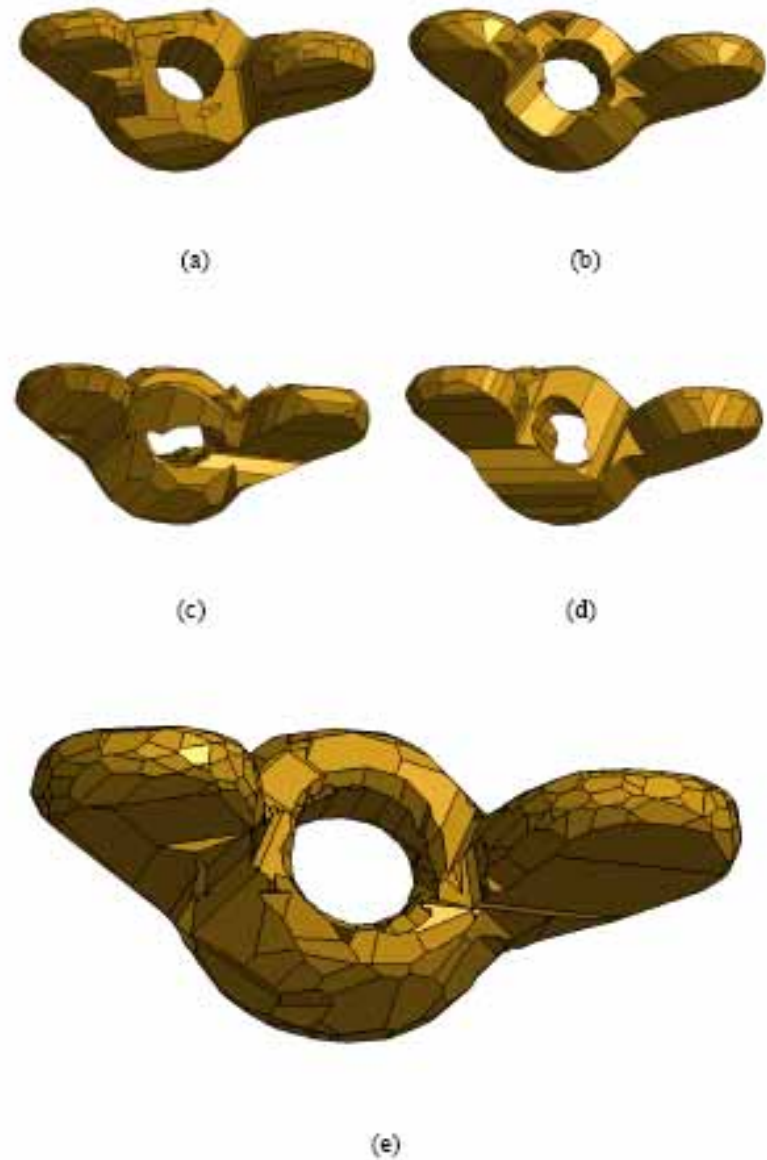


Figure 5: Visual hull models of a wing nut: (a)–(d) show four models each built from five silhouettes, (e) shows the model built from the 20 silhouettes used in (a)–(d) after the poses of all silhouettes have been determined in a common reference frame.



# Results

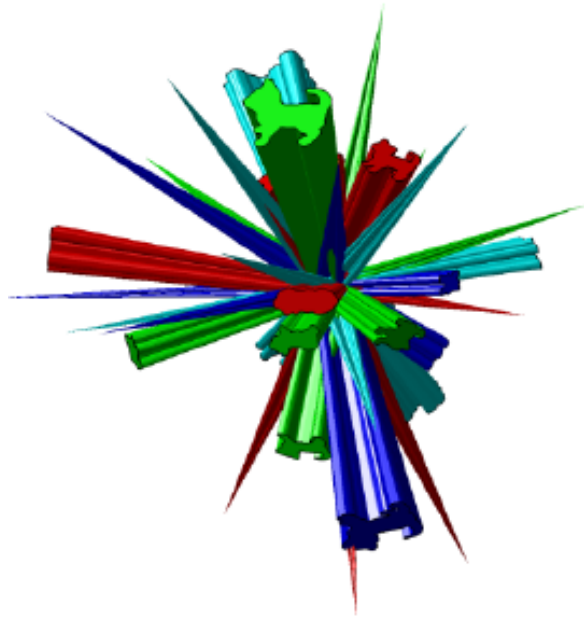


Figure 7: The twenty visual cones of the cat



(a)

(b)



(c)

(d)



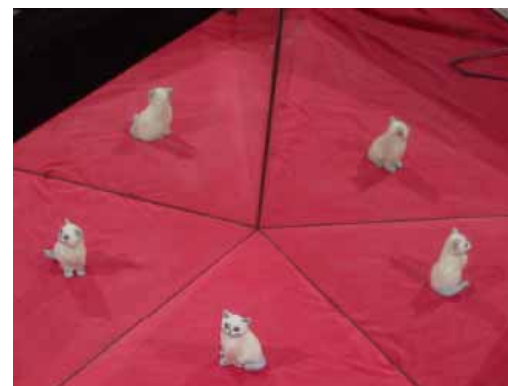
(e)

Figure 6: Visual hull models of a toy cat: (a)–(d) show four models each built from five silhouettes, (e) shows the model built from the 20 silhouettes used in (a)–(d) after the poses of all silhouettes have been determined in a common reference frame.



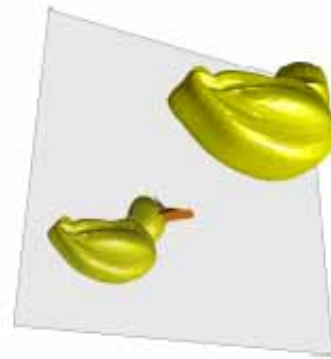
# Smart Low Cost Solution

- **Visual Hulls from Single Uncalibrated Snapshots Using Two Planar Mirrors**
- Keith Forbes,  
Anthon Voigt,  
Ndimi Bodika,  
PRASA2004 ([link](#))

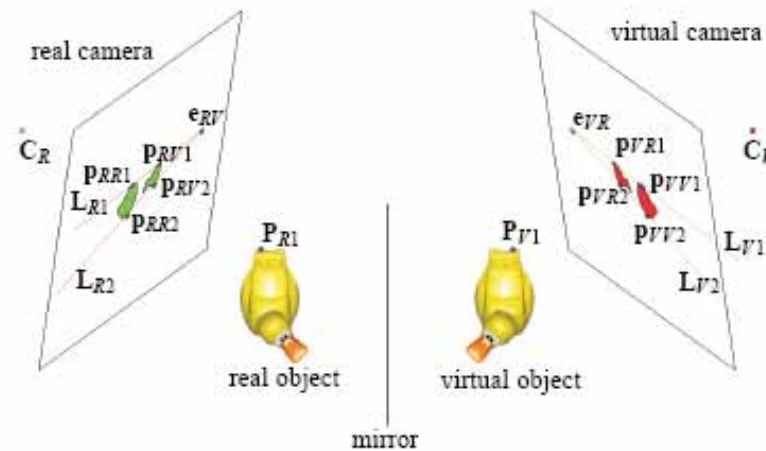




# Concept



(a)



(b)

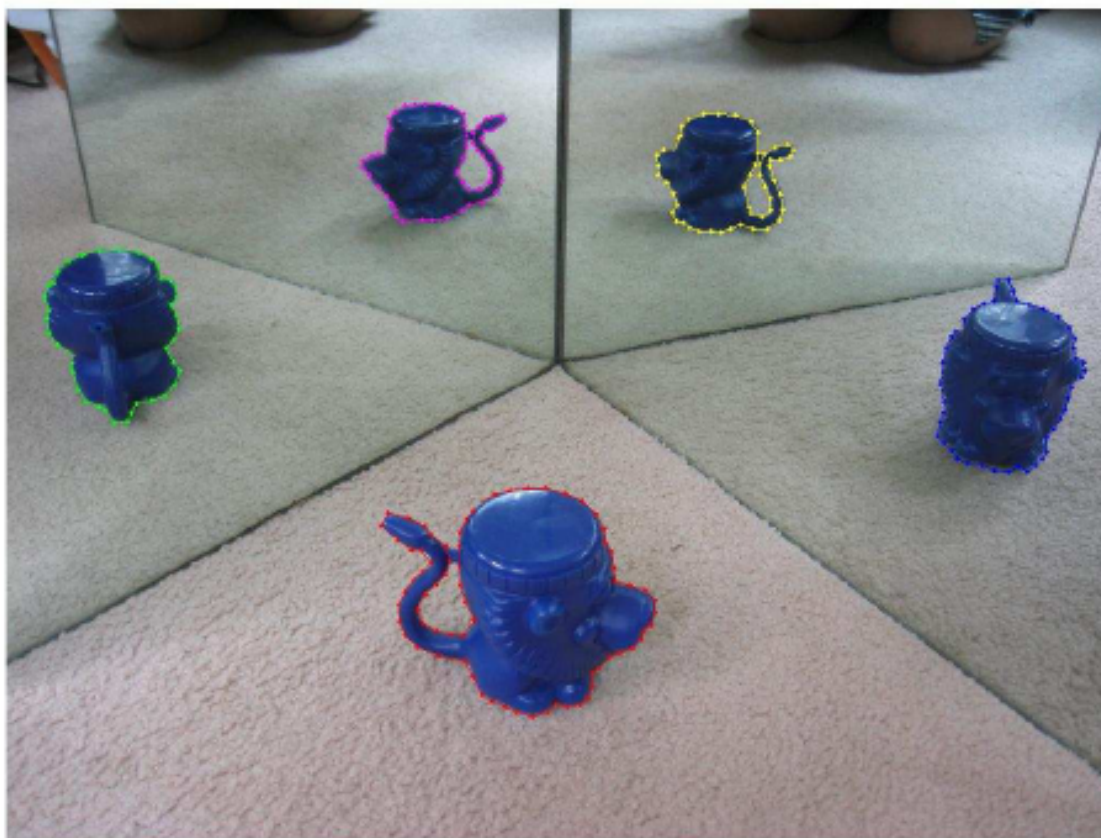
Figure 2: Reflection of a duck in a mirror: (a) shows the image seen by the real camera, (b) shows the silhouette views seen by the real camera and by the virtual camera that is the reflection of the real camera.

- Virtual camera does not really exist
- Determine images it would observe from the real camera's image
- Therefore: Two silhouettes captured by real camera are **two views of the real object**



# Visual Hulls from 2 Mirrors

Then I manually segmented the five silhouettes in Matlab using polygons. The coordinates of the five polygons are the inputs to the Matlab code used to calculate the visual hull.



Christine Xu, Class Project CV UNC Chapel Hill, 2005

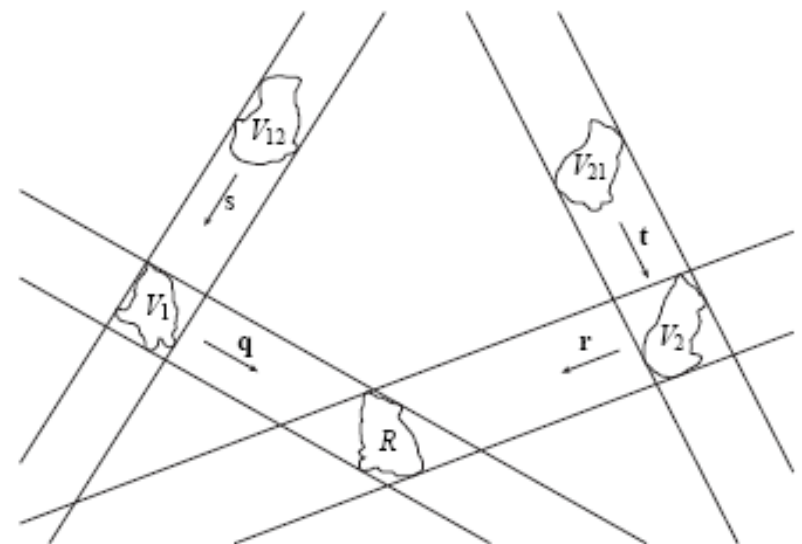


# Visual Hulls from 2 Mirrors

- Epipolar geometry of the object's five silhouettes is determined directly from the image without knowing the poses of the camera or the mirrors.
- Once the pose associated with each silhouette has been computed, a five-view visual hull of the object can be computed from the five silhouettes.
- After getting an initial estimation of all the camera poses, we can use the non-linear least square Levenberg-Marquardt method to iteratively minimize the reprojection error across every pair of silhouettes.



# Similar as before: Epipolar Tangency Lines



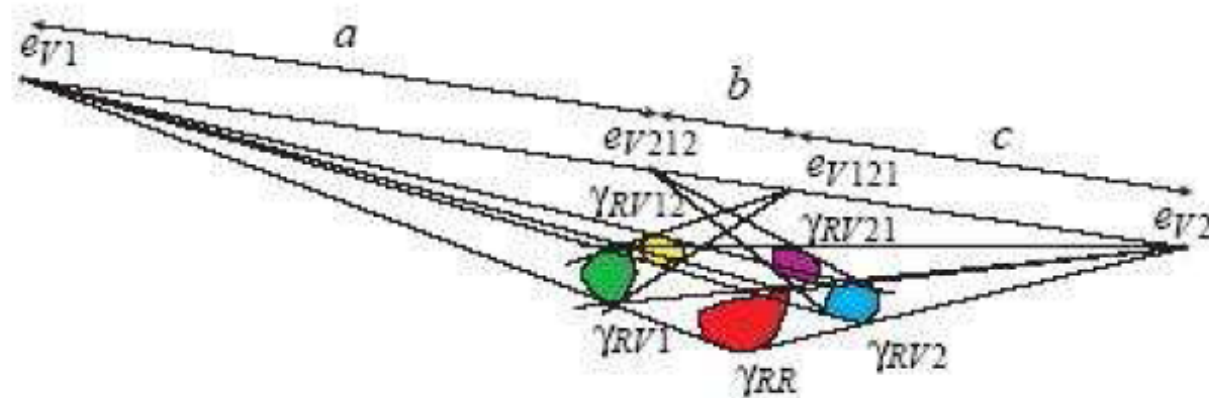
(c)

Figure 4: Images of a scene: (a) shows the raw image, (b) shows the segmented image with silhouette outlines and epipolar tangency lines, and (c) shows the derived orthographic image that would be seen by an orthographic camera.



# Visual Hulls from 2 Mirrors

The epipole corresponding to a camera's reflection can be computed from the camera's silhouette image of an object and its reflection by finding the intersection of the two outer bitangent lines.



In the above picture,  $ev_1$ ,  $ev_2$ ,  $ev_{121}$ , and  $ev_{212}$  are epipoles corresponding to camera  $Cv_1$ ,  $Cv_2$ ,  $Cv_{121}$ , and  $Cv_{212}$ , where  $Cv_1$  is the reflected camera by Mirror 1,  $Cv_{121}$  is reflected by Mirror 1 and then Mirror 2 and then again by Mirror 1, similar to  $Cv_2$  and  $Cv_{212}$ .



# Visual Hulls from 2 Mirrors (Forbes et al.)

Figure 4.5 shows how the epipoles  $eV1$ ,  $eV2$ ,  $eV121$ , and  $eV212$  are computed from the outlines of the five silhouettes observed by the real camera.

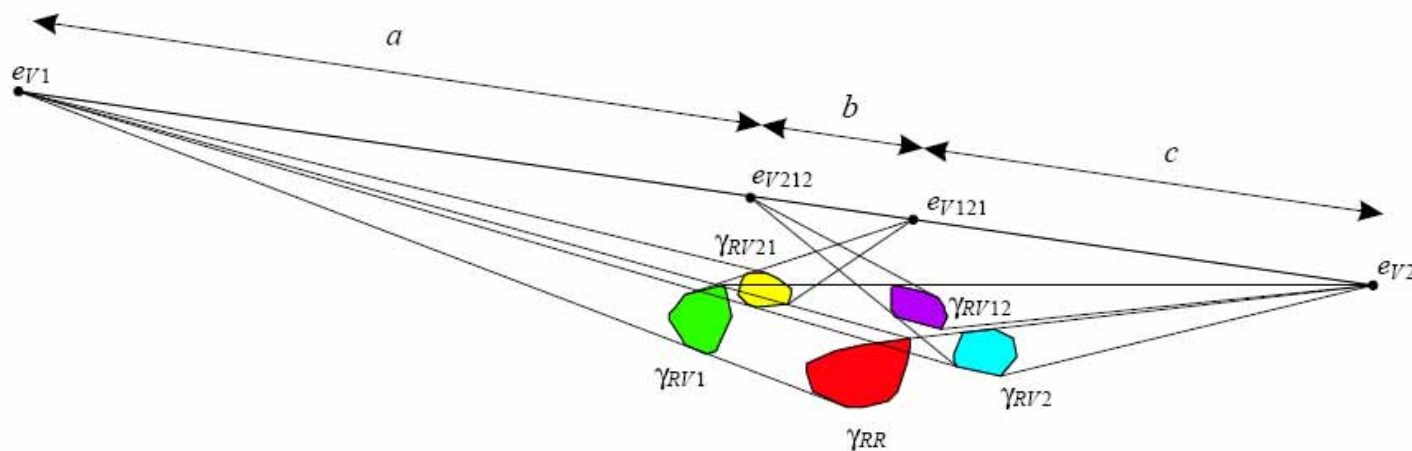
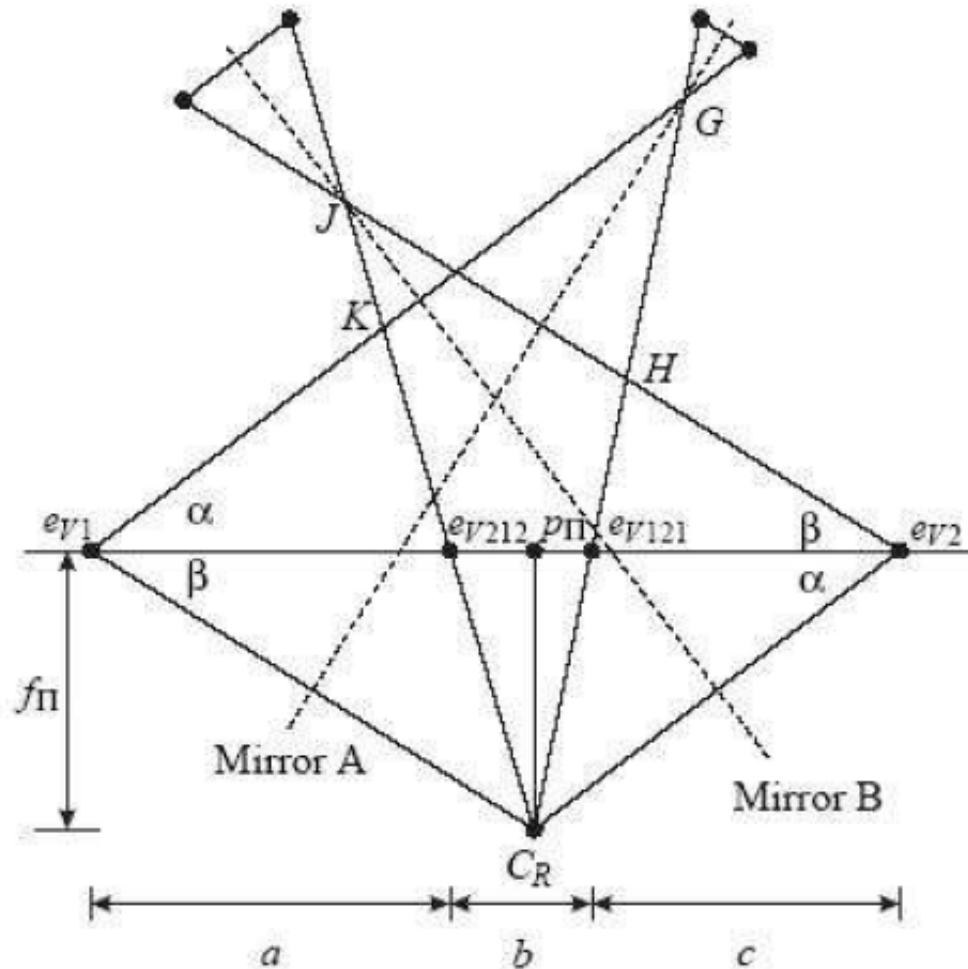


Figure 4.5: Computing epipoles  $eV1$ ,  $eV2$ ,  $eV121$ , and  $eV212$  from the silhouette outlines in an image.

Note that the epipoles  $eV1$ ,  $eV2$ ,  $eV121$ , and  $eV212$  are collinear, since they all lie in both the image plane of the real camera and in the plane  $PC$  in which all camera centres lie.



# Visual Hulls from 2 Mirrors

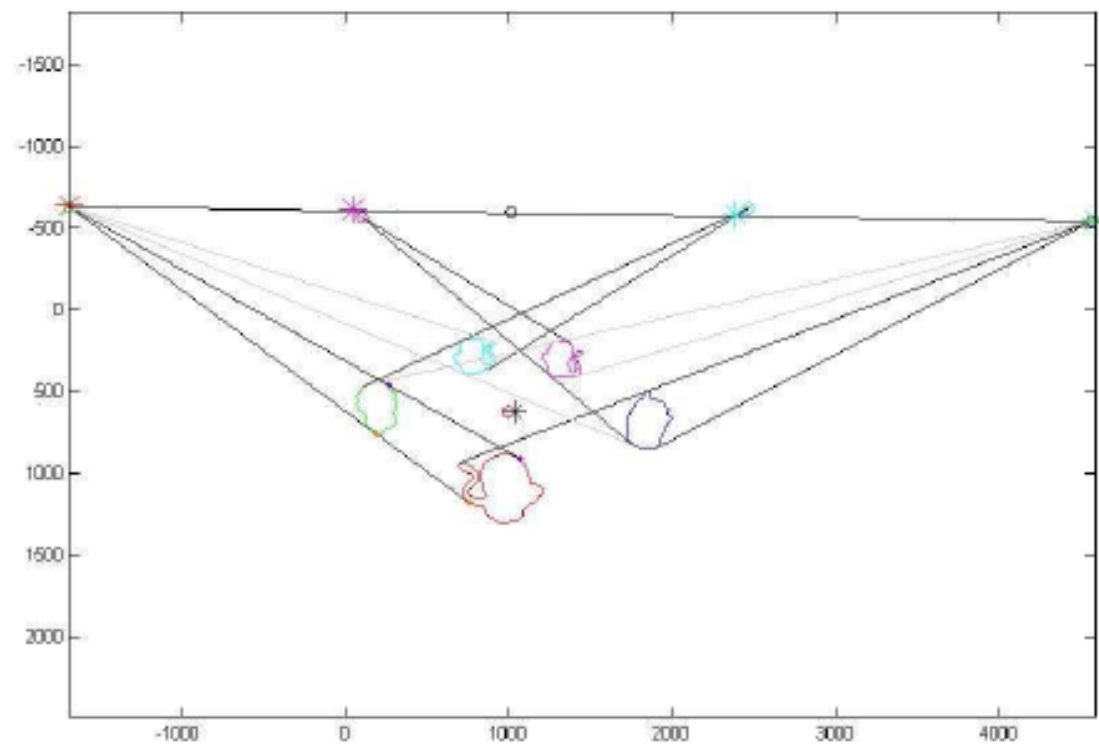


Once we know the focal length and the principal point  $p_0$ , we can compute the mirror normals.



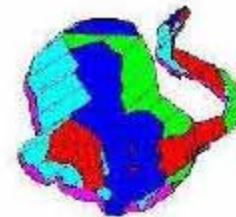
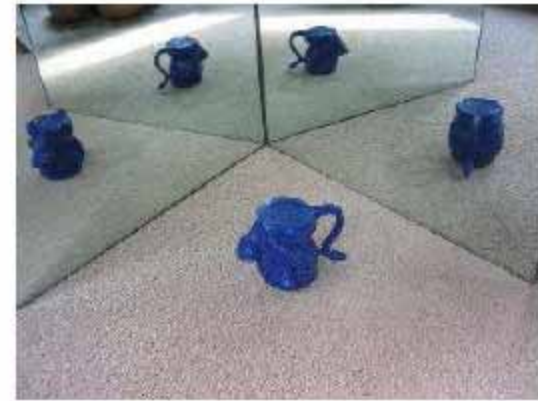
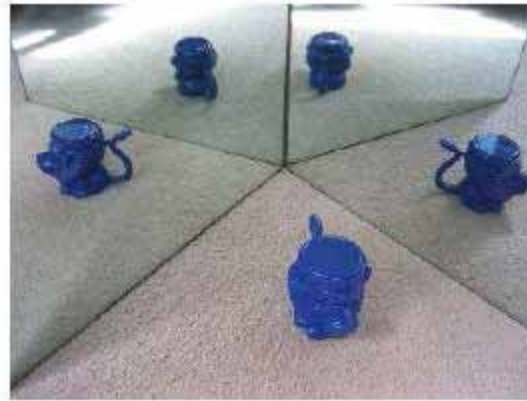
# Visual Hulls from 2 Mirrors

The four colinear epipoles determined directly using silhouette outlines are showed as follows.





# Visual Hulls from 2 Mirrors: Merge multiple 5 view hulls

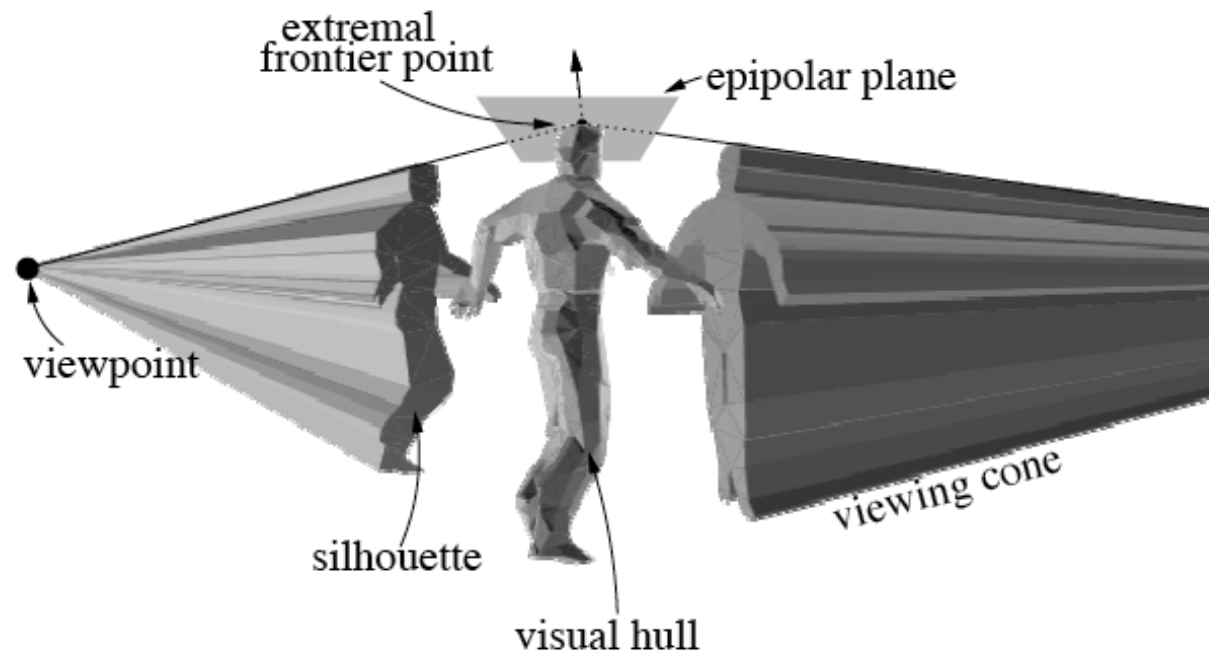


Christine Xu: Calculations in Matlab, all calculations <1Min



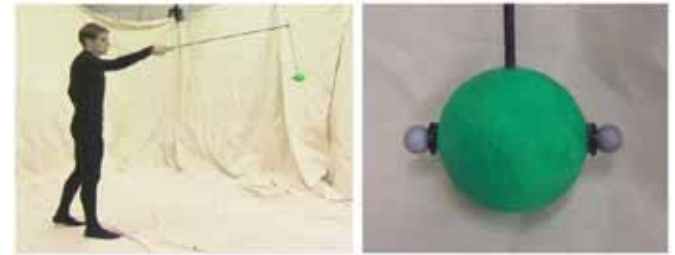
## What if my views aren't calibrated at all?

- Possible to calibrate from silhouettes
- Idea: optimize for a set of calibration parameters most consistent with silhouettes
- Boyer 05: define a dense distance between two cones
  - minimize the combined distances between viewing cones





# Camera network calibration using silhouettes



- 4 NTSC videos recorded by 4 computers for 4 minutes
- Manually synchronized and calibrated using MoCap system





Additional slides:  
Not used in Class

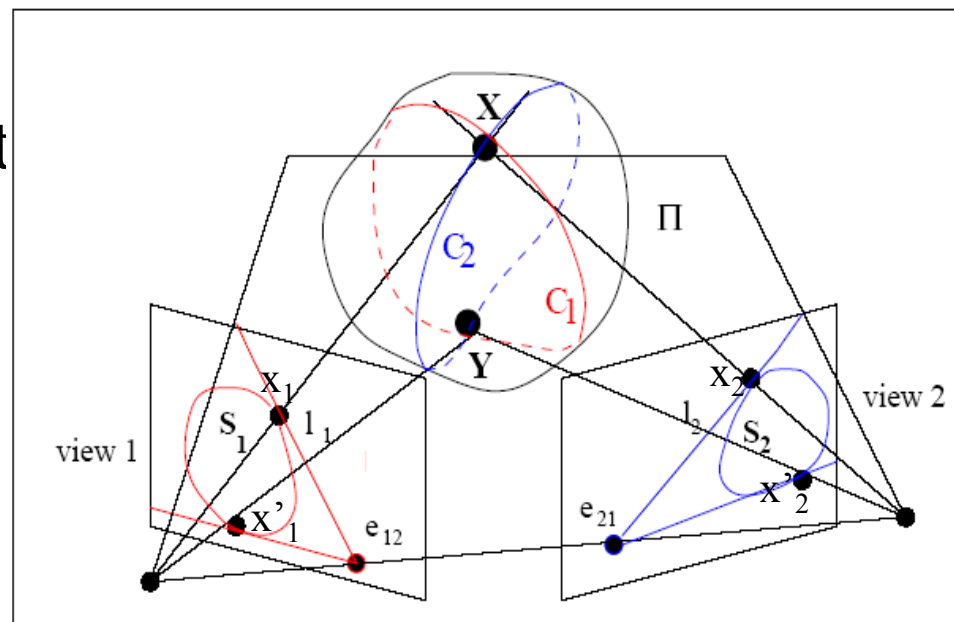


# Multiple View Geometry of Silhouettes

- Frontier Points
- Epipolar Tangent

$$\mathbf{x}_2^T \mathbf{F} \mathbf{x}_1 = 0$$

$$\mathbf{x}'_2{}^T \mathbf{F} \mathbf{x}'_1 = 0$$



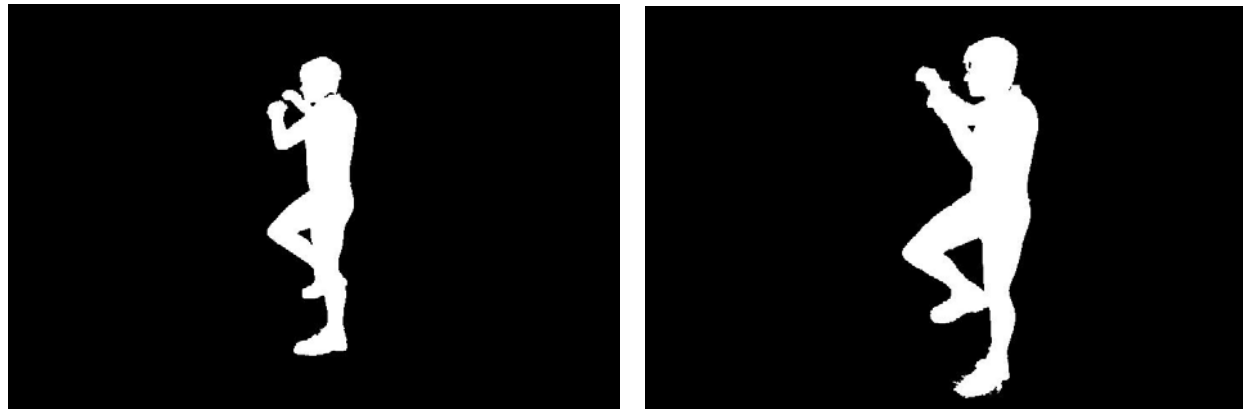
- Points on Silhouettes in 2 views do not correspond in general except for projected Frontier Points
- Always at least 2 extremal frontier points per silhouette
- In general, correspondence only over two views



## Camera Network Calibration from Silhouettes

(Sinha et al, CVPR'04)

- 7 or more corresponding frontier points needed to compute epipolar geometry for general motion
- Hard to find on single silhouette and possibly occluded

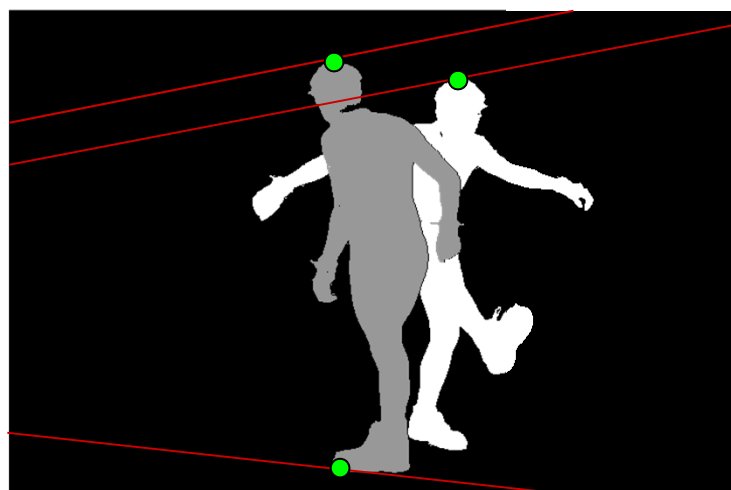
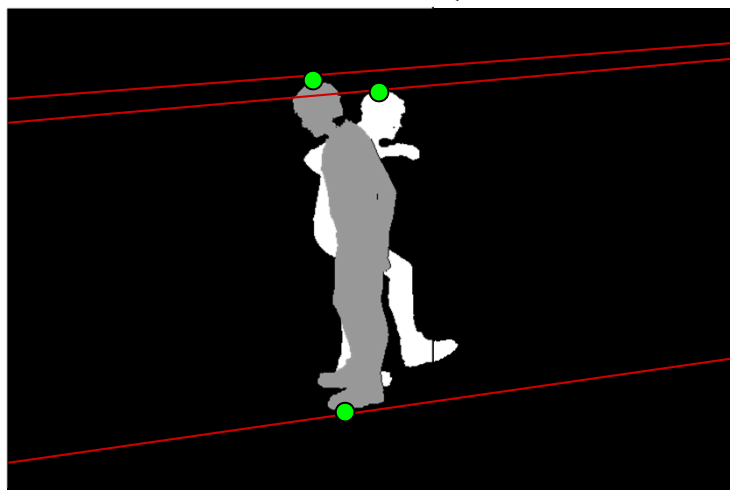


However, Visual Hull systems record many silhouettes!



## Camera Network Calibration from Silhouettes

- If we know the epipoles, it is simple
- Draw 3 outer epipolar tangents (from two silhouettes)



- Compute corresponding line homography  $H^{-T}$  (not unique)
- Epipolar Geometry  $F = [e]_x H$



# Let's just sample: RANSAC

- Repeat
  - Generate random hypothesis for epipoles
  - Compute epipolar geometry
  - Verify hypothesis and count inliers
- until satisfying hypothesis
- Refine hypothesis
  - minimize symmetric transfer error of frontier points
  - include more inliers

(use conservative threshold, e.g. 5 pixels, but abort early if not promising)

Until error and inliers stable

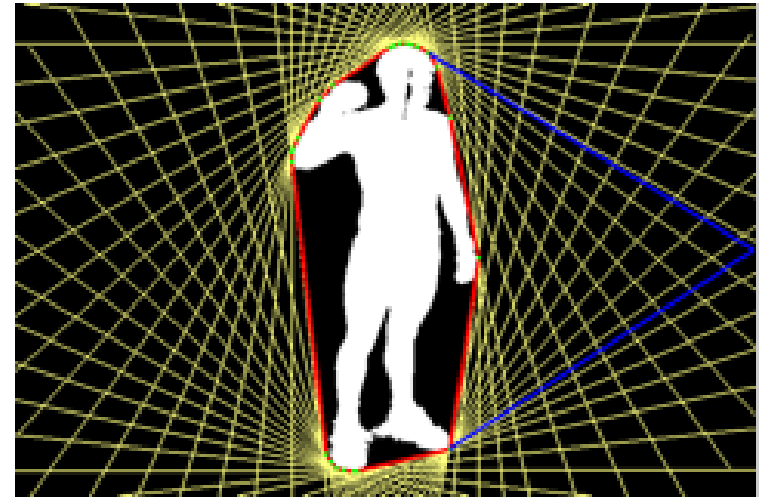
(use strict threshold, e.g. 1 pixels)

We'll need an efficient representation as we are likely to have to do many trials!



## A Compact Representation for Silhouettes Tangent Envelopes

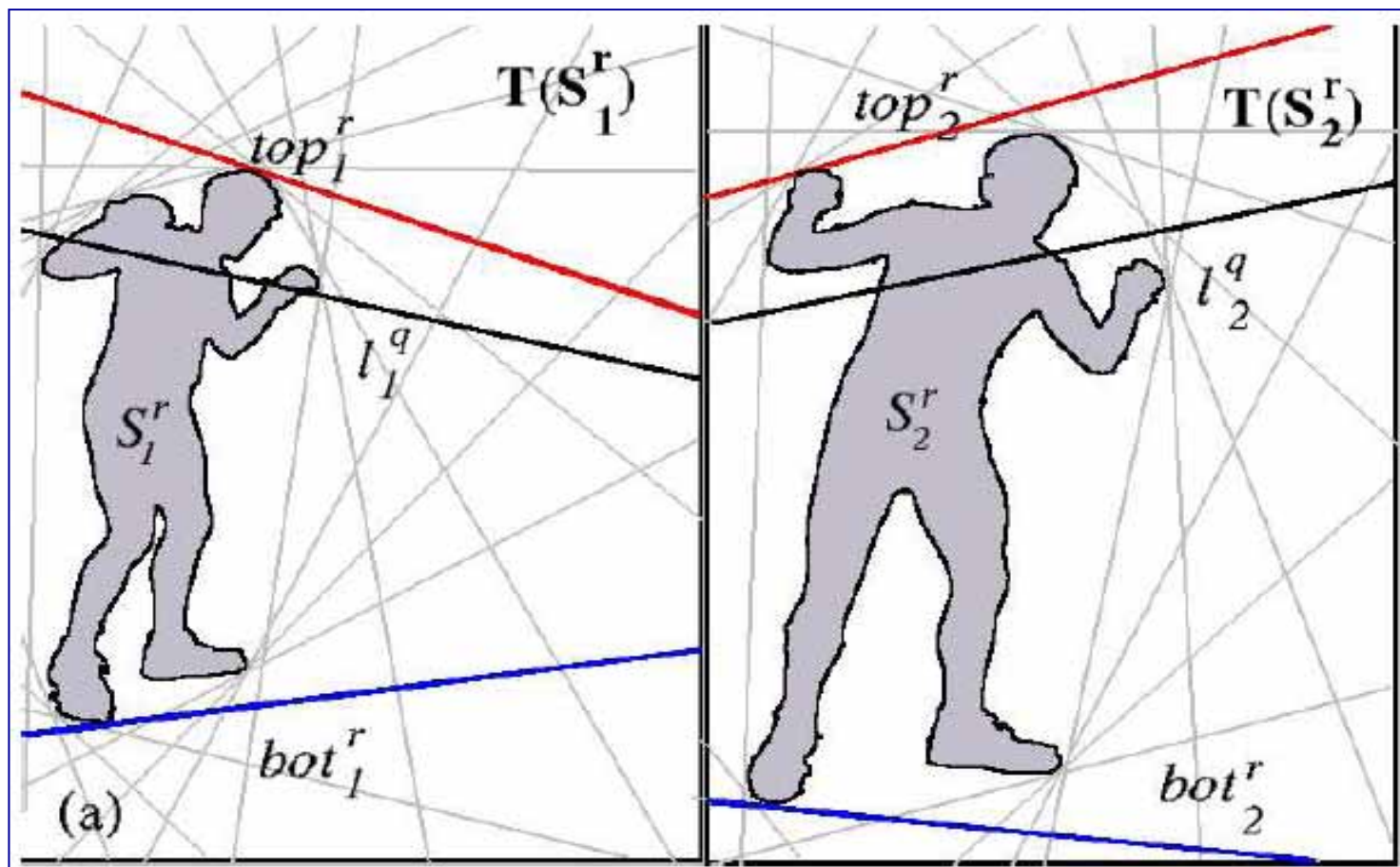
- Convex Hull of Silhouette.
- Tangency Points for a discrete set of angles.



- Approx. 500 bytes/frame. Hence a whole video sequences easily fits in memory.
- Tangency Computations are efficient.

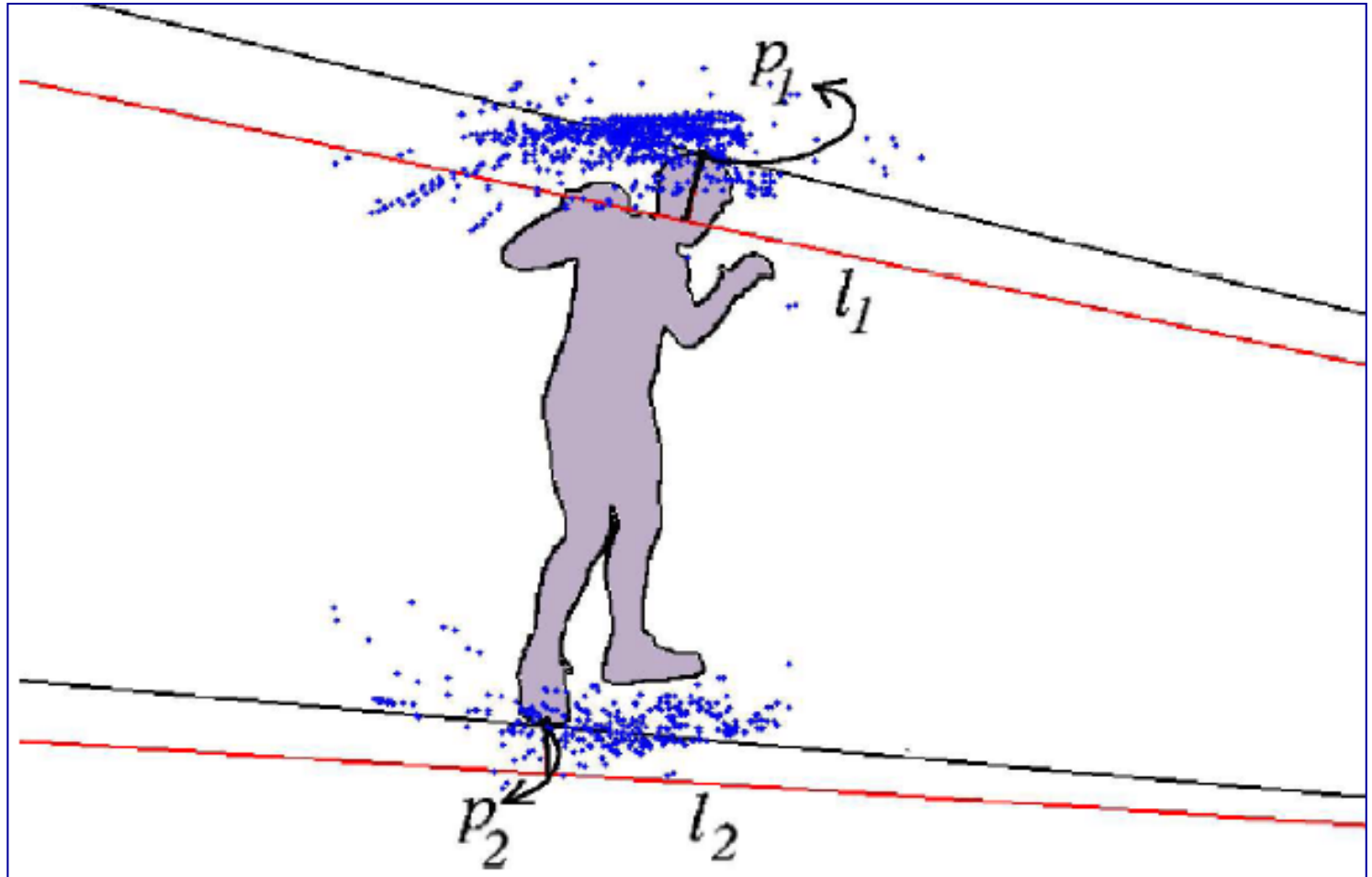


# Epipole Hypothesis and Computing H





# Model Verification







## Remarks

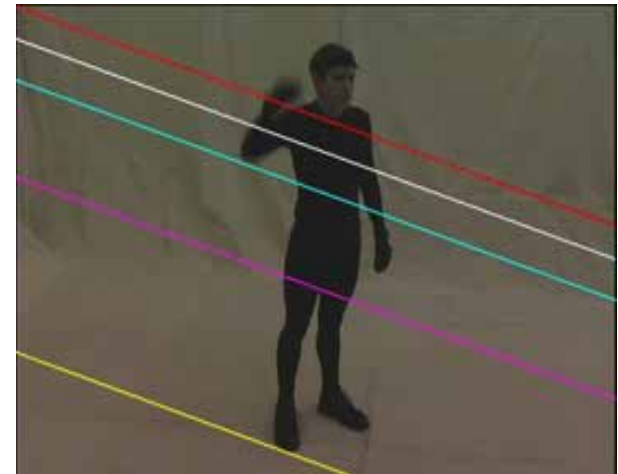
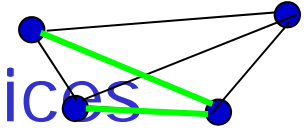
- RANSAC allows efficient exploration of 4D parameter space (i.e. epipole pair) while being robust to imperfect silhouettes



- Select key-frames to avoid having too many identical constraints (when silhouette is static)

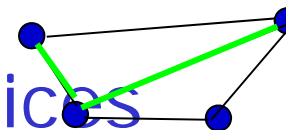


# Computed Fundamental Matrices

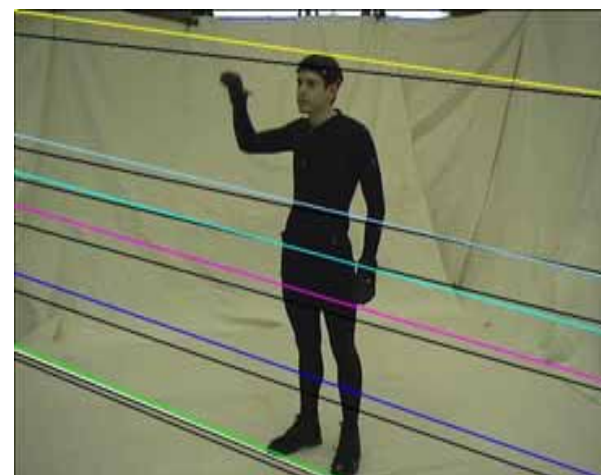
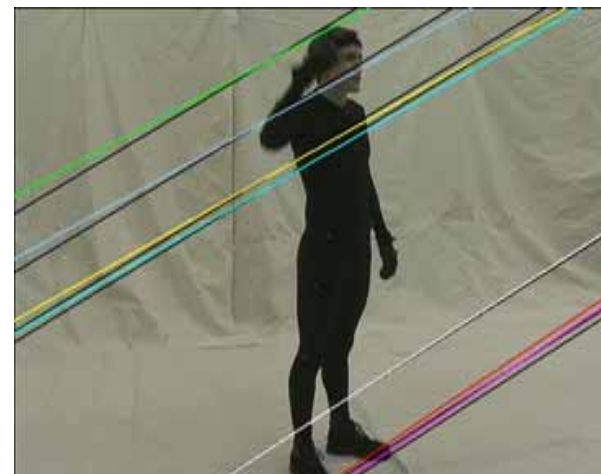




# Computed Fundamental Matrices

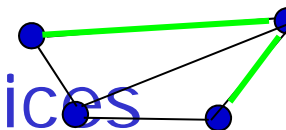


F computed directly (black epipolar lines)  
F after consistent 3D reconstruction (color)

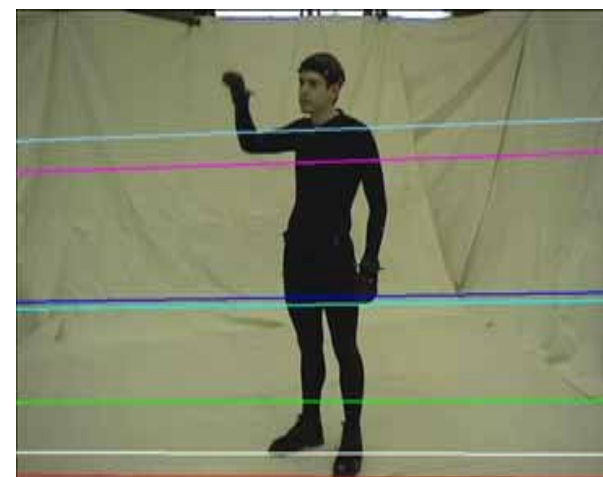
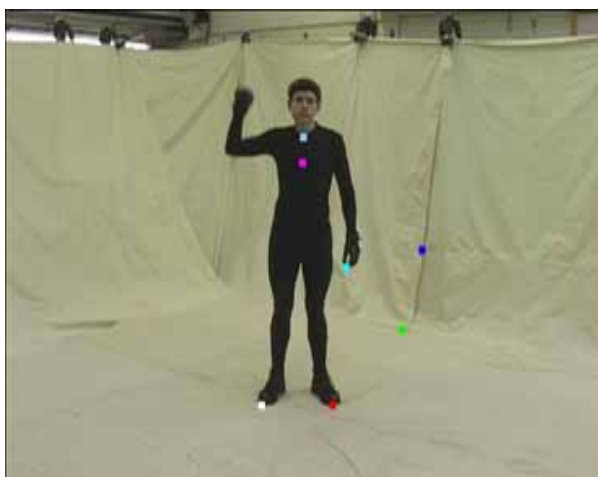
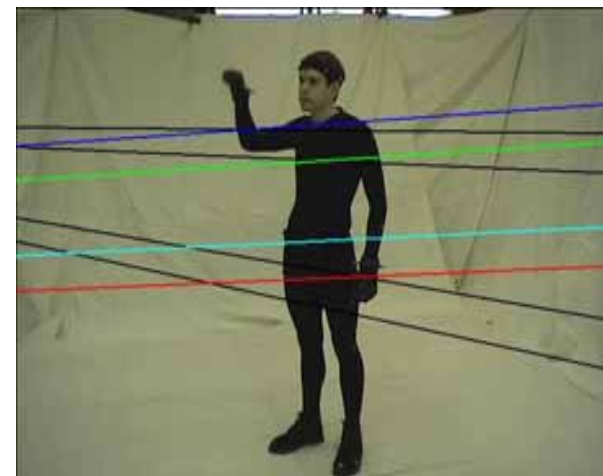




# Computed Fundamental Matrices



F computed directly (black epipolar lines)  
F after consistent 3D reconstruction (color)





## From epipolar geometry to full calibration

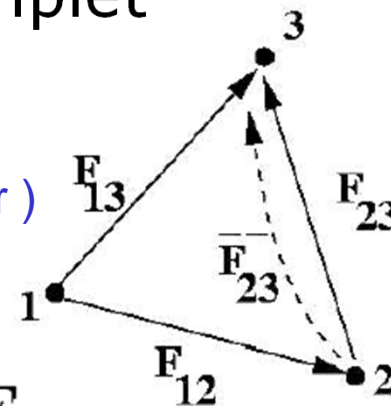
- Not trivial because only matches between two views
- Approach similar to Levi et al. CVPR'03, but practical
- Key step is to solve for camera triplet

$$P_1 = [I|0] \quad P_2 = [[e_{21}]_{\times} F_{12} | e_{21}]$$

$$P_3 = [[e_{31}]_{\times} F_{13} | 0] + e_{31} v^T \quad (v \text{ is 4-vector})$$

$$\bar{F}_{23} = [e_{32}]_{\times} P_3 P_2^+ \quad (\text{also linear in } v)$$

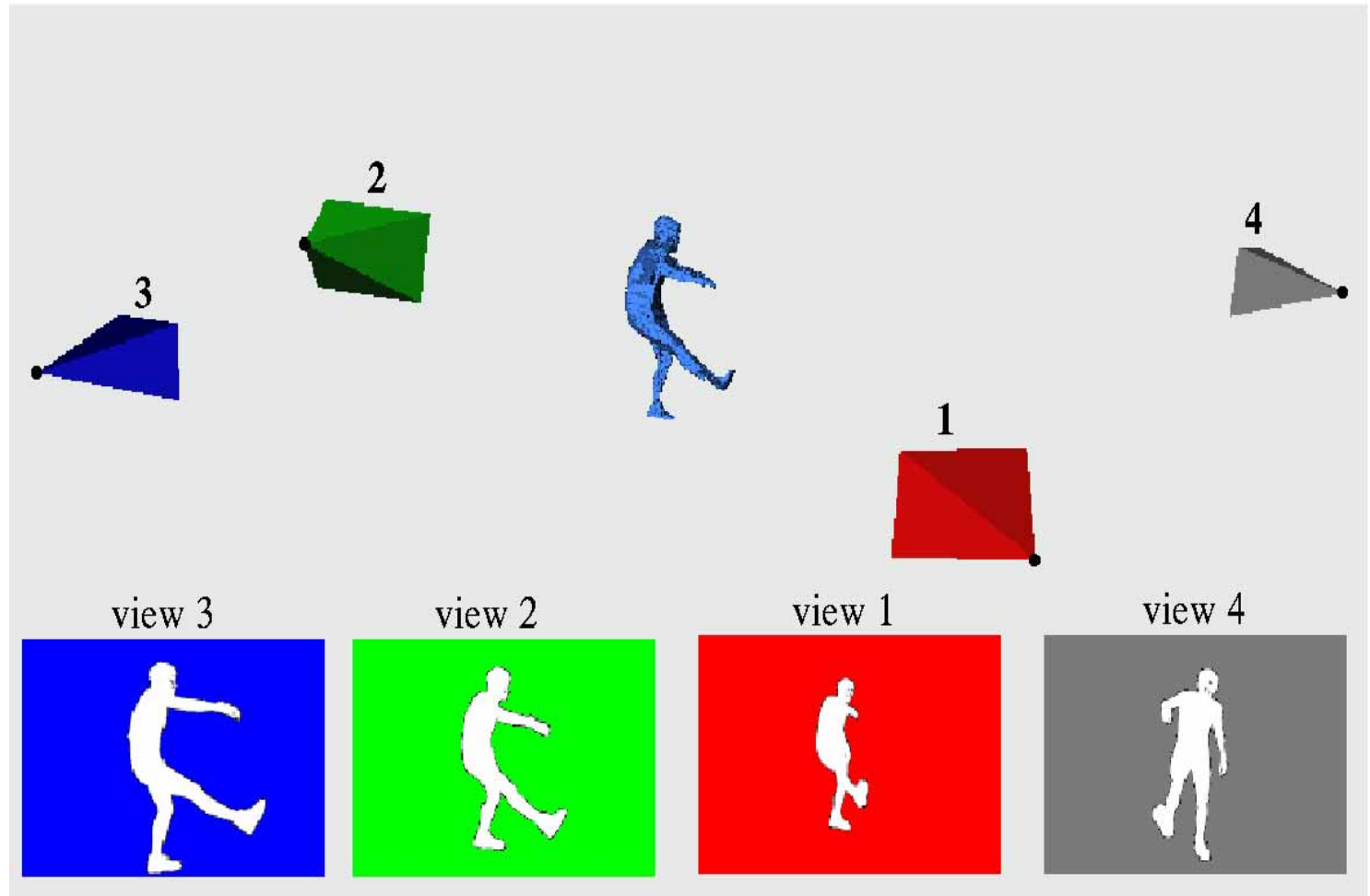
Choose  $P_3$  corresponding to  $\bar{F}_{23}$  closest  $F_{23}$



- Assemble complete camera network
- projective bundle, self-calibration, metric bundle



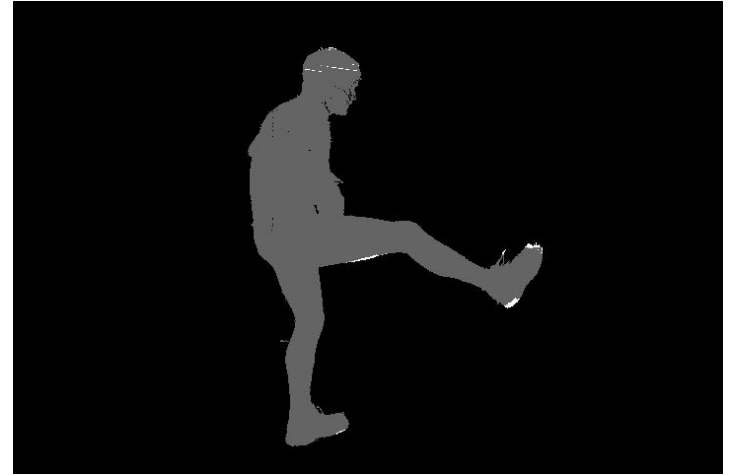
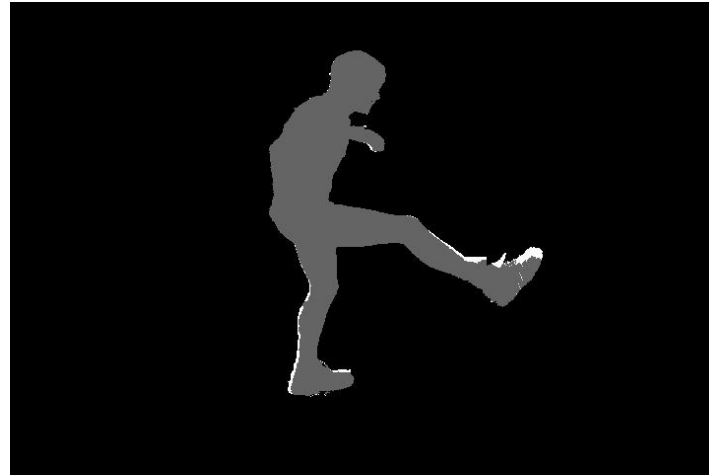
# Metric Cameras and Visual-Hull Reconstruction from 4 views



Final calibration quality comparable to explicit calibration procedure



# Validation experiment: Reprojection of silhouettes



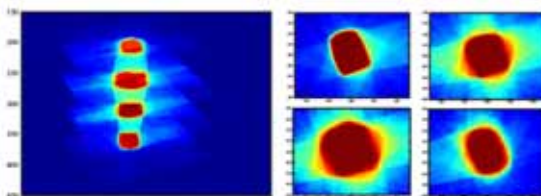


# Visual Hull Construction without Calibration

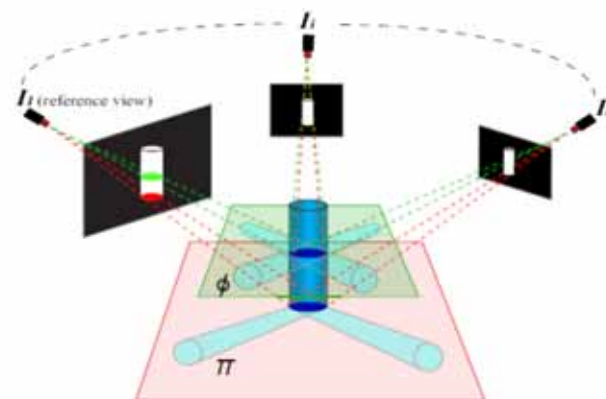
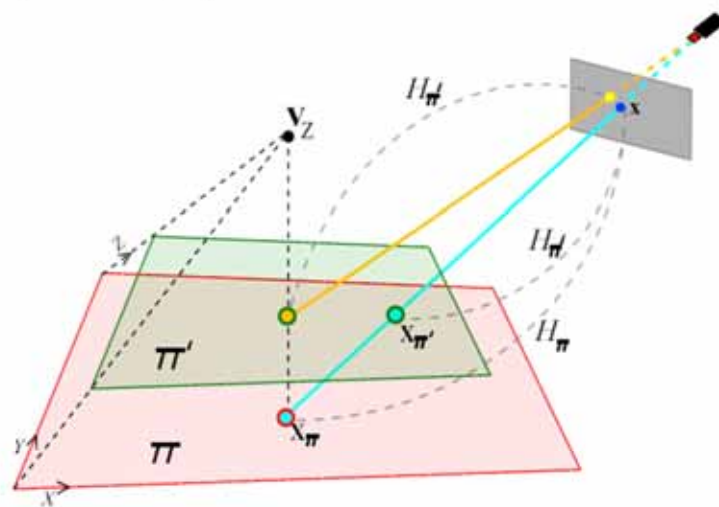
- Compute homography from image views to the horizontal slice [Khan et.al., A homographic framework for the fusion of multi-view silhouettes, ICCV, 2007]



(a)



(b)

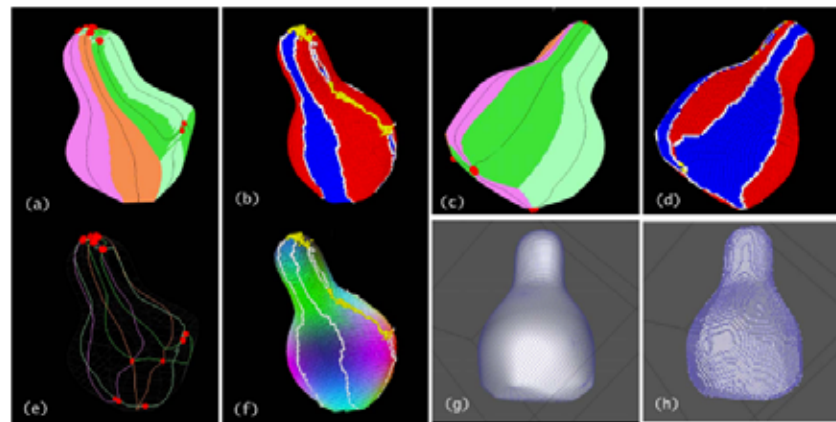






# Interesting ideas

- Use silhouettes + colors consistency



Sudipta's ICCV05 method

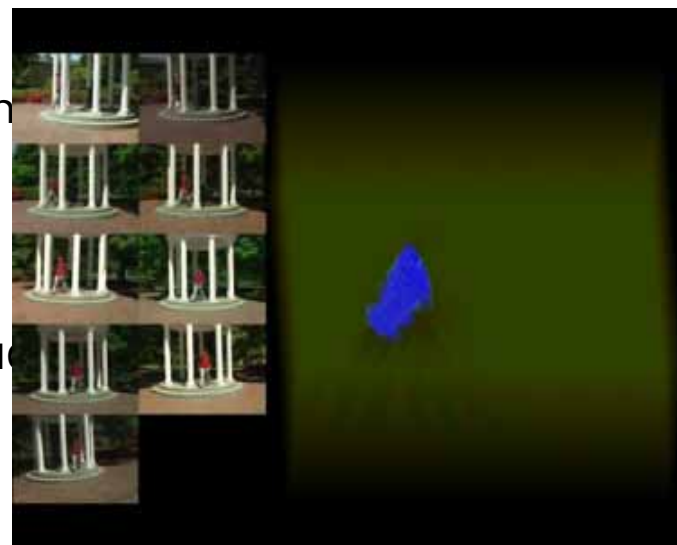


Ponce ECCV06



# Occluder Inference in Natural Environment

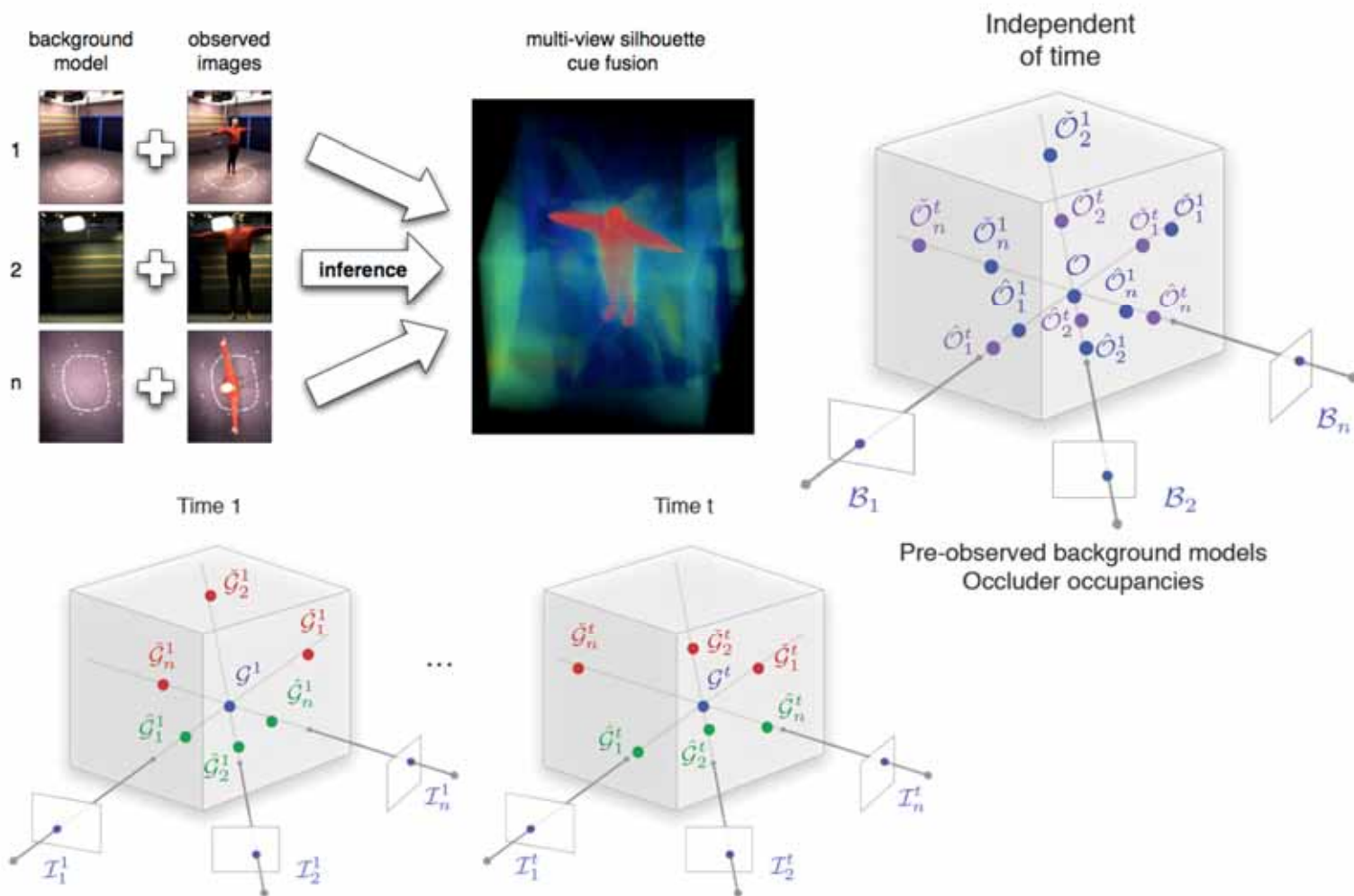
- Goal: 3D dynamic object (e.g. human) modeling in uncontrolled outdoor environment, with geometrically calibrated cameras
- Setup Difficulties
  - lighting variation
  - color inconsistency
  - little usable texture information
- SfS, 3D volume representation
- Model explicitly the static occluder
- Bayesian inference two steps:
  - Dynamic object
  - Static occluder
- Incremental scheme



[Guan et.al., CVPR 2007]



# Occluder Inference in Natural Environment (cont.)





# Perspectives

- Still many things to do:
  - accumulate information over time
  - combine different sources of information: silhouettes, color consistency, other cues.
  - new models to represent the scene
  - fully automatic system for multi-view reconstruction and data representation
    - Calibration
    - Static environment modeling
    - Dynamic objects analysis



# Perspectives

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  - accumulate information over time
  - combine different sources of information: silhouettes, color consistency, other cues.
  - new models to represent the scene
  - fully automatic system for multi-view reconstruction and data representation
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    - Static environment modeling
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## Why use a Visual Hull?

- Can be computed efficiently
- No photo-consistency required
- As bootstrap of many fancy refinement ...

## Why not a Visual Hull?

- No exact representation in concavity
- Sensitive to silhouette observation
- Closed surface representation
- Silhouette loses some information ...

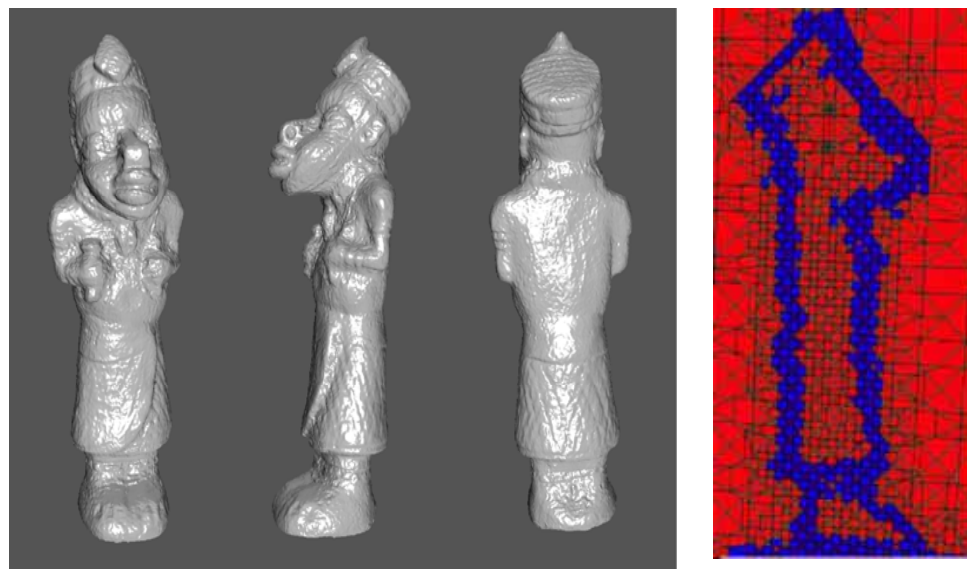


# Literature

- Theory
  - Laurentini '94, Petitjean '98, Laurentini '99
- Solid cone intersection:
  - Baumgart '74 (polyhedra), Szeliski '93 (octrees)
- Image-based visual hulls
  - Matusik et al. '00, Matusik et al. '01
- Advanced modeling
  - Sullivan & Ponce '98, Cross & Zisserman '00, Matusik et al. '02
- Applications
  - Leibe et al. '00, Lok '01, Shlyakhter et al. '01, ...



## Extension: Multi-view Stereo with exact silhouette constraints

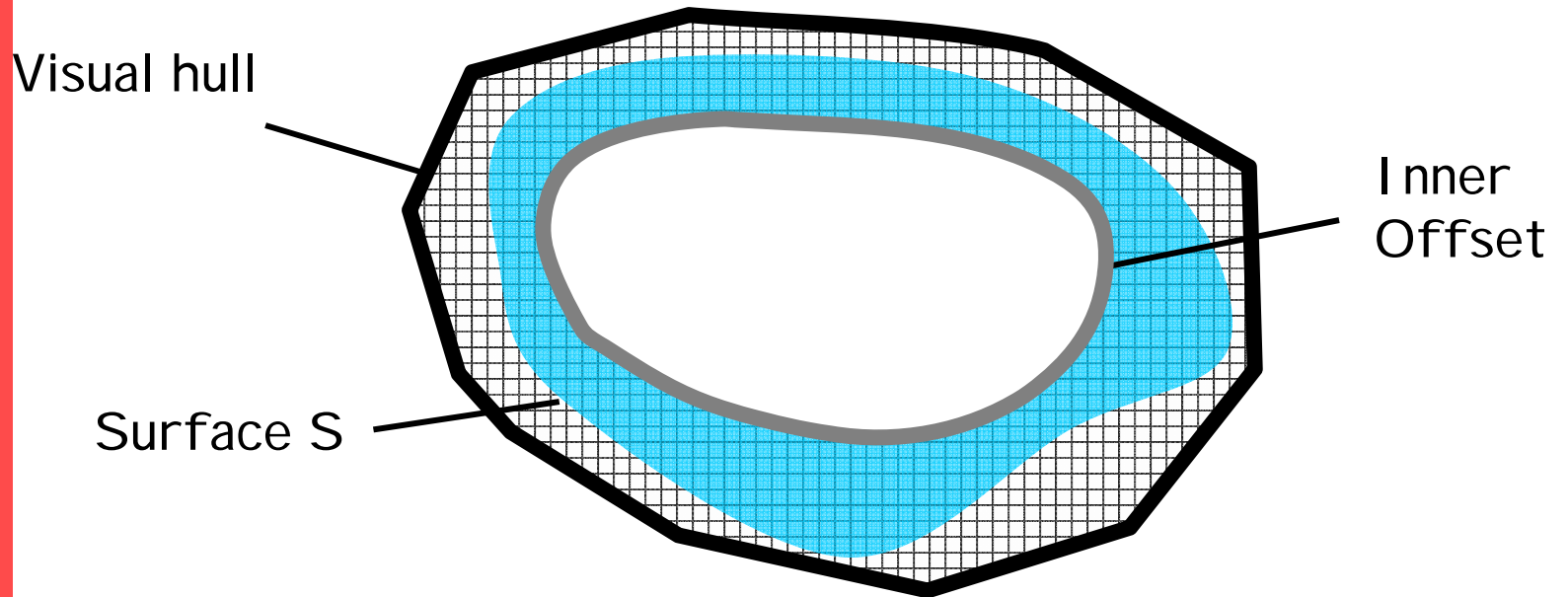


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**Silhouettes for Calibration and  
Reconstruction from Multiple Views**





# Volumetric Formulation

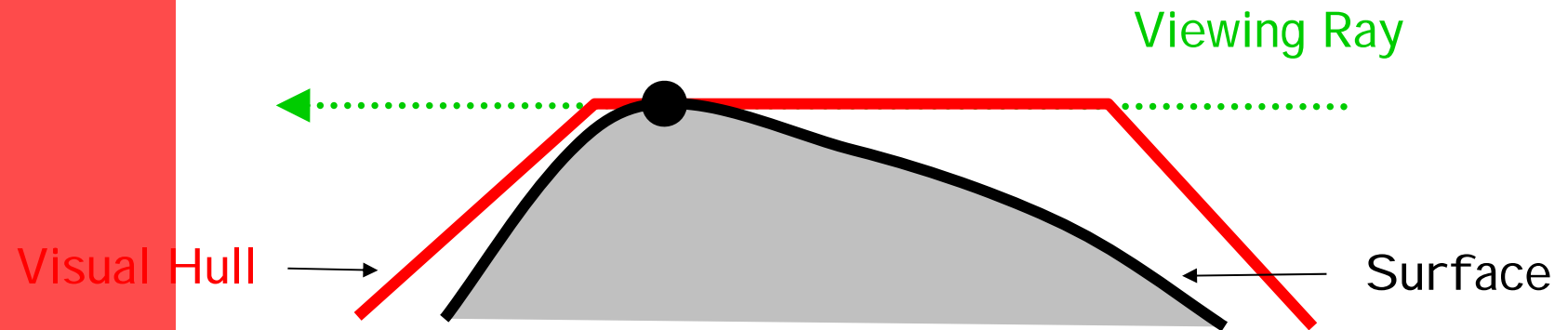


Find  $S$  which minimizes  $\int_S \phi(s) ds$

$\phi(s)$  is a measure of the photo-inconsistency of a surface element at  $s$

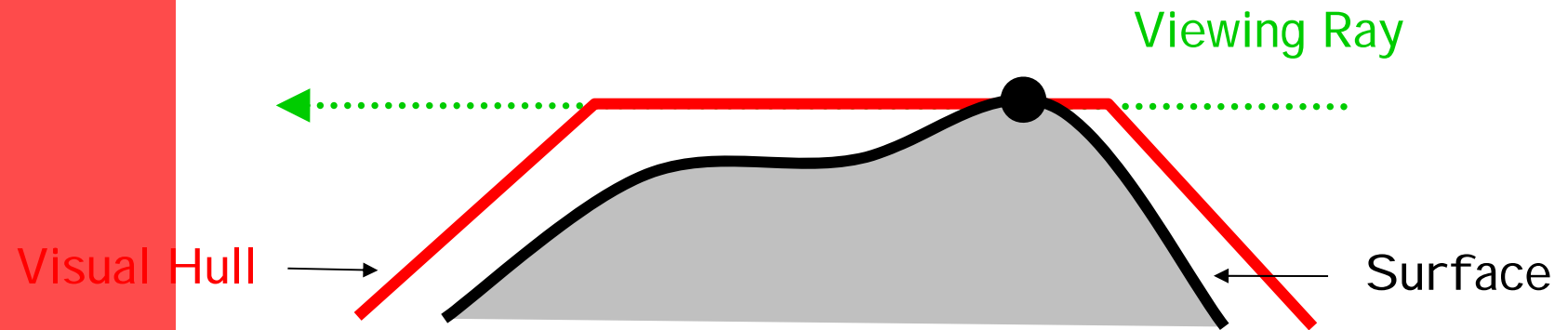


# Silhouette Consistent Shapes





# Silhouette Consistent Shapes





# Photoconsistency

- **Photo-consistency** is a function that how measures the likelihood of a 3D point of being on a opaque surface in the scene. This likelihood is computed based on the images in which this 3D point is potentially visible.
- An ideal Lambertian surface point will appear to have the **same color in all the images**.
- Photo-consistency can be measured in image space or object space.
  - Image space computations compare image patches centered at the pixels where the 3D point projects.
  - Object space computations are more general – a patch centered at the 3D point is projected into the images and the appearance of the projected patches are compared.



# Photoconsistency

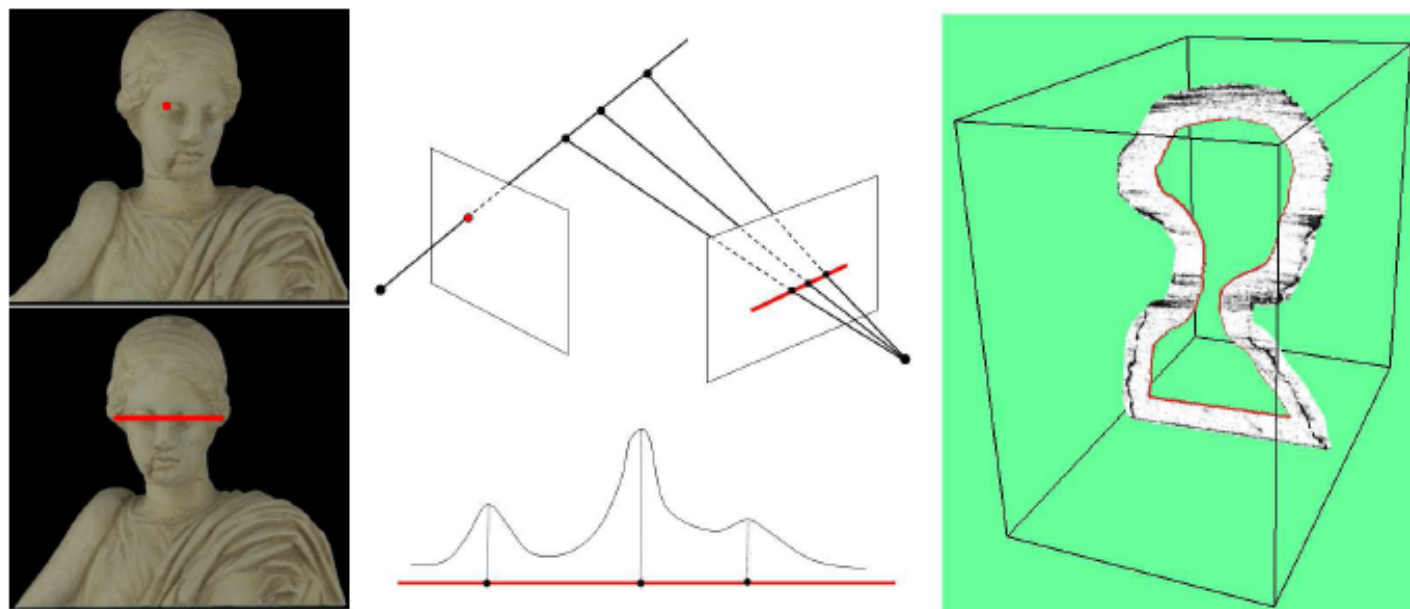


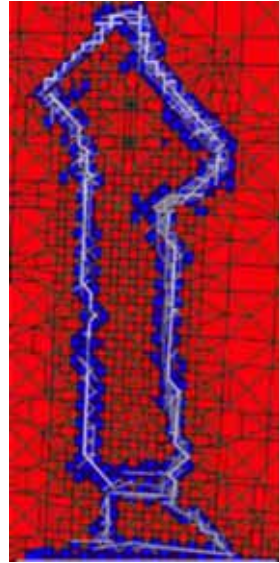
Figure 6.19: Computing multiple hypotheses for 2-view matches. These 2-view matches are triangulated and the generated 3D points are used to accumulate votes within a 3D volume. The photo-consistency measure is derived from these votes. A slice through the photo-consistency volume (interior of visual hull) is shown. Here black indicates regions of high photo-consistency.

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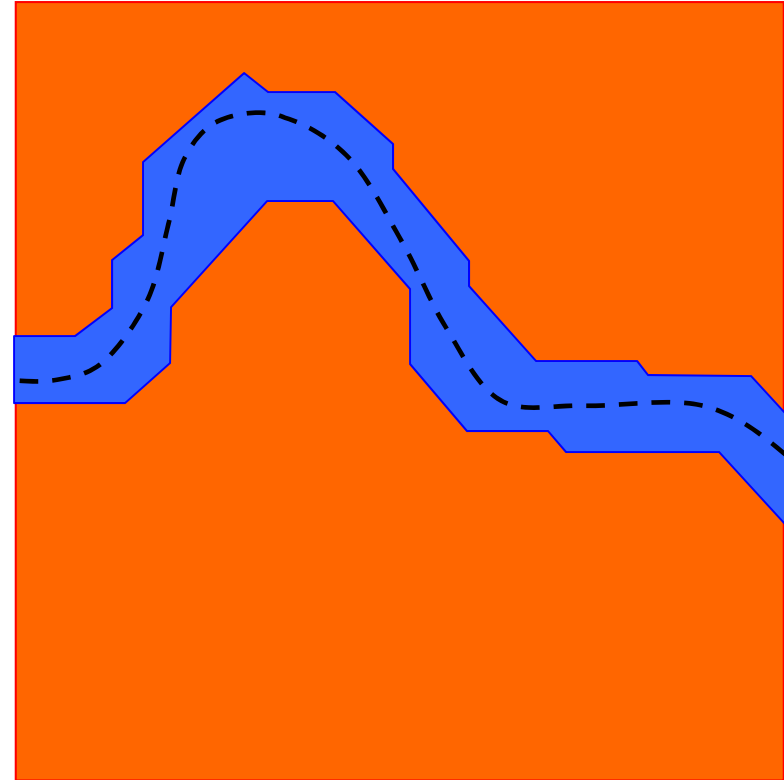
# Mesh with Photo-consistency



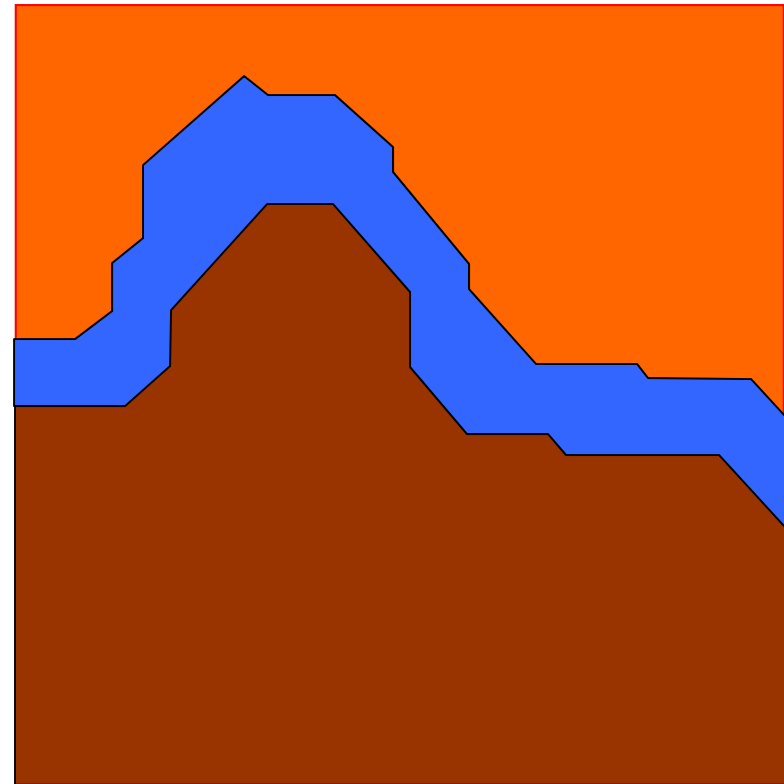
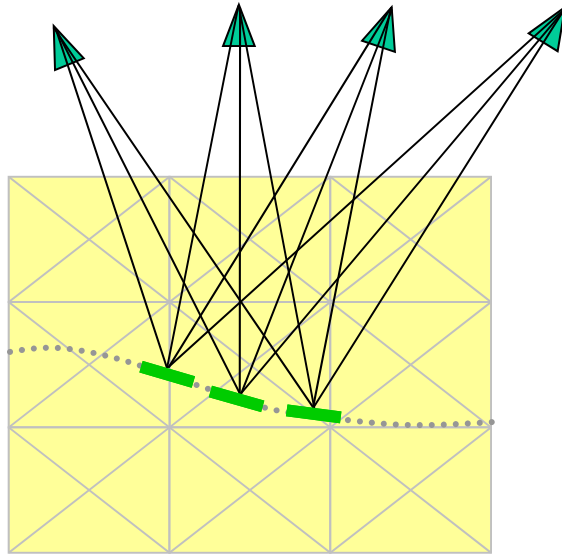
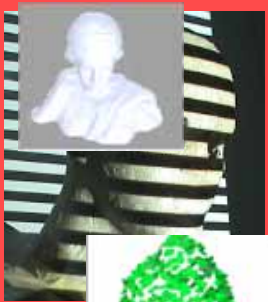
Final Mesh



shown with  
Photo-consistency



# Detect Interior



Use Visibility of the  
Photo-consistent Patches

Also proposed by  
Hernandez et. al. 2007, Labatut et.

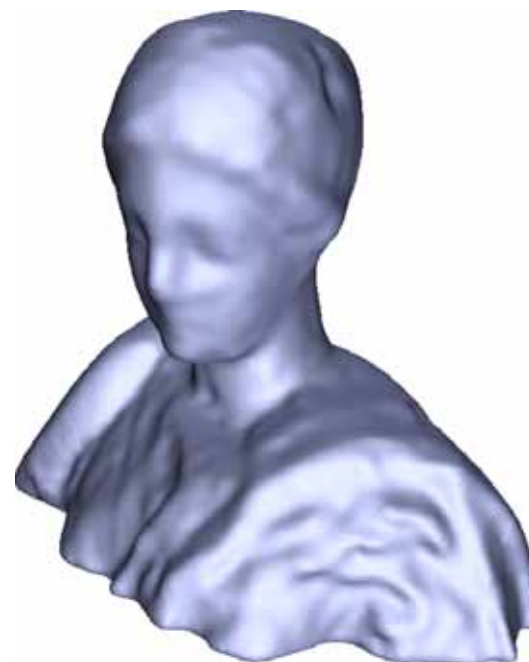
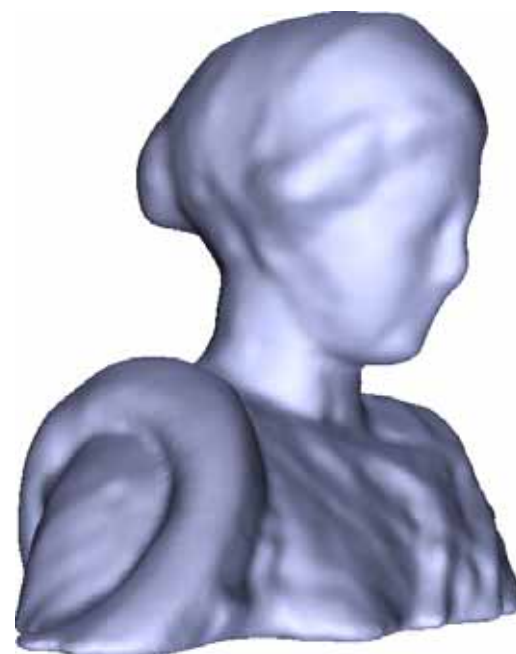
# Results



**36  
images**



**36  
images**





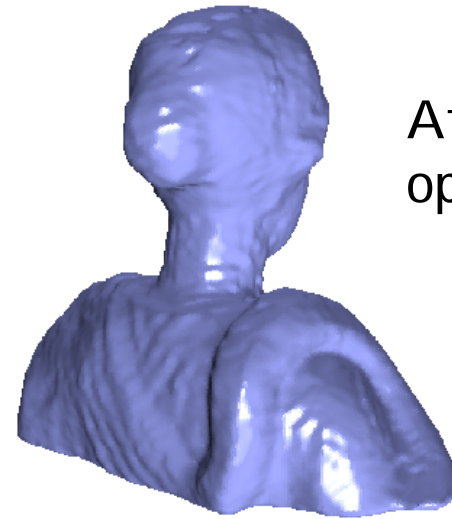
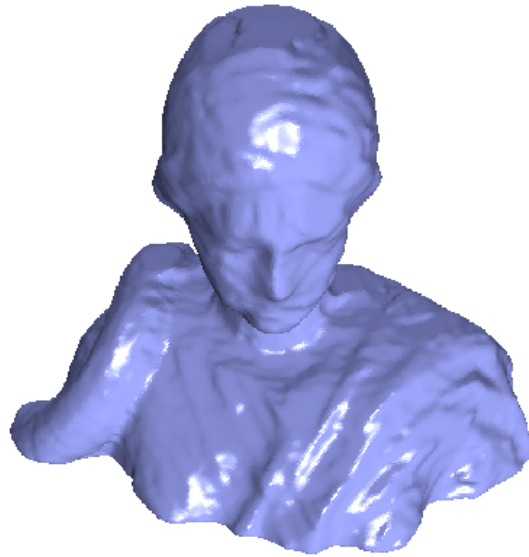
# Results



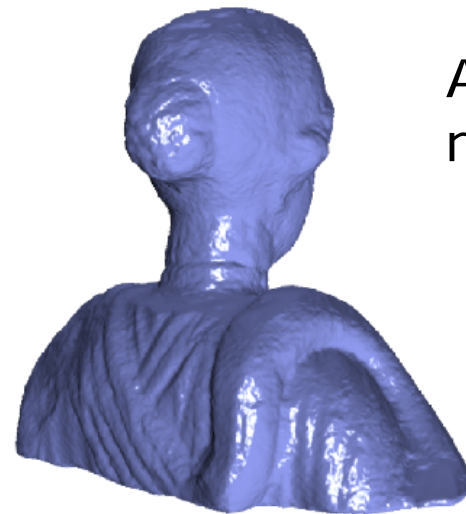
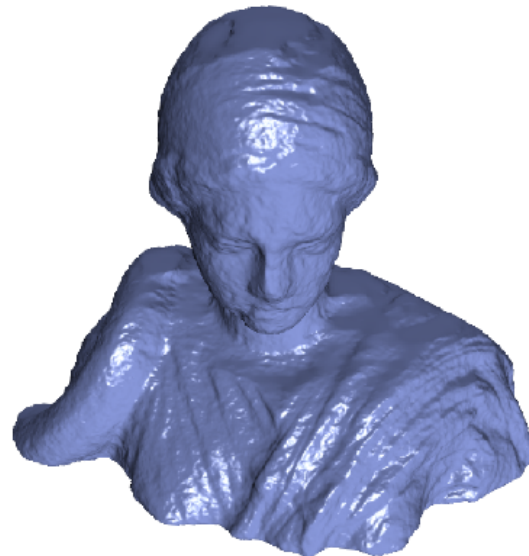
36

images

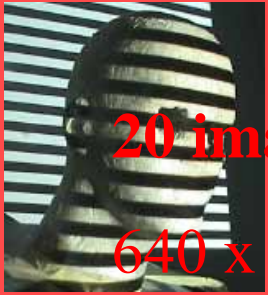
2000 x 3000



After graph-cut optimization



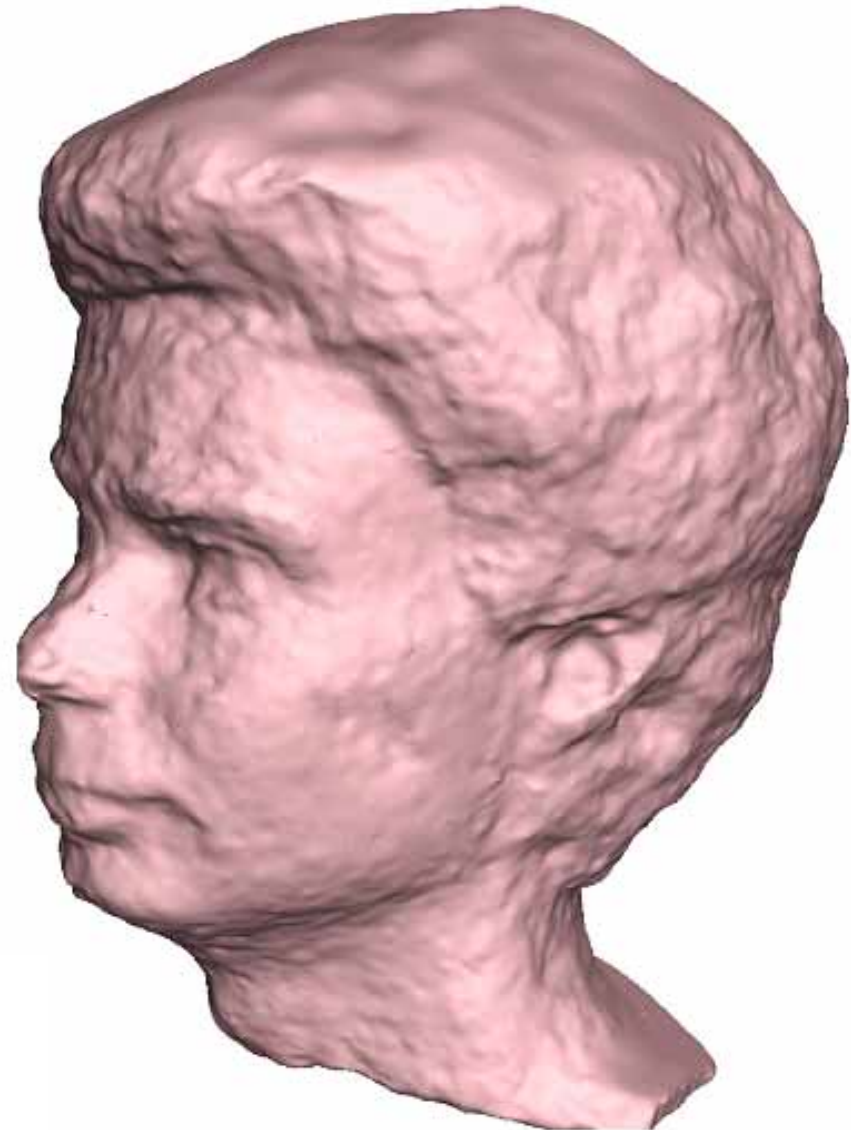
After local refinement



20 images

640 x 480

pixels

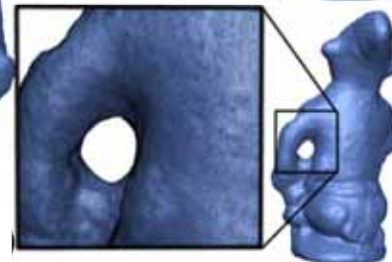
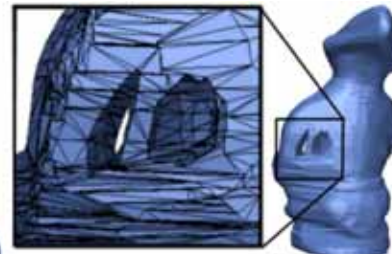


## Running Time:

Graph Construction :  
25 mins

Graph-cut :  
5 mins

Local Refiner  
20 mins



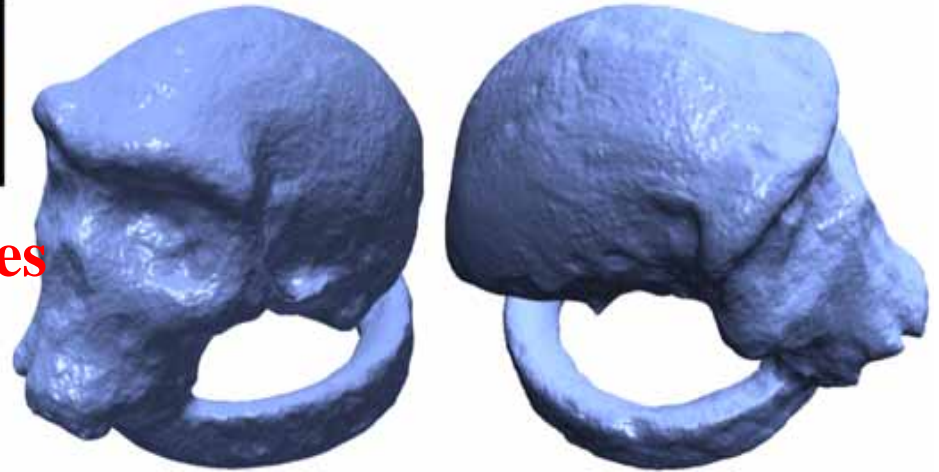
36  
images



36  
images



24 images

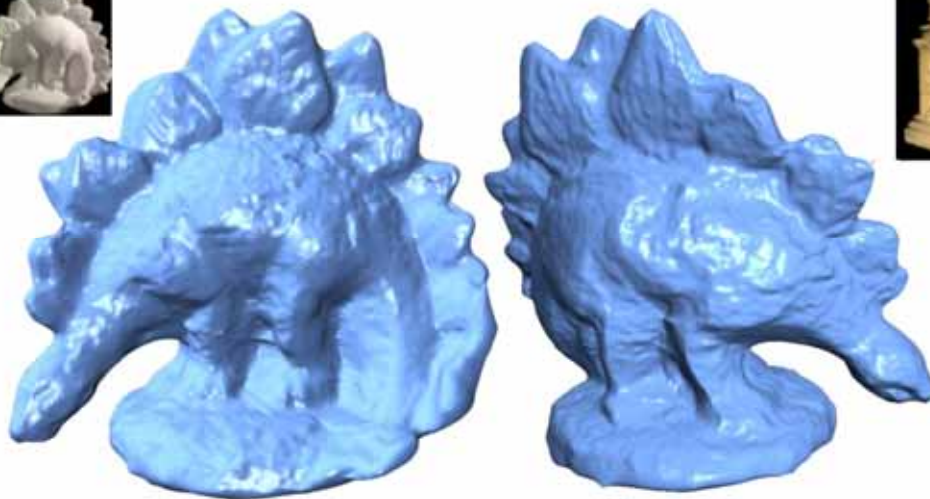


## Middlebury Evaluation

90% statistics	Accuracy	Completeness		Time
Dino-ring	0.69 mm	97.2 %		110 mins.
Temple-ring	0.79 mm	94.9 %		104 mins.

48

ii



47

